Project Details

Project Name: MTSOLAR_8HIKCGL23B39D- Venkat-Carport-5x14

Location: Richardson, TX 75082, USA

Unique ID: 5P-19.75-6TOP-SD-45-L-5Hx14W-I631

Dealer: ______________________________

Date: Tue Jan 21 2025

Number of Modules: 70

Number of Poles: 5

Date Sold:

____

Array Dimensions N/S	17.29 ft
Array Dimensions E/W	94.50 ft
Winter Tilt Angle	5
Front Edge Clearance	10 ft

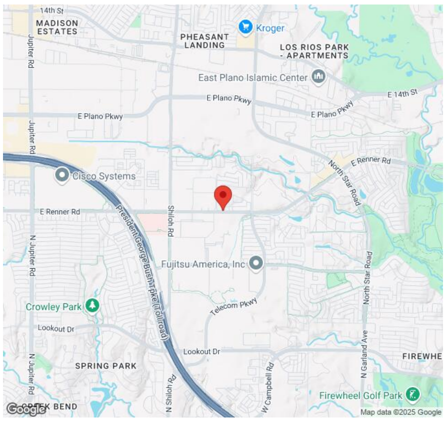
MT Solar Bill of Materials (5P-19.75-6TOP-SD-45-L-5Hx14W-I631)

Part	Short Description	BOM Qty
MTS-PC-6	6IN Pole Cap Assembly	5
MTS-HF-SD	H-Frame Assembly-SD	5
MTS-SD-Wing-45	45IN SD Wing	4
MTS-SD-Splice-90	90IN SD Splice	8
MTS-SD-Splice-57	57IN SD Splice	8
MTS-CLAMP-ANGLE-4PK	Angle Clamp	14

Rail Bill of Materials

Part	Qty
Rails (205in)	28
Rail Attachment	112
Module Mid Clamp	112
Module End Clamp	56
Ground Lug	14

Site Details:



Site Address: Richardson, TX 75082, USA

Array Specification

Duty Classification:	SD
Module Width:	41.00 in
Module Length:	80.00in
Number of Rows:	5
Number of Columns:	14
Total Number of Modules:	70
Winter Tilt Angle:	5
Front Edge Clearance:	10
Total Array Height at Tilt:	11.51 ft
Total Frame Length:	94.00 ft
Frame Weight:	4840 lbs
Array Dimensions N/S:	17.29 ft
Array Dimensions E/W:	94.50 ft
Rail Length:	207.50 in
Rail Spacing:	3.38 ft

Support Specifications

Pole Size:	6in Pipe Sch 40
Pole Length above Grade:	10.75 ft
Number of Poles:	5
Pole Spacing:	19.75 ft

Foundation Specifications

Foundation Type:	Square
Foundation Dimensions:	48 x 48 in
Foundation Depth (below grade):	Pile 1: 4.75 ft Pile 2: 5.00 ft Pile 3: 5.00 ft Pile 4: 5.00 ft Pile 5: 4.75 ft
Foundation Volume:	14.519 y^3

Site Info

Risk Category:	I
Exposure:	C
Soil Classification:	sand
Site Location:	Richardson, TX 75082, USA
Wind Speed:	101 mph

Snow Load:	5 psf

Design Disclaimer

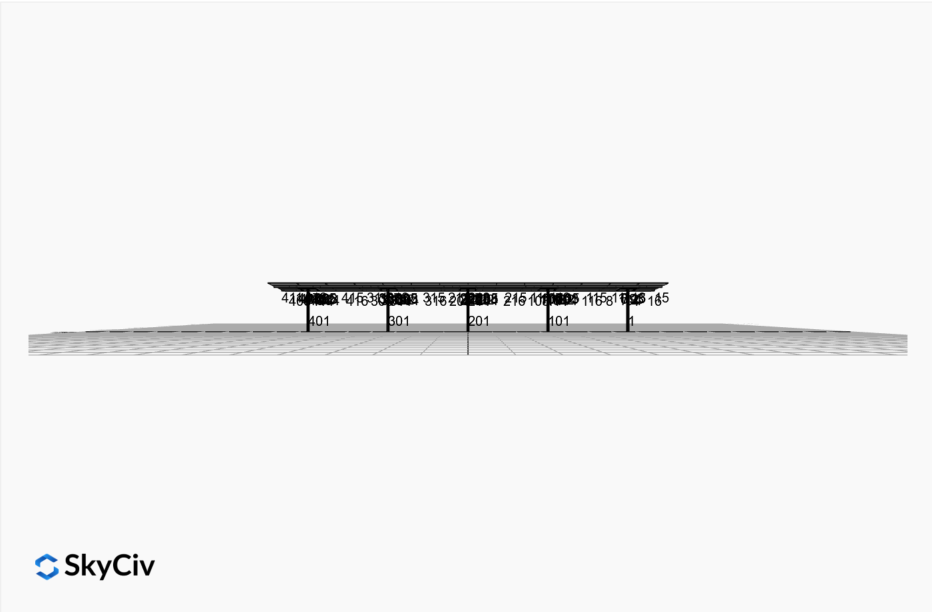
This software should be used for preliminary designs and should not be used as a final design unless reviewed, verified and designed by a qualified structural engineer.

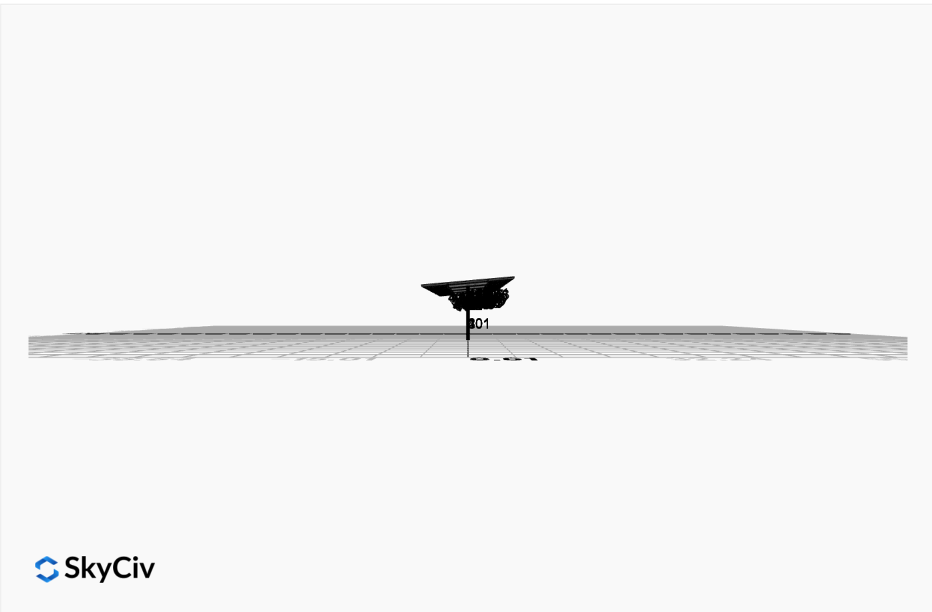
AutoDesigner Input

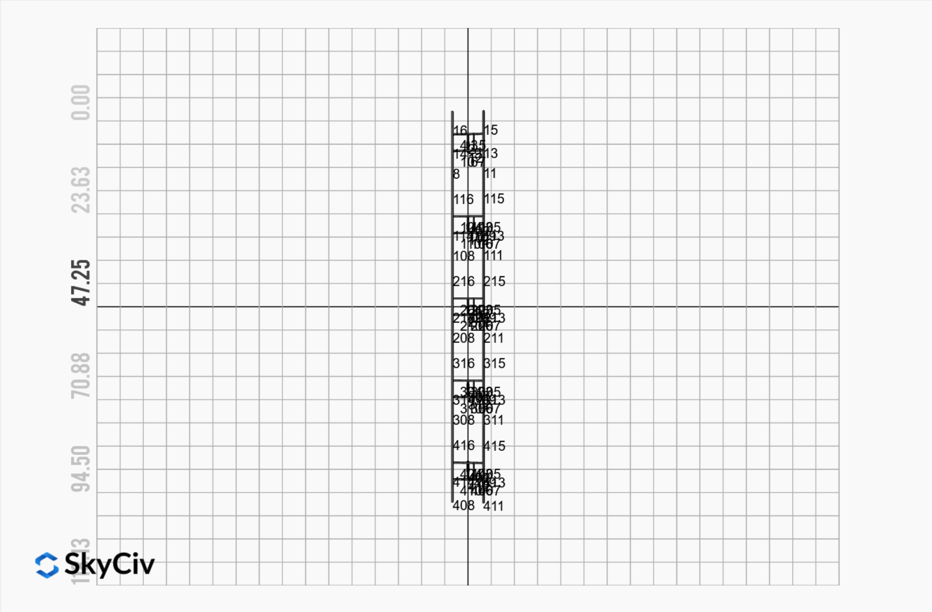
{"wind_speed_override":null,"snow_load_override":null,"direct_snow_load":false,"add_angle_brace":false,"product_type":"Beam","designer_name":"","designer_email":"contact@JeremyClemons.com","designer_phone":"","project_id":"MTSOLAR_8HIKCGL23B39D- Venkat-Carport-5x14","site_address":"Richardson, TX 75082, USA","module_width":41,"module_length":80,"number_rows":"5","number_columns":14,"pole_mount_section":"4_40","core_pipe_width":65,"core_pipe_section":"2_40","adjuster_section":"2_40","core_beam_height":65,"core_beam_section":"HSS3x2x1/8","main_pipe_section":"2_12GA","pole_spacing":"15","tilt_angle":5,"ground_clearance":10,"risk_category":"I","exposure_category":"C","frame_duty_override":"auto","pole_override":"auto","soil_type":"sand","customer_foundation_override":"48_Square","foundation_type":"Square","foundation_size":48,"check_rails":false}

Design Notes:

- AISC Deflection checks are set to L/1 due to structure design intent
- Foundation Soil Parameters used in this Autodesign are all estimates, proper geotechnical reports are required to confirm soil profiles
- Wind speeds, snow loads and other site specific results are based on ASCE 7 2016
- Steel frame design checks are based on AISC 360 2016 (LRFD)
- Foundation Design and Sizing is approximate only



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23.63
47.25
70.88
94.50
16
15
13
8
11
116
115
108
111
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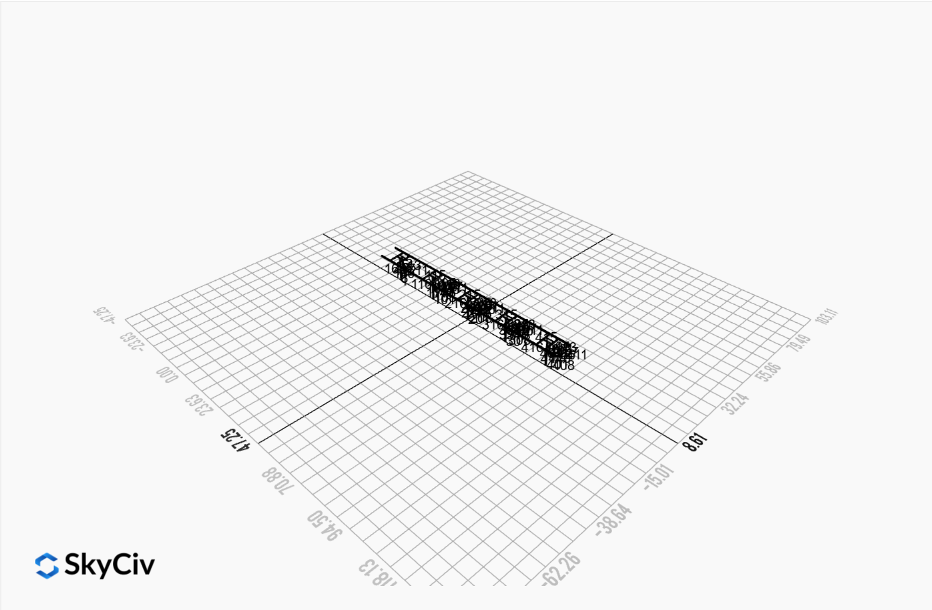
311
416
415
408
411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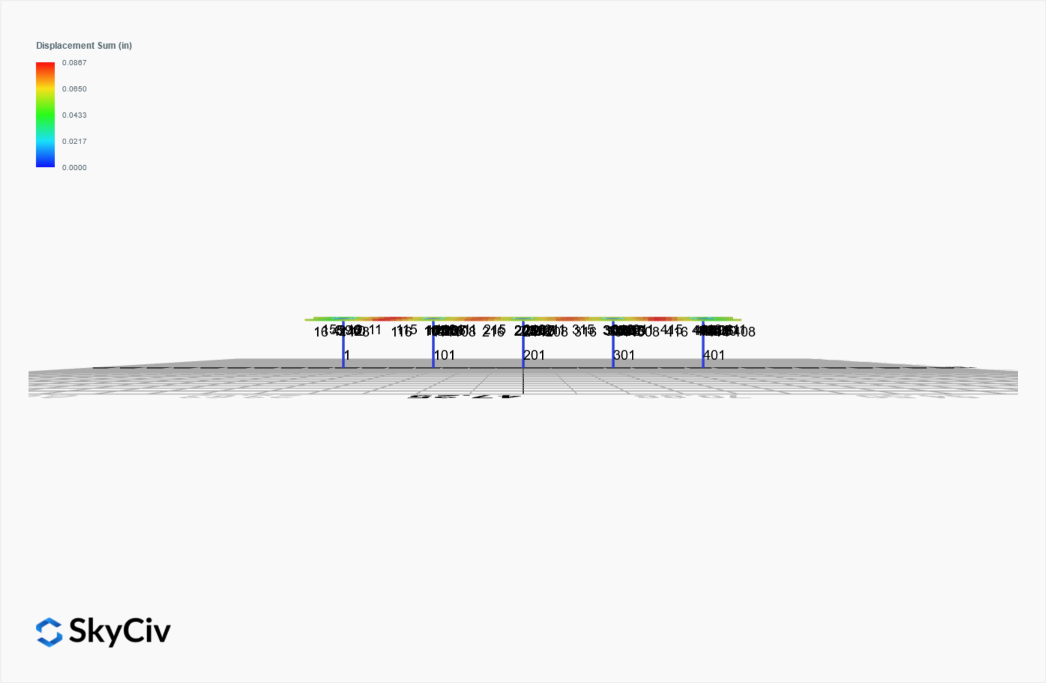
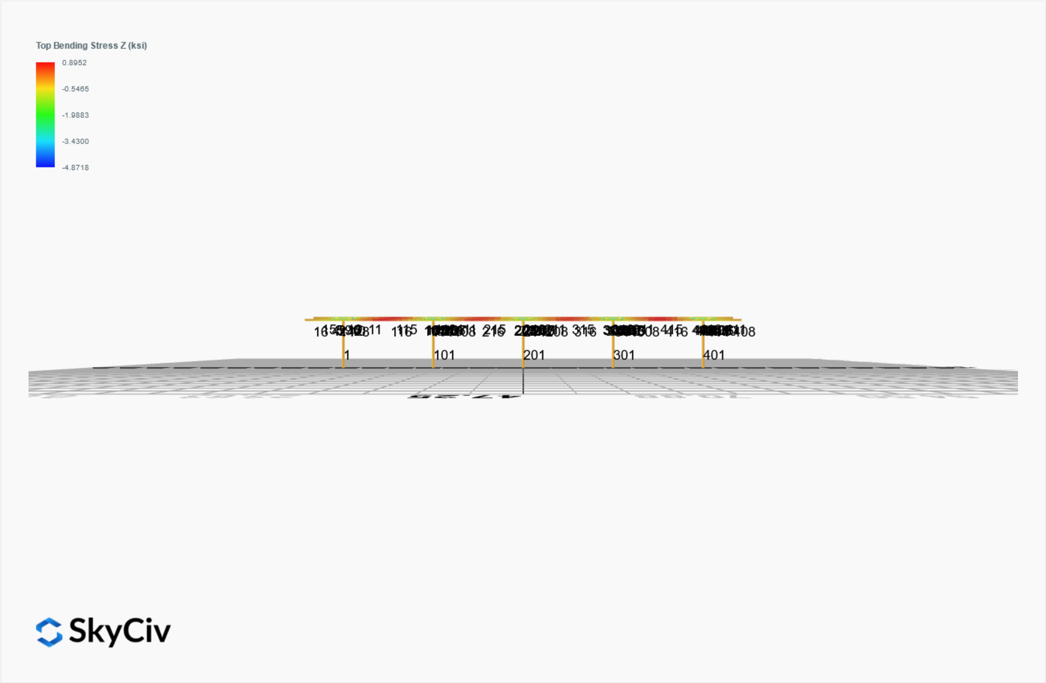
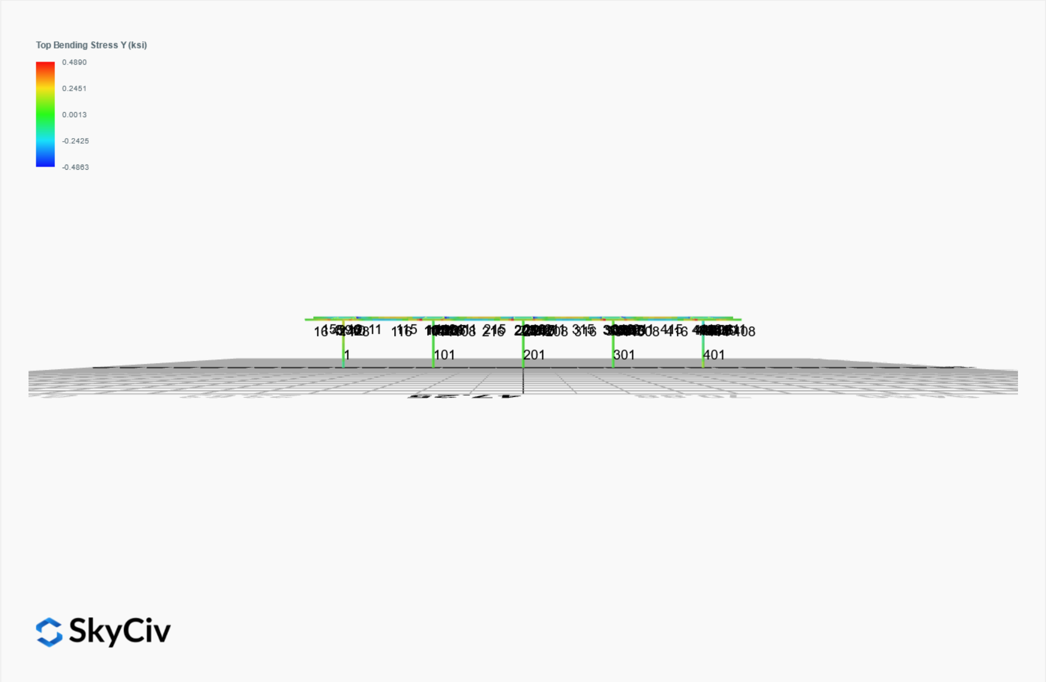
47.25
70.88
94.50
8.61
-15.01
-38.64
-62.26
32.24
55.86
79.49


401
301
201
101
1

FEM Results (Envelope Worst Case for each member)






Top Bending Stress Y (ksi)
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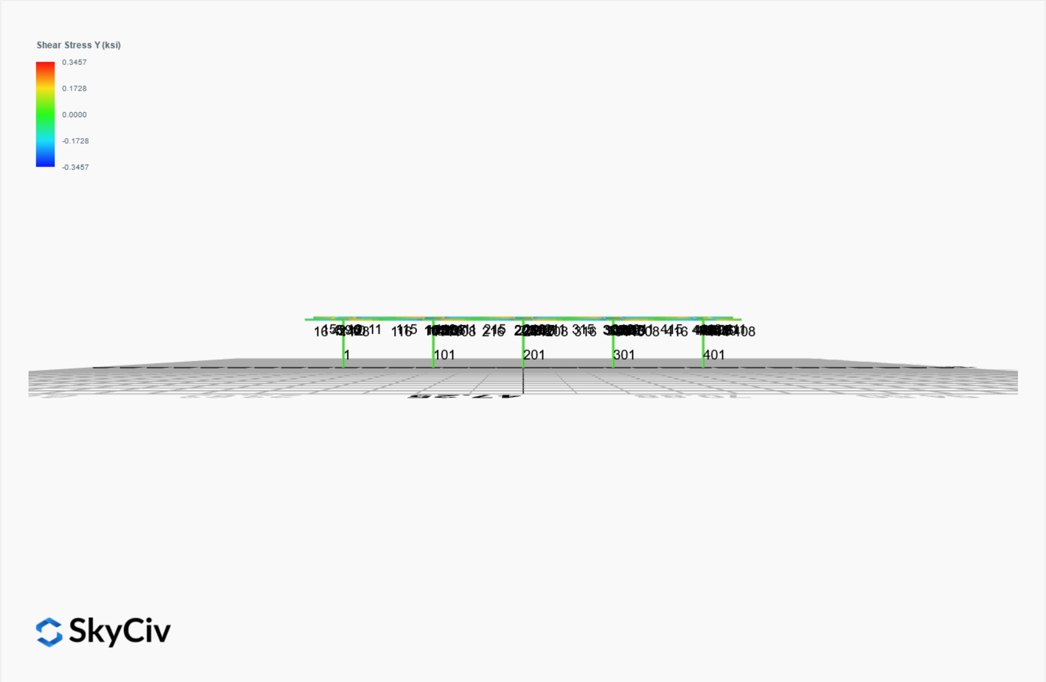
0.2451
0.0013
-0.2425
-0.4863
1
101
201
301
401
SkyCiv


Shear Stress Y (ksi)
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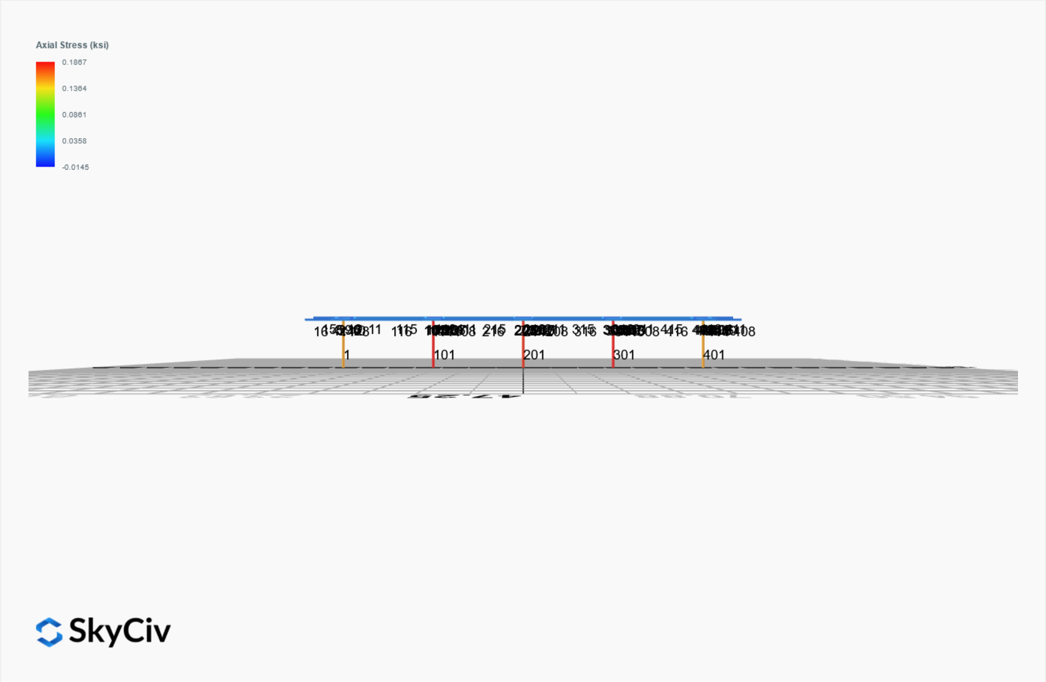
0.1728
0.0000
-0.1728
-0.3457
1
101
201
301
401
SkyCiv


Axial Stress (ksi)
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0.1364
0.0861
0.0358
-0.0145
1
101
201
301
401
SkyCiv

Reaction Forces for Foundation 1 (Node ID#1), (kip, kip-ft)

ASD Load Combination Results

Name	Fx	Fy	Fz	Mx	My	Mz
ULS: 1. D	0.0014	2.0115	0.0325	0.1074	-0.0035	0.0071
ULS: 2. D + L	0.0014	2.0115	0.0325	0.1074	-0.0035	0.0071
ULS: 3. D + (S or Lr or R)	0.0022	2.9050	0.0500	0.1654	-0.0053	-0.0003
ULS: 3. D + (S or Lr or R)	0.0014	2.0115	0.0325	0.1074	-0.0035	0.0071
ULS: 4. D + 0.75L + 0.75(S or Lr or R)	0.0020	2.6816	0.0457	0.1509	-0.0049	0.0016
ULS: 4. D + 0.75L + 0.75(S or Lr or R)	0.0014	2.0115	0.0325	0.1074	-0.0035	0.0071
ULS: 5b. D + 0.7E	0.0014	2.0115	0.0325	0.1074	-0.0035	0.0071
ULS: 6b. D + 0.75L + 0.75(0.7)E + 0.75S	0.0020	2.6816	0.0457	0.1509	-0.0049	0.0016
ULS: 8. 0.6D + 0.7E	0.0009	1.2069	0.0195	0.0644	-0.0021	0.0043
ULS: 5a. D + 0.6W_Wind downforce Case A only	-0.2616	4.9457	0.0912	0.3005	-0.0242	3.5124
ULS: 5a. D + 0.6W_Wind downforce Case B only	-0.2616	4.9457	0.0912	0.3005	-0.0242	3.5124
ULS: 5a. D + 0.6W_Wind uplift Case A only	0.0652	1.2201	0.0181	0.0597	-0.0029	2.3109
ULS: 5a. D + 0.6W_Wind uplift Case B only	0.1819	0.1477	-0.0070	-0.0210	0.0189	-8.4584
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case A only	-0.1953	4.8824	0.0897	0.2957	-0.0204	2.6305
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case B only	-0.1953	4.8824	0.0897	0.2957	-0.0204	2.6305
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case A only	0.0499	2.0881	0.0348	0.1152	-0.0044	1.7294
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case B only	0.1374	1.2838	0.0161	0.0546	0.0119	-6.3476
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case A only	-0.1959	4.2122	0.0765	0.2522	-0.0190	2.6361
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case B only	-0.1959	4.2122	0.0765	0.2522	-0.0190	2.6361
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case A only	0.0493	1.4180	0.0217	0.0716	-0.0030	1.7350
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case B only	0.1368	0.6136	0.0029	0.0111	0.0133	-6.3420
ULS: 7. 0.6D + 0.6W_Wind downforce Case A only	-0.2622	4.1412	0.0782	0.2575	-0.0228	3.5095
ULS: 7. 0.6D + 0.6W_Wind downforce Case B only	-0.2622	4.1412	0.0782	0.2575	-0.0228	3.5095
ULS: 7. 0.6D + 0.6W_Wind uplift Case A only	0.0646	0.4155	0.0051	0.0168	-0.0015	2.3080
ULS: 7. 0.6D + 0.6W_Wind uplift Case B only	0.1813	-0.6569	-0.0199	-0.0640	0.0203	-8.4613

Worst Case Reactions LRFD

These calculations are taken directly from the FEA via SkyCiv and are used in the Concrete Checks of the Foundatino Module.
Note: Worst case values are assumed as downforce wind load cases.

Result	Value (kip, kip-ft)
Axial	7.7510
Shear X	-0.4385
Shear Z	0.1461
Moment X	0.4823
Moment Y (Twist)	0.0400
Moment Z	14.5046

Worst Case Reactions ASD

These results are taken from the worst case values in the above table and are used in the Soil Checks in the Foundation Module.
Note: Worst case values are assumed as downforce wind load cases.

Result	Value (kip, kip-ft)
Axial	4.9457
Shear X	-0.2622
Shear Z	0.0912
Moment X	0.3005
Moment Y (Twist)	0.0242
Moment Z	8.4613

Reaction Forces for Foundation 2 (Node ID#101), (kip, kip-ft)

ASD Load Combination Results

Name	Fx	Fy	Fz	Mx	My	Mz
ULS: 1. D	-0.0016	2.2869	-0.0041	-0.0138	0.0010	0.0359
ULS: 2. D + L	-0.0016	2.2869	-0.0041	-0.0138	0.0010	0.0359
ULS: 3. D + (S or Lr or R)	-0.0024	3.3289	-0.0063	-0.0213	0.0016	0.0440
ULS: 3. D + (S or Lr or R)	-0.0016	2.2869	-0.0041	-0.0138	0.0010	0.0359
ULS: 4. D + 0.75L + 0.75(S or Lr or R)	-0.0022	3.0684	-0.0057	-0.0195	0.0014	0.0419

Name	Fx	Fy	Fz	Mx	My	Mz
ULS: 4. D + 0.75L + 0.75(S or Lr or R)	-0.0016	2.2869	-0.0041	-0.0138	0.0010	0.0359
ULS: 5b. D + 0.7E	-0.0016	2.2869	-0.0041	-0.0138	0.0010	0.0359
ULS: 6b. D + 0.75L + 0.75(0.7)E + 0.75S	-0.0022	3.0684	-0.0057	-0.0195	0.0014	0.0419
ULS: 8. 0.6D + 0.7E	-0.0009	1.3721	-0.0025	-0.0083	0.0006	0.0215
ULS: 5a. D + 0.6W_Wind downforce Case A only	-0.2952	5.7088	-0.0110	-0.0376	-0.0014	3.9421
ULS: 5a. D + 0.6W_Wind downforce Case B only	-0.2952	5.7088	-0.0110	-0.0376	-0.0014	3.9421
ULS: 5a. D + 0.6W_Wind uplift Case A only	0.0836	1.3627	-0.0015	-0.0056	-0.0037	2.4964
ULS: 5a. D + 0.6W_Wind uplift Case B only	0.1739	0.1157	-0.0008	-0.0017	0.0125	-9.1584
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case A only	-0.2224	5.6348	-0.0109	-0.0373	-0.0004	2.9716
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case B only	-0.2224	5.6348	-0.0109	-0.0373	-0.0004	2.9716
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case A only	0.0617	2.3753	-0.0038	-0.0133	-0.0021	1.8873
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case B only	0.1294	1.4401	-0.0033	-0.0103	0.0100	-6.8537
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case A only	-0.2218	4.8533	-0.0092	-0.0316	-0.0008	2.9656
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case B only	-0.2218	4.8533	-0.0092	-0.0316	-0.0008	2.9656
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case A only	0.0623	1.5938	-0.0022	-0.0077	-0.0025	1.8813
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case B only	0.1300	0.6585	-0.0017	-0.0047	0.0096	-6.8598
ULS: 7. 0.6D + 0.6W_Wind downforce Case A only	-0.2946	4.7940	-0.0093	-0.0320	-0.0018	3.9277
ULS: 7. 0.6D + 0.6W_Wind downforce Case B only	-0.2946	4.7940	-0.0093	-0.0320	-0.0018	3.9277
ULS: 7. 0.6D + 0.6W_Wind uplift Case A only	0.0842	0.4480	0.0001	-0.0001	-0.0041	2.4821
ULS: 7. 0.6D + 0.6W_Wind uplift Case B only	0.1745	-0.7990	0.0008	0.0039	0.0121	-9.1727

Worst Case Reactions LRFD

These calculations are taken directly from the FEA via SkyCiv and are used in the Concrete Checks of the Foundatino Module.
Note: Worst case values are assumed as downforce wind load cases.

Result	Value (kip, kip-ft)
Axial	8.9685
Shear X	-0.4912
Shear Z	-0.0175
Moment X	-0.0602
Moment Y (Twist)	0.0216
Moment Z	15.7408

Worst Case Reactions ASD

These results are taken from the worst case values in the above table and are used in the Soil Checks in the Foundation Module.
Note: Worst case values are assumed as downforce wind load cases.

Result	Value (kip, kip-ft)
Axial	5.7088
Shear X	-0.2952
Shear Z	-0.0110
Moment X	-0.0376
Moment Y (Twist)	0.0125
Moment Z	9.1727

Reaction Forces for Foundation 3 (Node ID#201), (kip, kip-ft)

ASD Load Combination Results

Name	Fx	Fy	Fz	Mx	My	Mz
ULS: 1. D	0.0002	2.2560	-0.0000	0.0000	0.0000	0.0216
ULS: 2. D + L	0.0002	2.2560	-0.0000	0.0000	0.0000	0.0216
ULS: 3. D + (S or Lr or R)	0.0003	3.2814	-0.0000	0.0000	0.0000	0.0219
ULS: 3. D + (S or Lr or R)	0.0002	2.2560	-0.0000	0.0000	0.0000	0.0216
ULS: 4. D + 0.75L + 0.75(S or Lr or R)	0.0003	3.0250	-0.0000	0.0000	0.0000	0.0218
ULS: 4. D + 0.75L + 0.75(S or Lr or R)	0.0002	2.2560	-0.0000	0.0000	0.0000	0.0216
ULS: 5b. D + 0.7E	0.0002	2.2560	-0.0000	0.0000	0.0000	0.0216
ULS: 6b. D + 0.75L + 0.75(0.7)E + 0.75S	0.0003	3.0250	-0.0000	0.0000	0.0000	0.0218
ULS: 8. 0.6D + 0.7E	0.0001	1.3536	-0.0000	0.0000	0.0000	0.0130
ULS: 5a. D + 0.6W_Wind downforce Case A only	-0.2932	5.6236	-0.0000	-0.0000	0.0000	3.9540
ULS: 5a. D + 0.6W_Wind downforce Case B only	-0.2932	5.6236	-0.0000	-0.0000	0.0000	3.9540
ULS: 5a. D + 0.6W_Wind uplift Case A only	0.0820	1.3480	-0.0000	0.0000	0.0000	2.5453
ULS: 5a. D + 0.6W_Wind uplift Case B only	0.1817	0.1165	-0.0000	0.0000	0.0000	-9.3213

Name	Fx	Fy	Fz	Mx	My	Mz
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case A only	-0.2197	5.5507	-0.0000	-0.0000	0.0000	2.9711
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case B only	-0.2197	5.5507	-0.0000	-0.0000	0.0000	2.9711
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case A only	0.0616	2.3440	-0.0000	0.0000	0.0000	1.9146
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case B only	0.1364	1.4204	-0.0000	0.0000	0.0000	-6.9853
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case A only	-0.2198	4.7817	-0.0000	-0.0000	0.0000	2.9709
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case B only	-0.2198	4.7817	-0.0000	-0.0000	0.0000	2.9709
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case A only	0.0615	1.5750	-0.0000	0.0000	0.0000	1.9144
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case B only	0.1363	0.6514	-0.0000	0.0000	0.0000	-6.9856
ULS: 7. 0.6D + 0.6W_Wind downforce Case A only	-0.2933	4.7212	-0.0000	-0.0000	0.0000	3.9454
ULS: 7. 0.6D + 0.6W_Wind downforce Case B only	-0.2933	4.7212	-0.0000	-0.0000	0.0000	3.9454
ULS: 7. 0.6D + 0.6W_Wind uplift Case A only	0.0819	0.4456	-0.0000	0.0000	0.0000	2.5367
ULS: 7. 0.6D + 0.6W_Wind uplift Case B only	0.1816	-0.7859	-0.0000	0.0000	0.0000	-9.3299

Worst Case Reactions LRFD

These calculations are taken directly from the FEA via SkyCiv and are used in the Concrete Checks of the Foundatino Module.
Note: Worst case values are assumed as downforce wind load cases.

Result	Value (kip, kip-ft)
Axial	8.8325
Shear X	-0.4890
Shear Z	-0.0000
Moment X	0.0000
Moment Y (Twist)	0.0000
Moment Z	16.0214

Worst Case Reactions ASD

These results are taken from the worst case values in the above table and are used in the Soil Checks in the Foundation Module.
Note: Worst case values are assumed as downforce wind load cases.

Result	Value (kip, kip-ft)
Axial	5.6236
Shear X	-0.2933
Shear Z	-0.0000
Moment X	-0.0000
Moment Y (Twist)	0.0000
Moment Z	9.3299

Reaction Forces for Foundation 4 (Node ID#301), (kip, kip-ft)

ASD Load Combination Results

Name	Fx	Fy	Fz	Mx	My	Mz
ULS: 1. D	-0.0016	2.2869	0.0041	0.0138	-0.0010	0.0359
ULS: 2. D + L	-0.0016	2.2869	0.0041	0.0138	-0.0010	0.0359
ULS: 3. D + (S or Lr or R)	-0.0024	3.3289	0.0063	0.0213	-0.0016	0.0440
ULS: 3. D + (S or Lr or R)	-0.0016	2.2869	0.0041	0.0138	-0.0010	0.0359
ULS: 4. D + 0.75L + 0.75(S or Lr or R)	-0.0022	3.0684	0.0057	0.0195	-0.0014	0.0419
ULS: 4. D + 0.75L + 0.75(S or Lr or R)	-0.0016	2.2869	0.0041	0.0138	-0.0010	0.0359
ULS: 5b. D + 0.7E	-0.0016	2.2869	0.0041	0.0138	-0.0010	0.0359
ULS: 6b. D + 0.75L + 0.75(0.7)E + 0.75S	-0.0022	3.0684	0.0057	0.0195	-0.0014	0.0419
ULS: 8. 0.6D + 0.7E	-0.0009	1.3721	0.0025	0.0083	-0.0006	0.0215
ULS: 5a. D + 0.6W_Wind downforce Case A only	-0.2952	5.7088	0.0110	0.0376	0.0014	3.9421
ULS: 5a. D + 0.6W_Wind downforce Case B only	-0.2952	5.7088	0.0110	0.0376	0.0014	3.9421
ULS: 5a. D + 0.6W_Wind uplift Case A only	0.0836	1.3627	0.0015	0.0056	0.0037	2.4964
ULS: 5a. D + 0.6W_Wind uplift Case B only	0.1739	0.1157	0.0008	0.0017	-0.0125	-9.1584
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case A only	-0.2224	5.6348	0.0109	0.0373	0.0004	2.9716
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case B only	-0.2224	5.6348	0.0109	0.0373	0.0004	2.9716
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case A only	0.0617	2.3753	0.0038	0.0133	0.0021	1.8873
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case B only	0.1294	1.4401	0.0033	0.0103	-0.0100	-6.8537
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case A only	-0.2218	4.8533	0.0092	0.0316	0.0008	2.9656
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case B only	-0.2218	4.8533	0.0092	0.0316	0.0008	2.9656
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case A only	0.0623	1.5938	0.0022	0.0077	0.0025	1.8813
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case B only	0.1300	0.6585	0.0017	0.0047	-0.0096	-6.8598

Name	Fx	Fy	Fz	Mx	My	Mz
ULS: 7. 0.6D + 0.6W_Wind downforce Case A only	-0.2946	4.7940	0.0093	0.0320	0.0018	3.9277
ULS: 7. 0.6D + 0.6W_Wind downforce Case B only	-0.2946	4.7940	0.0093	0.0320	0.0018	3.9277
ULS: 7. 0.6D + 0.6W_Wind uplift Case A only	0.0842	0.4480	-0.0001	0.0001	0.0041	2.4821
ULS: 7. 0.6D + 0.6W_Wind uplift Case B only	0.1745	-0.7990	-0.0008	-0.0039	-0.0121	-9.1727

Worst Case Reactions LRFD

These calculations are taken directly from the FEA via SkyCiv and are used in the Concrete Checks of the Foundatino Module.
Note: Worst case values are assumed as downforce wind load cases.

Result	Value (kip, kip-ft)
Axial	8.9685
Shear X	-0.4912
Shear Z	0.0175
Moment X	0.0602
Moment Y (Twist)	0.0216
Moment Z	15.7408

Worst Case Reactions ASD

These results are taken from the worst case values in the above table and are used in the Soil Checks in the Foundation Module.
Note: Worst case values are assumed as downforce wind load cases.

Result	Value (kip, kip-ft)
Axial	5.7088
Shear X	-0.2952
Shear Z	0.0110
Moment X	0.0376
Moment Y (Twist)	0.0125
Moment Z	9.1727

Reaction Forces for Foundation 5 (Node ID#401), (kip, kip-ft)

ASD Load Combination Results

Name	Fx	Fy	Fz	Mx	My	Mz
ULS: 1. D	0.0014	2.0115	-0.0325	-0.1074	0.0035	0.0071
ULS: 2. D + L	0.0014	2.0115	-0.0325	-0.1074	0.0035	0.0071
ULS: 3. D + (S or Lr or R)	0.0022	2.9050	-0.0500	-0.1654	0.0053	-0.0003
ULS: 3. D + (S or Lr or R)	0.0014	2.0115	-0.0325	-0.1074	0.0035	0.0071
ULS: 4. D + 0.75L + 0.75(S or Lr or R)	0.0020	2.6816	-0.0457	-0.1509	0.0049	0.0016
ULS: 4. D + 0.75L + 0.75(S or Lr or R)	0.0014	2.0115	-0.0325	-0.1074	0.0035	0.0071
ULS: 5b. D + 0.7E	0.0014	2.0115	-0.0325	-0.1074	0.0035	0.0071
ULS: 6b. D + 0.75L + 0.75(0.7)E + 0.75S	0.0020	2.6816	-0.0457	-0.1509	0.0049	0.0016
ULS: 8. 0.6D + 0.7E	0.0009	1.2069	-0.0195	-0.0644	0.0021	0.0043
ULS: 5a. D + 0.6W_Wind downforce Case A only	-0.2616	4.9457	-0.0912	-0.3005	0.0242	3.5124
ULS: 5a. D + 0.6W_Wind downforce Case B only	-0.2616	4.9457	-0.0912	-0.3005	0.0242	3.5124
ULS: 5a. D + 0.6W_Wind uplift Case A only	0.0652	1.2201	-0.0181	-0.0597	0.0029	2.3109
ULS: 5a. D + 0.6W_Wind uplift Case B only	0.1819	0.1477	0.0070	0.0210	-0.0189	-8.4584
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case A only	-0.1953	4.8824	-0.0897	-0.2957	0.0204	2.6305
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case B only	-0.1953	4.8824	-0.0897	-0.2957	0.0204	2.6305
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case A only	0.0499	2.0881	-0.0348	-0.1152	0.0044	1.7294
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case B only	0.1374	1.2838	-0.0161	-0.0546	-0.0119	-6.3476
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case A only	-0.1959	4.2122	-0.0765	-0.2522	0.0190	2.6361
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case B only	-0.1959	4.2122	-0.0765	-0.2522	0.0190	2.6361
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case A only	0.0493	1.4180	-0.0217	-0.0716	0.0030	1.7350
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case B only	0.1368	0.6136	-0.0029	-0.0111	-0.0133	-6.3420
ULS: 7. 0.6D + 0.6W_Wind downforce Case A only	-0.2622	4.1412	-0.0782	-0.2575	0.0228	3.5095
ULS: 7. 0.6D + 0.6W_Wind downforce Case B only	-0.2622	4.1412	-0.0782	-0.2575	0.0228	3.5095
ULS: 7. 0.6D + 0.6W_Wind uplift Case A only	0.0646	0.4155	-0.0051	-0.0168	0.0015	2.3080
ULS: 7. 0.6D + 0.6W_Wind uplift Case B only	0.1813	-0.6569	0.0199	0.0640	-0.0203	-8.4613

Worst Case Reactions LRFD

These calculations are taken directly from the FEA via SkyCiv and are used in the Concrete Checks of the Foundatino Module.
Note: Worst case values are assumed as downforce wind load cases.

Worst Case Reactions ASD

These results are taken from the worst case values in the above table and are used in the Soil Checks in the Foundation Module.
Note: Worst case values are assumed as downforce wind load cases.

Result	Value (kip, kip-ft)
Axial	7.7510
Shear X	-0.4385
Shear Z	-0.1461
Moment X	-0.4823
Moment Y (Twist)	0.0400
Moment Z	14.5047

Result	Value (kip, kip-ft)
Axial	4.9457
Shear X	-0.2622
Shear Z	-0.0912
Moment X	-0.3005
Moment Y (Twist)	0.0242
Moment Z	8.4613

Project Details

Design Code: AISC 360-16 LRFD
Provision: LRFD
Country: United States

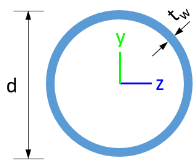
User Name: sales@mtsolar.us
Unit System: imperial

Design Input Information

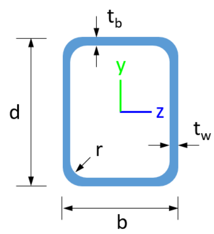
Design Factors			
Φ_t	Φ_c	Φ_b	Φ_v
0.9	0.9	0.9	0.9

Design Materials			
ID	E (ksi)	F_y (ksi)	F_u (ksi)
1	29000	50	65

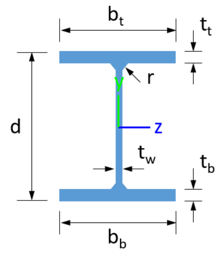
Section Dimensions



ID	Name	d (in)	t_w (in)					
1	2in Pipe Sch 40	2.38	0.15					
4	4in Pipe Sch 40	4.50	0.24					
7	6in Pipe Sch 40	6.63	0.28					



ID	Name	d (in)	b (in)	t_w (in)	t_b (in)	r (in)		
15	HSS5x3x1/8	5.00	3.00	0.12	0.12	0.12		



ID	Name	d (in)	t_w (in)	b_t (in)	b_b (in)	t_t (in)	t_b (in)	r (in)
18	W6x9	5.90	0.17	3.94	3.94	0.21	0.21	0.25

Section Properties								
ID	Name	A (in^2)	J (in^4)	I_{yp} (in^4)	I_{zp} (in^4)	I_w (in^6)	S_{yp} (in^3)	S_{zp} (in^3)

1	2in Pipe Sch 40	1.07	1.33	0.67	0.67	0.00	0.76	0.76
4	4in Pipe Sch 40	3.17	14.47	7.23	7.23	0.00	4.31	4.31
7	6in Pipe Sch 40	5.58	56.28	28.14	28.14	0.00	11.28	11.28
15	HSS5x3x1/8	1.77	6.02	2.75	6.03	0.51	2.07	2.93
18	W6x9	2.68	0.04	2.20	16.40	17.70	1.72	6.23

Member Properties

Member ID	Section ID	K_zL (ft)	K_yL (ft)	L_b(ft)	C_b	LST	LSC	LD
1	7	22.58	22.58	10.75	-	300	200	1
2	4	1.30	1.30	2.00	-	300	200	1
3	15	0.92	0.92	1.42	1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.17,1.18,1.18,1.18,1.17,1.18,1.18,1.18,1.22,1.18,1.18,1.18,1.16,1.18,1.18,1.18,1.17	300	200	1
4	15	2.44	2.44	3.75	1.68,1.68,1.68,1.67,1.68,1.68,1.67,1.67,1.53,1.68,1.67,1.67,1.62,1.68,1.67,1.67,1.68,1.67,1.67,1.67,1.71,1.68,1.67,1.67,1.65,1.68	300	200	1
5	15	1.52	1.52	2.33	1.67,1.67,1.67,1.67,1.67,1.67,1.67,1.67,1.67,1.66,1.67,1.67,1.67,1.66,1.67,1.67,1.67,1.71,1.67,1.67,1.67,1.65,1.67,1.67,1.67,1.66	300	200	1
6	15	0.92	0.92	1.42	1.19,1.18,1.19,1.18,1.19,1.19,1.18,1.18,1.19,1.18,1.18,1.18,1.19,1.18,1.18,1.18,1.18,1.21,1.18,1.18,1.19,1.17,1.18,1.18,1.19,1.18	300	200	1
7	15	1.52	1.52	2.33	1.67,1.67,1.67,1.67,1.67,1.67,1.67,1.67,1.67,1.66,1.67,1.67,1.67,1.66,1.67,1.67,1.67,1.71,1.67,1.67,1.67,1.65,1.67,1.67,1.67,1.66	300	200	1
8	18	1.33	1.33	2.05	1.73,1.73,1.73,1.74,1.73,1.73,1.72,1.72,1.93,2.07,1.72,1.72,2.10,2.09,1.72,1.72,1.66,1.87,1.72,1.72,1.54,2.01,1.72,1.72,2.06,2.12	300	200	1
9	1	2.60	2.60	4.00	-	300	200	1
10	15	2.44	2.44	3.75	1.68,1.68,1.68,1.67,1.68,1.68,1.67,1.67,1.54,1.68,1.67,1.67,1.63,1.68,1.67,1.67,1.68,1.67,1.67,1.67,1.70,1.68,1.67,1.67,1.65,1.68	300	200	1
11	18	1.33	1.33	2.05	1.75,1.75,1.75,1.75,1.75,1.75,1.78,1.78,1.93,2.06,1.78,1.78,1.98,2.04,1.77,1.77,1.81,1.23,1.77,1.77,1.85,2.09,1.78,1.78,2.06,2.00	300	200	1
12	4	1.30	1.30	2.00	-	300	200	1
13	18	4.88	4.00	7.50	1.11,1.11,1.11,1.11,1.11,1.11,1.11,1.11,1.12,1.12,1.11,1.11,1.12,1.12,1.11,1.11,1.11,1.06,1.11,1.11,1.11,1.22,1.11,1.11,1.12,1.12	300	200	1
14	18	4.88	4.00	7.50	1.11,1.11,1.11,1.11,1.11,1.11,1.11,1.11,2.62,1.17,1.11,1.11,1.35,1.23,1.11,1.11,1.10,1.12,1.11,1.11,1.08,1.13,1.11,1.11,1.15,1.36	300	200	1
15	18	7.88	7.88	3.75	2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33	300	200	1
16	18	7.88	7.88	3.75	2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33	300	200	1
101	7	22.58	22.58	10.75	-	300	200	1
102	4	1.30	1.30	2.00	-	300	200	1
103	15	0.92	0.92	1.42	1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.17,1.18,1.18,1.18,1.17,1.18,1.18,1.18,1.21,1.18,1.18,1.18,1.16,1.18,1.18,1.18,1.18	300	200	1
104	15	2.44	2.44	3.75	1.68,1.68,1.68,1.67,1.68,1.68,1.67,1.67,1.52,1.68,1.67,1.67,1.63,1.68,1.67,1.67,1.68,1.67,1.67,1.67,1.70,1.68,1.67,1.67,1.65,1.68	300	200	1
105	15	1.52	1.52	2.33	1.67,1.67,1.67,1.67,1.67,1.67,1.67,1.67,1.67,1.66,1.67,1.67,1.67,1.66,1.67,1.67,1.67,1.70,1.67,1.67,1.67,1.65,1.67,1.67,1.67,1.66	300	200	1
106	15	0.92	0.92	1.42	1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.20,1.18,1.18,1.18,1.17,1.18,1.18,1.18,1.18	300	200	1
107	15	1.52	1.52	2.33	1.67,1.67,1.67,1.67,1.67,1.67,1.67,1.67,1.67,1.66,1.67,1.67,1.67,1.66,1.67,1.67,1.67,1.70,1.67,1.67,1.67,1.65,1.67,1.67,1.67,1.66	300	200	1
108	18	1.33	1.33	2.05	2.09,2.09,2.09,2.09,2.09,2.09,2.10,2.10,1.82,2.07,2.10,2.10,2.07,2.07,2.10,2.10,2.10,2.09,2.10,2.10,2.11,2.08,2.10,2.10,2.08,2.06	300	200	1
109	1	2.60	2.60	4.00	-	300	200	1
110	15	2.44	2.44	3.75	1.68,1.68,1.68,1.67,1.68,1.68,1.67,1.67,1.55,1.68,1.67,1.67,1.63,1.68,1.67,1.67,1.68,1.67,1.67,1.67,1.70,1.68,1.67,1.67,1.65,1.68	300	200	1
111	18	1.33	1.33	2.05	2.09,2.09,2.09,2.09,2.09,2.09,2.09,2.09,2.08,2.08,2.09,2.09,2.08,2.08,2.09,2.09,2.09,2.27,2.09,2.09,2.09,2.07,2.09,2.09,2.08,2.08	300	200	1
112	4	1.30	1.30	2.00	-	300	200	1

113	18	4.88	4.00	7.50	1.04,1.04,1.04,1.04,1.04,1.04,1.04,1.04,1.06,1.12,1.04,1.04,1.08,1.10,1.04,1.04,1.04,1.03,1.04,1.04,1.05,1.26,1.04,1.04,1.12,1.09	300	200	1
114	18	4.88	4.00	7.50	1.04,1.04,1.04,1.04,1.04,1.04,1.04,1.04,1.87,1.20,1.04,1.04,1.42,1.27,1.04,1.04,1.04,1.05,1.04,1.04,1.03,1.09,1.04,1.04,1.17,1.47	300	200	1
115	18	6.63	6.63	10.20	1.16,1.16,1.16,1.16,1.16,1.16,1.16,1.16,1.15,1.14,1.16,1.16,1.14,1.14,1.16,1.16,1.15,1.30,1.16,1.16,1.15,1.12,1.16,1.16,1.14,1.14	300	200	1
116	18	6.63	6.63	10.20	1.16,1.16,1.16,1.16,1.16,1.16,1.16,1.16,1.11,1.13,1.16,1.16,1.12,1.13,1.16,1.16,1.16,1.15,1.16,1.16,1.18,1.14,1.16,1.16,1.14,1.11	300	200	1
201	7	22.58	22.58	10.75	-	300	200	1
202	4	1.30	1.30	2.00	-	300	200	1
203	15	0.92	0.92	1.42	1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.17,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.21,1.18,1.18,1.18,1.17,1.18,1.18,1.18,1.18	300	200	1
204	15	2.44	2.44	3.75	1.68,1.68,1.68,1.67,1.68,1.68,1.67,1.67,1.55,1.68,1.67,1.67,1.63,1.68,1.67,1.67,1.68,1.67,1.67,1.67,1.70,1.68,1.67,1.67,1.65,1.68	300	200	1
205	15	1.52	1.52	2.33	1.67,1.67,1.67,1.67,1.67,1.67,1.67,1.67,1.67,1.66,1.67,1.67,1.67,1.66,1.67,1.67,1.67,1.70,1.67,1.67,1.67,1.65,1.67,1.67,1.67,1.66	300	200	1
206	15	0.92	0.92	1.42	1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.17,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.21,1.18,1.18,1.18,1.17,1.18,1.18,1.18,1.18	300	200	1
207	15	1.52	1.52	2.33	1.67,1.67,1.67,1.67,1.67,1.67,1.67,1.67,1.67,1.66,1.67,1.67,1.67,1.66,1.67,1.67,1.67,1.70,1.67,1.67,1.67,1.65,1.67,1.67,1.67,1.66	300	200	1
208	18	1.33	1.33	2.05	2.08,2.08,2.08,2.08,2.08,2.08,2.08,2.08,2.31,2.09,2.08,2.08,2.11,2.10,2.08,2.08,2.08,2.09,2.08,2.08,2.07,2.09,2.08,2.08,2.10,2.11	300	200	1
209	1	2.60	2.60	4.00	-	300	200	1
210	15	2.44	2.44	3.75	1.68,1.68,1.68,1.67,1.68,1.68,1.67,1.67,1.55,1.68,1.67,1.67,1.63,1.68,1.67,1.67,1.68,1.67,1.67,1.67,1.70,1.68,1.67,1.67,1.65,1.68	300	200	1
211	18	1.33	1.33	2.05	2.08,2.08,2.08,2.08,2.08,2.08,2.08,2.08,2.09,2.09,2.08,2.08,2.09,2.09,2.08,2.08,2.09,2.06,2.08,2.08,2.09,2.09,2.08,2.08,2.09,2.09	300	200	1
212	4	1.30	1.30	2.00	-	300	200	1
213	18	4.88	4.00	7.50	1.04,1.04,1.04,1.04,1.04,1.04,1.04,1.04,1.04,1.08,1.04,1.04,1.06,1.07,1.04,1.04,1.04,1.03,1.04,1.04,1.04,1.17,1.04,1.04,1.09,1.06	300	200	1
214	18	4.88	4.00	7.50	1.04,1.04,1.04,1.04,1.04,1.04,1.04,1.04,2.83,1.14,1.04,1.04,1.29,1.19,1.04,1.04,1.04,1.04,1.04,1.04,1.03,1.06,1.04,1.04,1.13,1.29	300	200	1
215	18	6.63	6.63	10.20	1.16,1.16,1.16,1.16,1.16,1.16,1.16,1.16,1.16,1.16,1.16,1.16,1.16,1.16,1.16,1.16,1.16,1.14,1.16,1.16,1.16,1.16,1.16,1.16,1.16,1.16	300	200	1
216	18	6.63	6.63	10.20	1.15,1.15,1.15,1.15,1.15,1.15,1.15,1.15,1.20,1.16,1.15,1.15,1.17,1.16,1.15,1.15,1.15,1.16,1.15,1.15,1.15,1.16,1.15,1.15,1.16,1.17	300	200	1
301	7	22.58	22.58	10.75	-	300	200	1
302	4	1.30	1.30	2.00	-	300	200	1
303	15	0.92	0.92	1.42	1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.20,1.18,1.18,1.18,1.17,1.18,1.18,1.18,1.18	300	200	1
304	15	2.44	2.44	3.75	1.68,1.68,1.68,1.67,1.68,1.68,1.67,1.67,1.55,1.68,1.67,1.67,1.63,1.68,1.67,1.67,1.68,1.67,1.67,1.67,1.70,1.68,1.67,1.67,1.65,1.68	300	200	1
305	15	1.52	1.52	2.33	1.67,1.67,1.67,1.67,1.67,1.67,1.67,1.67,1.67,1.66,1.67,1.67,1.67,1.66,1.67,1.67,1.67,1.70,1.67,1.67,1.67,1.65,1.67,1.67,1.67,1.66	300	200	1
306	15	0.92	0.92	1.42	1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.17,1.18,1.18,1.18,1.17,1.18,1.18,1.18,1.21,1.18,1.18,1.18,1.16,1.18,1.18,1.18,1.18	300	200	1
307	15	1.52	1.52	2.33	1.67,1.67,1.67,1.67,1.67,1.67,1.67,1.67,1.67,1.66,1.67,1.67,1.67,1.66,1.67,1.67,1.67,1.70,1.67,1.67,1.67,1.65,1.67,1.67,1.67,1.66	300	200	1
308	18	1.33	1.33	2.05	2.08,2.08,2.08,2.08,2.08,2.08,2.09,2.09,1.34,1.88,2.09,2.09,1.79,1.80,2.08,2.08,2.09,2.07,2.09,2.09,2.12,2.05,2.09,2.09,2.00,1.67	300	200	1
309	1	2.60	2.60	4.00	-	300	200	1
310	15	2.44	2.44	3.75	1.68,1.68,1.68,1.67,1.68,1.68,1.67,1.67,1.52,1.68,1.67,1.67,1.63,1.68,1.67,1.67,1.68,1.67,1.67,1.67,1.70,1.68,1.67,1.67,1.65,1.68	300	200	1
311	18	1.33	1.33	2.05	2.08,2.08,2.08,2.08,2.08,2.08,2.08,2.08,2.06,1.99,2.08,2.08,2.06,2.03,2.08,2.08,2.08,2.00,2.08,2.08,2.07,1.78,2.08,2.08,2.01,2.06	300	200	1
312	4	1.30	1.30	2.00	-	300	200	1
313	18	4.88	4.00	7.50	1.04,1.04,1.04,1.04,1.04,1.04,1.04,1.04,1.06,1.12,1.04,1.04,1.08,1.10,1.04,1.04,1.04,1.03,1.04,1.04,1.05,1.26,1.04,1.04,1.12,1.09	300	200	1
314	18	4.88	4.00	7.50	1.04,1.04,1.04,1.04,1.04,1.04,1.04,1.04,1.87,1.20,1.04,1.04,1.42,1.28,1.04,1.04,1.04,1.05,1.04,1.04,1.03,1.09,1.04,1.04,1.17,1.47	300	200	1

315	18	6.63	6.63	10.20	1.16,1.16,1.16,1.16,1.16,1.16,1.16,1.16,1.16,1.15,1.16,1.16,1.15,1.15,1.16,1.16,1.16,1.21,1.16,1.16,1.16,1.15,1.16,1.16,1.15,1.15	300	200	1
316	18	6.63	6.63	10.20	1.16,1.16,1.16,1.16,1.16,1.16,1.16,1.16,1.12,1.15,1.16,1.16,1.15,1.15,1.16,1.16,1.16,1.16,1.16,1.16,1.17,1.15,1.16,1.16,1.15,1.14	300	200	1
401	7	22.58	22.58	10.75	-	300	200	1
402	4	1.30	1.30	2.00	-	300	200	1
403	15	0.92	0.92	1.42	1.19,1.18,1.19,1.18,1.19,1.19,1.18,1.18,1.19,1.18,1.18,1.18,1.19,1.18,1.18,1.18,1.18,1.21,1.18,1.18,1.19,1.17,1.18,1.18,1.19,1.18	300	200	1
404	15	2.44	2.44	3.75	1.68,1.68,1.68,1.67,1.68,1.68,1.67,1.67,1.54,1.68,1.67,1.67,1.63,1.68,1.67,1.67,1.68,1.67,1.67,1.67,1.70,1.68,1.67,1.67,1.65,1.68	300	200	1
405	15	1.52	1.52	2.33	1.67,1.67,1.67,1.67,1.67,1.67,1.67,1.67,1.67,1.66,1.67,1.67,1.67,1.66,1.67,1.67,1.67,1.71,1.67,1.67,1.67,1.65,1.67,1.67,1.67,1.66	300	200	1
406	15	0.92	0.92	1.42	1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.17,1.18,1.18,1.18,1.17,1.18,1.18,1.18,1.22,1.18,1.18,1.18,1.16,1.18,1.18,1.18,1.17	300	200	1
407	15	1.52	1.52	2.33	1.67,1.67,1.67,1.67,1.67,1.67,1.67,1.67,1.67,1.66,1.67,1.67,1.67,1.66,1.67,1.67,1.67,1.71,1.67,1.67,1.67,1.65,1.67,1.67,1.67,1.66	300	200	1
408	18	7.88	7.88	3.75	2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33	300	200	1
409	1	2.60	2.60	4.00	-	300	200	1
410	15	2.44	2.44	3.75	1.68,1.68,1.68,1.67,1.68,1.68,1.67,1.67,1.53,1.68,1.67,1.67,1.62,1.68,1.67,1.67,1.68,1.67,1.67,1.67,1.71,1.68,1.67,1.67,1.65,1.68	300	200	1
411	18	7.88	7.88	3.75	2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33,2.33	300	200	1
412	4	1.30	1.30	2.00	-	300	200	1
413	18	4.88	4.00	7.50	1.11,1.11,1.11,1.11,1.11,1.11,1.11,1.11,1.12,1.12,1.11,1.11,1.12,1.12,1.11,1.11,1.11,1.06,1.11,1.11,1.11,1.22,1.11,1.11,1.12,1.12	300	200	1
414	18	4.88	4.00	7.50	1.11,1.11,1.11,1.11,1.11,1.11,1.11,1.11,2.62,1.17,1.11,1.11,1.35,1.23,1.11,1.11,1.10,1.12,1.11,1.11,1.08,1.13,1.11,1.11,1.15,1.36	300	200	1
415	18	6.63	6.63	10.20	1.12,1.12,1.12,1.12,1.12,1.12,1.12,1.12,1.14,1.14,1.13,1.13,1.14,1.14,1.12,1.12,1.13,1.10,1.12,1.12,1.13,1.16,1.13,1.13,1.14,1.14	300	200	1
416	18	6.63	6.63	10.20	1.12,1.12,1.12,1.12,1.12,1.12,1.12,1.12,1.30,1.15,1.12,1.12,1.17,1.16,1.12,1.12,1.12,1.13,1.12,1.12,1.11,1.14,1.12,1.12,1.15,1.17	300	200	1

Member Design Capacity

Member ID	$\Phi_t P_n$ (kip)	$\Phi_c P_n$ (kip)	$\Phi_b M_{zn}$ (k-ft)	$\Phi_b M_{yn}$ (k-ft)	$\Phi_v V_{yn}$ (kip)	$\Phi_v V_{zn}$ (kip)
1	251.16	86.58	42.30	42.30	75.35	75.35
2	142.83	141.72	16.17	16.17	42.85	42.85
3	79.65	74.02	10.99	6.26	29.14	16.61
4	79.65	72.01	10.99	6.26	29.14	16.61
5	79.65	73.44	10.99	6.26	29.14	16.61
6	79.65	74.02	10.99	6.26	29.14	16.61
7	79.65	73.44	10.99	6.26	29.14	16.61
8	120.60	115.40	23.36	6.45	30.09	45.74
9	48.35	43.11	2.85	2.85	14.51	14.51
10	79.65	72.01	10.99	6.26	29.14	16.61
11	120.60	115.40	23.36	6.45	30.09	45.74
12	142.83	141.72	16.17	16.17	42.85	42.85
13	120.60	84.03	18.67	6.45	30.09	45.74
14	120.60	84.03	19.04	6.45	30.09	45.74
15	120.60	54.44	23.36	6.45	30.09	45.74
16	120.60	54.44	23.36	6.45	30.09	45.74
101	251.16	86.58	42.30	42.30	75.35	75.35
102	142.83	141.72	16.17	16.17	42.85	42.85
103	79.65	74.02	10.99	6.26	29.14	16.61

104	79.65	72.01	10.99	6.26	29.14	16.61
105	79.65	73.44	10.99	6.26	29.14	16.61
106	79.65	74.02	10.99	6.26	29.14	16.61
107	79.65	73.44	10.99	6.26	29.14	16.61
108	120.60	115.40	23.36	6.45	30.09	45.74
109	48.35	43.11	2.85	2.85	14.51	14.51
110	79.65	72.01	10.99	6.26	29.14	16.61
111	120.60	115.40	23.36	6.45	30.09	45.74
112	142.83	141.72	16.17	16.17	42.85	42.85
113	120.60	84.03	18.22	6.45	30.09	45.74
114	120.60	84.03	18.16	6.45	30.09	45.74
115	120.60	68.63	15.36	6.45	30.09	45.74
116	120.60	68.63	15.21	6.45	30.09	45.74
201	251.16	86.58	42.30	42.30	75.35	75.35
202	142.83	141.72	16.17	16.17	42.85	42.85
203	79.65	74.02	10.99	6.26	29.14	16.61
204	79.65	72.01	10.99	6.26	29.14	16.61
205	79.65	73.44	10.99	6.26	29.14	16.61
206	79.65	74.02	10.99	6.26	29.14	16.61
207	79.65	73.44	10.99	6.26	29.14	16.61
208	120.60	115.40	23.36	6.45	30.09	45.74
209	48.35	43.11	2.85	2.85	14.51	14.51
210	79.65	72.01	10.99	6.26	29.14	16.61
211	120.60	115.40	23.36	6.45	30.09	45.74
212	142.83	141.72	16.17	16.17	42.85	42.85
213	120.60	84.03	18.06	6.45	30.09	45.74
214	120.60	84.03	18.19	6.45	30.09	45.74
215	120.60	68.63	15.53	6.45	30.09	45.74
216	120.60	68.63	15.66	6.45	30.09	45.74
301	251.16	86.58	42.30	42.30	75.35	75.35
302	142.83	141.72	16.17	16.17	42.85	42.85
303	79.65	74.02	10.99	6.26	29.14	16.61
304	79.65	72.01	10.99	6.26	29.14	16.61
305	79.65	73.44	10.99	6.26	29.14	16.61
306	79.65	74.02	10.99	6.26	29.14	16.61
307	79.65	73.44	10.99	6.26	29.14	16.61
308	120.60	115.40	23.36	6.45	30.09	45.74
309	48.35	43.11	2.85	2.85	14.51	14.51
310	79.65	72.01	10.99	6.26	29.14	16.61
311	120.60	115.40	23.36	6.45	30.09	45.74
312	142.83	141.72	16.17	16.17	42.85	42.85
313	120.60	84.03	18.22	6.45	30.09	45.74
314	120.60	84.03	18.16	6.45	30.09	45.74
315	120.60	68.63	15.66	6.45	30.09	45.74
316	120.60	68.63	15.35	6.45	30.09	45.74
401	251.16	86.58	42.30	42.30	75.35	75.35
402	142.83	141.72	16.17	16.17	42.85	42.85
403	79.65	74.02	10.99	6.26	29.14	16.61
404	79.65	72.01	10.99	6.26	29.14	16.61
405	79.65	73.44	10.99	6.26	29.14	16.61
406	79.65	74.02	10.99	6.26	29.14	16.61
407	79.65	73.44	10.99	6.26	29.14	16.61

407	79.65	73.44	10.99	6.26	29.14	16.61
408	120.60	54.44	23.36	6.45	30.09	45.74
409	48.35	43.11	2.85	2.85	14.51	14.51
410	79.65	72.01	10.99	6.26	29.14	16.61
411	120.60	54.44	23.36	6.45	30.09	45.74
412	142.83	141.72	16.17	16.17	42.85	42.85
413	120.60	84.03	18.67	6.45	30.09	45.74
414	120.60	84.03	19.04	6.45	30.09	45.74
415	120.60	68.63	15.01	6.45	30.09	45.74
416	120.60	68.63	15.12	6.45	30.09	45.74

Design Ratio

Member ID	P	M_z	M_y	V_y	V_z	(P,M_z,M_y)	Worst LC	KL/r	δ	Status
1	0.090	0.343	0.026	0.006	0.002	0.345	#16	0.603	Not Required	Pass
2	0.001	0.384	0.027	0.082	0.005	0.412	#13	0.034	Not Required	Pass
3	0.001	0.617	0.006	0.062	0.001	0.621	#13	0.044	Not Required	Pass
4	0.001	0.577	0.021	0.059	0.004	0.598	#13	0.078	Not Required	Pass
5	0.001	0.382	0.014	0.062	0.003	0.386	#13	0.073	Not Required	Pass
6	0.001	0.689	0.017	0.071	0.003	0.706	#13	0.044	Not Required	Pass
7	0.001	0.427	0.029	0.069	0.006	0.435	#13	0.073	Not Required	Pass
8	0.001	0.077	0.021	0.040	0.001	0.085	#13	0.088	Not Required	Pass
9	0.002	0.081	0.014	0.002	0.001	0.095	#13	0.198	Not Required	Pass
10	0.001	0.642	0.029	0.065	0.005	0.649	#13	0.078	Not Required	Pass
11	0.001	0.079	0.021	0.044	0.001	0.085	#13	0.088	Not Required	Pass
12	0.000	0.452	0.029	0.093	0.006	0.481	#13	0.052	Not Required	Pass
13	0.001	0.187	0.037	0.056	0.002	0.198	#13	0.265	Not Required	Pass
14	0.001	0.178	0.037	0.052	0.002	0.183	#13	0.177	Not Required	Pass
15	0.000	0.066	0.009	0.028	0.001	0.073	#13	Not Required	Not Required	Pass
16	0.000	0.062	0.009	0.026	0.001	0.069	#13	Not Required	Not Required	Pass
101	0.104	0.372	0.003	0.007	0.000	0.373	#16	0.603	Not Required	Pass
102	0.000	0.491	0.032	0.102	0.005	0.523	#13	0.052	Not Required	Pass
103	0.001	0.761	0.010	0.077	0.002	0.771	#13	0.044	Not Required	Pass
104	0.001	0.718	0.021	0.073	0.004	0.729	#13	0.078	Not Required	Pass
105	0.001	0.472	0.023	0.076	0.005	0.477	#13	0.073	Not Required	Pass
106	0.001	0.755	0.011	0.076	0.003	0.759	#13	0.044	Not Required	Pass
107	0.001	0.468	0.020	0.076	0.004	0.472	#13	0.073	Not Required	Pass
108	0.001	0.052	0.011	0.042	0.001	0.056	#13	0.088	Not Required	Pass
109	0.001	0.083	0.010	0.001	0.000	0.093	#13	0.198	Not Required	Pass
110	0.001	0.708	0.021	0.072	0.004	0.719	#13	0.078	Not Required	Pass
111	0.001	0.057	0.011	0.045	0.001	0.060	#13	0.088	Not Required	Pass
112	0.000	0.483	0.033	0.101	0.006	0.515	#13	0.052	Not Required	Pass
113	0.001	0.216	0.030	0.059	0.002	0.226	#13	0.265	Not Required	Pass
114	0.002	0.211	0.031	0.056	0.002	0.220	#13	0.265	Not Required	Pass
115	0.001	0.223	0.016	0.046	0.001	0.234	#13	0.439	Not Required	Pass
116	0.001	0.209	0.016	0.044	0.001	0.221	#13	0.439	Not Required	Pass
201	0.102	0.379	0.000	0.006	0.000	0.379	#16	0.603	Not Required	Pass
202	0.000	0.479	0.032	0.100	0.006	0.511	#13	0.034	Not Required	Pass
203	0.001	0.748	0.009	0.076	0.001	0.755	#13	0.044	Not Required	Pass
204	0.001	0.700	0.019	0.071	0.003	0.710	#13	0.078	Not Required	Pass
205	0.001	0.464	0.020	0.075	0.004	0.467	#13	0.073	Not Required	Pass

206	0.001	0.748	0.009	0.076	0.001	0.755	#13	0.044	Not Required	Pass
207	0.001	0.464	0.020	0.075	0.004	0.467	#13	0.073	Not Required	Pass
208	0.001	0.055	0.010	0.042	0.001	0.058	#13	0.088	Not Required	Pass
209	0.001	0.080	0.008	0.001	0.000	0.088	#13	0.198	Not Required	Pass
210	0.001	0.700	0.019	0.071	0.003	0.710	#13	0.078	Not Required	Pass
211	0.001	0.059	0.010	0.045	0.001	0.061	#13	0.088	Not Required	Pass
212	0.000	0.479	0.032	0.100	0.006	0.511	#13	0.034	Not Required	Pass
213	0.001	0.211	0.027	0.058	0.002	0.218	#13	0.265	Not Required	Pass
214	0.001	0.204	0.027	0.054	0.002	0.210	#13	0.265	Not Required	Pass
215	0.001	0.201	0.015	0.045	0.001	0.212	#13	0.439	Not Required	Pass
216	0.001	0.188	0.015	0.042	0.001	0.200	#13	0.439	Not Required	Pass
301	0.104	0.372	0.003	0.007	0.000	0.373	#16	0.603	Not Required	Pass
302	0.000	0.483	0.033	0.101	0.006	0.515	#13	0.052	Not Required	Pass
303	0.001	0.755	0.011	0.076	0.003	0.759	#13	0.044	Not Required	Pass
304	0.001	0.708	0.021	0.072	0.004	0.719	#13	0.078	Not Required	Pass
305	0.001	0.468	0.020	0.076	0.004	0.472	#13	0.073	Not Required	Pass
306	0.001	0.761	0.010	0.077	0.002	0.771	#13	0.044	Not Required	Pass
307	0.001	0.472	0.023	0.076	0.005	0.477	#13	0.073	Not Required	Pass
308	0.001	0.059	0.013	0.044	0.001	0.060	#13	0.088	Not Required	Pass
309	0.001	0.083	0.010	0.001	0.000	0.093	#13	0.198	Not Required	Pass
310	0.001	0.718	0.021	0.073	0.004	0.729	#13	0.078	Not Required	Pass
311	0.001	0.064	0.013	0.046	0.001	0.066	#13	0.088	Not Required	Pass
312	0.000	0.491	0.032	0.102	0.005	0.523	#13	0.052	Not Required	Pass
313	0.001	0.216	0.030	0.059	0.002	0.226	#13	0.265	Not Required	Pass
314	0.002	0.211	0.031	0.056	0.002	0.220	#13	0.265	Not Required	Pass
315	0.001	0.200	0.015	0.045	0.001	0.211	#13	0.439	Not Required	Pass
316	0.001	0.187	0.015	0.042	0.001	0.199	#13	0.439	Not Required	Pass
401	0.090	0.343	0.026	0.006	0.002	0.345	#16	0.603	Not Required	Pass
402	0.000	0.452	0.029	0.093	0.006	0.481	#13	0.052	Not Required	Pass
403	0.001	0.689	0.017	0.071	0.003	0.706	#13	0.044	Not Required	Pass
404	0.001	0.642	0.029	0.065	0.005	0.649	#13	0.078	Not Required	Pass
405	0.001	0.427	0.029	0.069	0.006	0.435	#13	0.073	Not Required	Pass
406	0.001	0.617	0.006	0.062	0.001	0.621	#13	0.044	Not Required	Pass
407	0.001	0.382	0.014	0.062	0.003	0.386	#13	0.073	Not Required	Pass
408	0.000	0.062	0.009	0.026	0.001	0.069	#13	Not Required	Not Required	Pass
409	0.002	0.081	0.014	0.002	0.001	0.095	#13	0.198	Not Required	Pass
410	0.001	0.577	0.021	0.059	0.004	0.598	#13	0.078	Not Required	Pass
411	0.000	0.066	0.009	0.028	0.001	0.073	#13	Not Required	Not Required	Pass
412	0.001	0.384	0.027	0.082	0.005	0.412	#13	0.034	Not Required	Pass
413	0.001	0.187	0.037	0.056	0.002	0.198	#13	0.177	Not Required	Pass
414	0.001	0.178	0.037	0.052	0.002	0.183	#13	0.265	Not Required	Pass
415	0.001	0.227	0.021	0.044	0.001	0.238	#13	0.439	Not Required	Pass
416	0.001	0.215	0.021	0.040	0.001	0.227	#13	0.439	Not Required	Pass

Definitions

Φ_t	Safety factor for tensile
Φ_c	Safety factor for compression
Φ_b	Safety factor for flexure
Φ_v	Safety factor for shear
E	Modulus of elasticity
F_y	Specified minimum yield stress
F_u	Specified minimum tensile strength

A	Cross-sectional area
J	Torsional constant
I_{yp}	Moment of inertia about the Y axes
I_{zp}	Moment of inertia about the Z axes
I_w	Warping constant
S_{yp}	Plastic section modulus about the Y axis
S_{zp}	Plastic section modulus about the Z axis
KL	Effective length
C_b	Buckling modification factor (from all load combinations)
L_b	Length between braced points
LST	Limited slenderness for tension
LSC	Limited slenderness for compression
LD	Limited deflection
P_n	Nominal axial strength (tension/comression)
M_n	Nominal flexural strength (about Z/Y axis)
V_n	Nominal shear strength (along Z/Y axis)
P	Design ratio in case of axial force
M_z	Design ratio in case of bending about Z axis
M_y	Design ratio in case of bending about Y axis
V_y	Design ratio in case of shear along Y axis
V_z	Design ratio in case of shear along Z axis
(P,M_z,M_y)	Design ratio in case of axial force and bending action
KL/r	Design ratio in case of section slenderness
δ	Design ratio in case of member deflection
OK	Capacity is provided
NG	Capacity is not provided

REFERENCES	CALCULATIONS	RESULTS

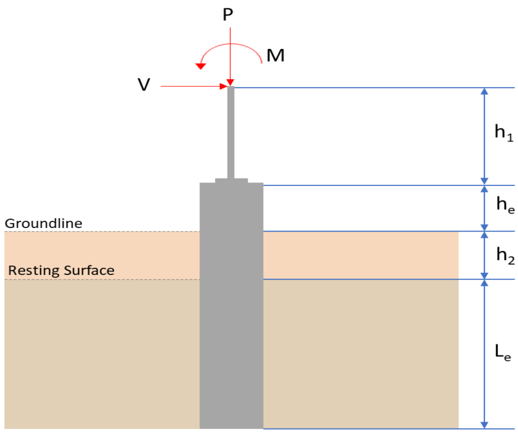
SkyCiv Foundation Design

Pile Foundation

Design Information :

Design code : IBC 2021 (International Building Code)
Unit System : Imperial

Pile Input



Geometry

Pile shape: rectangular

$b = 48\ \text{in}$ - Pile width

$D = 48\ \text{in}$ - Pile depth

$L = 4.75\ \text{ft}$ - Total pile length

$h_1 = 0\ \text{ft}$ - Lateral load height from the top of the pile,

$h_2 = 0\ \text{ft}$ - Depth to resisting surface

$h_e = 0\ \text{ft}$ - Length of pile above the ground

Tabulation of Soil Parameters

Layer	Label	Allowable Bearing Pressure (q_a) (psf)	Allowable Lateral Pressure (R) (psf/ft)
1	Sand, silty sand, clayey sand, silty gravel & clayey gravel	2000.000	150.000

Tabulation of Loads

Load Component	ASD	LRFD
P (kip)	4.946	7.751
V_x (kip)	-0.262	-0.438
V_z (kip)	0.091	0.146
M_x (kipft)	0.300	0.482
M_z (kipft)	8.461	14.505

Material Properties

$f'_{ck} = 2.5\ \text{ksi}$ - Concrete strength,

Required depth to resist lateral loads (ASD)

H - Point of application of the lateral load

$$H = h_1 + h_2 + h_e$$

$$H = (0\ \text{ft}) + (0\ \text{ft}) + (0\ \text{ft})$$

$$H = 0\ \text{ft}$$

Considering x-direction:

H_o - Lateral force per length of pile,

$$H_o = \frac{V_x}{1.57\ D}$$

$$H_o = \frac{(-0.262\ \text{kip})}{1.57 \times (48\ \text{in})}$$

$$H_o = -0.04172\ \text{kip/ft}$$

M_o - Moment per length of pile,

$$M_o = \frac{M_z + (V_x\ H)}{1.57\ D}$$

$$M_o = \frac{(8.461\ \text{kipft}) + ((-0.262\ \text{kip}) \times (0\ \text{ft}))}{1.57 \times (48\ \text{in})}$$

$$M_o = 1.3473\ \text{kipft/ft}$$

Required depth of embedment in earth:

$$L_x^3 - \left(14.14 \times \frac{H_o \times L_x}{R}\right) - \left(18.85 \times \frac{M_o}{R}\right) = 0$$

Solving the cubic equation:
$L_{e,x} = 4.5838\ \text{ft}$ - Required depth in x-direction,

Considering z-direction:

H_o - Lateral force per length of pile,

$$H_o = \frac{V_z}{1.57\ b}$$

$$H_o = \frac{(0.091\ \text{kip})}{1.57 \times (48\ \text{in})}$$

$$H_o = 0.01449\ \text{kip/ft}$$

M_o - Moment per length of pile,

$$M_o = \frac{M_x + (V_z\ H)}{1.57\ b}$$

$$M_o = \frac{(0.3\ \text{kipft}) + ((0.091\ \text{kip}) \times (0\ \text{ft}))}{1.57 \times (48\ \text{in})}$$

$$M_o = 0.047771\ \text{kipft/ft}$$

Required depth of embedment in earth:

$$L_z^3 - \left(14.14 \times \frac{H_o \times L_z}{R}\right) - \left(18.85 \times \frac{M_o}{R}\right) = 0$$

Solving the cubic equation:
$L_{e,z} = 1.748\ \text{ft}$ - Required depth in z-direction,

Minimum embedded depth required:

$L_{e,req}$ - Depth of pile required,

$$L_{e,req} = MAX[L_{e,x}, L_{e,z}]$$

$$L_{e,req} = MAX[(4.5838\ \text{ft}), (1.748\ \text{ft})]$$

$$L_{e,req} = 4.584\ \text{ft}$$

L_e - Actual embedded length of pile,

$$L_e = L - h_e - h_2$$

$$L_e = (4.75\ \text{ft}) - (0\ \text{ft}) - (0\ \text{ft})$$

$$L_e = 4.75\ \text{ft}$$

$Ratio$ - Embedded depth

$$Ratio = \frac{L_{e,req}}{L_e}$$

$$Ratio = \frac{(4.584\ \text{ft})}{(4.75\ \text{ft})}$$

$$Ratio = 0.96505$$

Status: **PASS**
Ratio: **0.970**

End-bearing Capacity (ASD)

A - Pile cross-section area

$$A = b\ D$$

$$A = (48\ \text{in}) \times (48\ \text{in})$$

$$A = 16\ \text{ft}^2$$

q - End-bearing pressure

$$q = \frac{P_v}{A}$$

$$q = \frac{(4.946 \text{ kip})}{(16 \text{ ft}^2)}$$

$$q = 0.30912 \text{ kip/ft}^2$$

Check bearing capacity ratio:

$Ratio$ - Capacity

$$Ratio = \frac{q}{q_a}$$

$$Ratio = \frac{\left(0.30912 \text{ kip/ft}^2\right)}{(2000 \text{ psf})}$$

$$Ratio = 0.15456$$

Status: **PASS**
Ratio: **0.150**

Czerniak

Lateral Soil Pressure (ASD):

L/D - Length to least lateral dimension ratio,

$$L/D = \frac{L}{D}$$

$$L/D = \frac{(4.75 \text{ ft})}{(48 \text{ in})}$$

$$L/D = 1.1875$$

Since L/D $\leq$ 10,

Pile is short.

Considering x-direction:

$H_o = -0.04172 \text{ kip/ft}$ - Lateral force per length of pile,
$M_o = 1.3473 \text{ kipft/ft}$ - Overturning moment per length of pile,
a - Distance from resting surface to pivot point,

$$a = \frac{(4\, M_o\, L_e) + \left(3\, H_o\, L_e^2\right)}{(6\, M_o) + (4\, H_o\, L_e)}$$

$$a = \frac{(4 \times (1.3473 \text{ kipft/ft}) \times (4.75 \text{ ft})) + \left(3 \times (-0.04172 \text{ kip/ft}) \times (4.75 \text{ ft})^2\right)}{(6 \times (1.3473 \text{ kipft/ft})) + (4 \times (-0.04172 \text{ kip/ft}) \times (4.75 \text{ ft}))}$$

$$a = 3.202 \text{ ft}$$

p - Earth pressure against the pile at distance a/2 from resting surface,

$$p = \frac{0.75\, [(4\, M_o) + (3\, H_o\, L_e)]^2}{L_e^2\, [(3\, M_o) + (2\, H_o\, L_e)]}$$

$$p = \frac{0.75 \times [(4 \times (1.3473 \text{ kipft/ft})) + (3 \times (-0.04172 \text{ kip/ft}) \times (4.75 \text{ ft})]^2}{(4.75 \text{ ft})^2 \times [(3 \times (1.3473 \text{ kipft/ft})) + (2 \times (-0.04172 \text{ kip/ft}) \times (4.75 \text{ ft}))]}$$

$$p = 0.20962 \text{ kip/ft}^2$$

s - Earth pressure against the pile at distance L_e,

$$s = \frac{6\, [(2\, M_o) + (H_o\, L_e)]}{L_e^2}$$

$$s = \frac{6 \times [(2 \times (1.3473 \text{ kipft/ft})) + ((-0.04172 \text{ kip/ft}) \times (4.75 \text{ ft}))]}{(4.75 \text{ ft})^2}$$

$$s = 0.66387 \text{ kip/ft}^2$$

Check lateral soil pressure capacity:

p_a - Allowable lateral soil pressure at depth a/2,

$$p_a = R\, \frac{a}{2}$$

$$p_a = (150 \text{ psf/ft}) \times \frac{(3.202 \text{ ft})}{2}$$

$$p_a = 0.24015 \text{ kip/ft}^2$$

$Ratio$ - Lateral soil capacity

$$Ratio = \frac{p}{p_a}$$

$$Ratio = \frac{\left(0.20962\ \mathrm{kip/ft^2}\right)}{\left(0.24015\ \mathrm{kip/ft^2}\right)}$$

$$Ratio = 0.87286$$

Status: **PASS**
Ratio: **0.870**

p_s - Allowable lateral soil pressure at depth L_e,

$$p_s = R\,L_e$$

$$p_s = (150\ \mathrm{psf/ft}) \times (4.75\ \mathrm{ft})$$

$$p_s = 0.7125\ \mathrm{kip/ft^2}$$

$Ratio$ - Lateral soil capacity

$$Ratio = \frac{s}{p_s}$$

$$Ratio = \frac{\left(0.66387\ \mathrm{kip/ft^2}\right)}{\left(0.7125\ \mathrm{kip/ft^2}\right)}$$

$$Ratio = 0.93174$$

Status: **PASS**
Ratio: **0.930**

Considering z-direction:

$H_o = 0.01449\ \mathrm{kip/ft}$ - Lateral force per length of pile,
$M_o = 0.047771\ \mathrm{kipft/ft}$ - Overturning moment per length of pile,
a - Distance from resting surface to pivot point,

$$a = \frac{(4\,M_o\,L_e) + \left(3\,H_o\,L_e^2\right)}{(6\,M_o) + (4\,H_o\,L_e)}$$

$$a = \frac{(4 \times (0.047771\ \mathrm{kipft/ft}) \times (4.75\ \mathrm{ft})) + \left(3 \times (0.01449\ \mathrm{kip/ft}) \times (4.75\ \mathrm{ft})^2\right)}{(6 \times (0.047771\ \mathrm{kipft/ft})) + (4 \times (0.01449\ \mathrm{kip/ft}) \times (4.75\ \mathrm{ft}))}$$

$$a = 3.3606\ \mathrm{ft}$$

p - Earth pressure against the pile at distance a/2 from resting surface,

$$p = \frac{0.75\,[(4\,M_o) + (3\,H_o\,L_e)]^2}{L_e^2\,[(3\,M_o) + (2\,H_o\,L_e)]}$$

$$p = \frac{0.75 \times [(4 \times (0.047771\ \mathrm{kipft/ft})) + (3 \times (0.01449\ \mathrm{kip/ft}) \times (4.75\ \mathrm{ft}))]^2}{(4.75\ \mathrm{ft})^2 \times [(3 \times (0.047771\ \mathrm{kipft/ft})) + (2 \times (0.01449\ \mathrm{kip/ft}) \times (4.75\ \mathrm{ft}))]}$$

$$p = 0.0187\ \mathrm{kip/ft^2}$$

s - Earth pressure against the pile at distance L_e,

$$s = \frac{6\,[(2\,M_o) + (H_o\,L_e)]}{L_e^2}$$

$$s = \frac{6 \times [(2 \times (0.047771\ \mathrm{kipft/ft})) + ((0.01449\ \mathrm{kip/ft}) \times (4.75\ \mathrm{ft}))]}{(4.75\ \mathrm{ft})^2}$$

$$s = 0.043711\ \mathrm{kip/ft^2}$$

Check lateral soil pressure capacity:

p_a - Allowable lateral soil pressure at depth a/2,

$$p_a = R\,\frac{a}{2}$$

$$p_a = (150\ \mathrm{psf/ft}) \times \frac{(3.3606\ \mathrm{ft})}{2}$$

$$p_a = 0.25205\ \mathrm{kip/ft^2}$$

$Ratio$ - Lateral soil capacity

$$Ratio = \frac{p}{p_a}$$

$$Ratio = \frac{\left(0.0187\ \mathrm{kip/ft^2}\right)}{\left(0.25205\ \mathrm{kip/ft^2}\right)}$$

$$Ratio = 0.074193$$

Status: **PASS**
Ratio: **0.070**

p_s - Allowable lateral soil pressure at depth L_e,

$$p_s = R\,L_e$$

$$p_s = (150\ \mathrm{psf/ft}) \times (4.75\ \mathrm{ft})$$

$$p_s = 0.7125\ \mathrm{kip/ft^2}$$

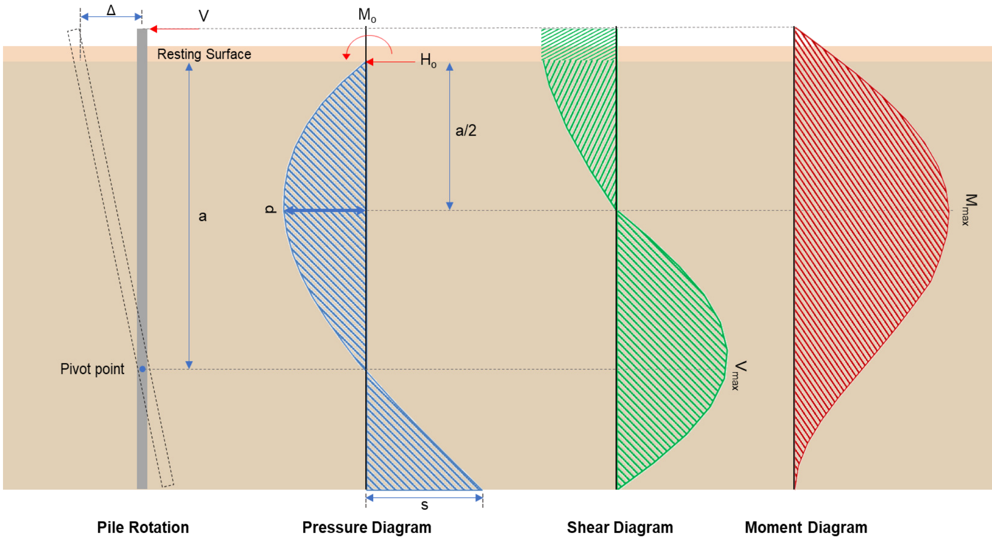
$Ratio$ - Lateral soil capacity

$$Ratio = \frac{s}{p_s}$$

$$Ratio = \frac{(0.043711\ \mathrm{kip/ft^2})}{(0.7125\ \mathrm{kip/ft^2})}$$

$$Ratio = 0.061349$$

Status: **PASS**
Ratio: **0.060**



Shear force and Bending moment (x-direction, LRFD)

H_o - Lateral force per length of pile,

$$H_o = \frac{V_x}{1.57\,D}$$

$$H_o = \frac{(-0.438\ \mathrm{kip})}{1.57 \times (48\ \mathrm{in})}$$

$$H_o = -0.069745\ \mathrm{kip/ft}$$

M_o - Moment per length of pile,

$$M_o = \frac{M_z + (V_x\,H)}{1.57\,D}$$

$$M_o = \frac{(14.505\ \mathrm{kipft}) + ((-0.438\ \mathrm{kip}) \times (0\ \mathrm{ft}))}{1.57 \times (48\ \mathrm{in})}$$

$$M_o = 2.3097\ \mathrm{kipft/ft}$$

E - Distance from lateral load to resisting surface,

$$E = \frac{M_o}{H_o}$$

$$E = \frac{(2.3097\ \mathrm{kipft/ft})}{(-0.069745\ \mathrm{kip/ft})}$$

$$E = 33.116\ \mathrm{ft}$$

a - Distance from resting surface to pivot point,

$$a = \frac{(4\,M_o\,L_e) + \left(3\,H_o\,L_e^2\right)}{(6\,M_o) + (4\,H_o\,L_e)}$$

$$a = \frac{(4 \times (2.3097\ \mathrm{kipft/ft}) \times (4.75\ \mathrm{ft})) + \left(3 \times (-0.069745\ \mathrm{kip/ft}) \times (4.75\ \mathrm{ft})^2\right)}{\ldots}$$

$$a = \frac{}{(6 \times (2.3097 \text{ kipft/ft})) + (4 \times (-0.069745 \text{ kip/ft}) \times (4.75 \text{ ft}))}$$

$$a = 3.2012 \text{ ft}$$

V_{max} - Max shear force located at depth a,

$$V_{max} = (H_o\, D) \left[1 - \left[3 \left(\frac{4\,E}{L_e} + 3\right) \left(\frac{a}{L_e}\right)^2\right] + \left[4 \left(\frac{3\,E}{L_e} + 2\right) \left(\frac{a}{L_e}\right)^3\right]\right]$$

$$V_{max} = ((-0.069745 \text{ kip/ft}) \times (48 \text{ in})) \times \left[1 - \left[3 \times \left(\frac{4 \times (33.116 \text{ ft})}{(4.75 \text{ ft})} + 3\right) \times \left(\frac{(3.2012 \text{ ft})}{(4.75 \text{ ft})}\right)^2\right] + \left[4 \times \left(\frac{3 \times (33.116 \text{ ft})}{(4.75 \text{ ft})} + 2\right) \times \left(\frac{(3.2012 \text{ ft})}{(4.75 \text{ ft})}\right)^3\right]\right]$$

$$V_{max} = 3.6348 \text{ kip}$$

M_{max} - Max bending moment located at depth a/2,

$$M_{max} = (H_o\, D\, L_e) \left[\left(\frac{E}{L_e} + \frac{a}{2\,L_e}\right) - \left[\left(\frac{4\,E}{L_e} + 3\right) \left(\frac{a}{2\,L_e}\right)^3\right] + \left[\left(\frac{3\,E}{L_e} + 2\right) \left(\frac{a}{2\,L_e}\right)^4\right]\right]$$

$$M_{max} = ((-0.069745 \text{ kip/ft}) \times (48 \text{ in}) \times (4.75 \text{ ft})) \times \left[\left(\frac{(33.116 \text{ ft})}{(4.75 \text{ ft})} + \frac{(3.2012 \text{ ft})}{2 \times (4.75 \text{ ft})}\right) - \left[\left(\frac{4 \times (33.116 \text{ ft})}{(4.75 \text{ ft})} + 3\right) \times \left(\frac{(3.2012 \text{ ft})}{2 \times (4.75 \text{ ft})}\right)^3\right] + \left[\left(\frac{3 \times (33.116 \text{ ft})}{(4.75 \text{ ft})} + 2\right) \times \left(\frac{(3.2012 \text{ ft})}{2 \times (4.75 \text{ ft})}\right)^4\right]\right]$$

$$M_{max} = 8.5108 \text{ kipft}$$

Shear force and Bending moment (z-direction, LRFD)

H_o - Lateral force per length of pile,

$$H_o = \frac{V_z}{1.57\,b}$$

$$H_o = \frac{(0.146 \text{ kip})}{1.57 \times (48 \text{ in})}$$

$$H_o = 0.023248 \text{ kip/ft}$$

M_o - Moment per length of pile,

$$M_o = \frac{M_x + (V_z\, H)}{1.57\,b}$$

$$M_o = \frac{(0.482 \text{ kipft}) + ((0.146 \text{ kip}) \times (0 \text{ ft}))}{1.57 \times (48 \text{ in})}$$

$$M_o = 0.076752 \text{ kipft/ft}$$

E - Distance from lateral load to resisting surface,

$$E = \frac{M_o}{H_o}$$

$$E = \frac{(0.076752 \text{ kipft/ft})}{(0.023248 \text{ kip/ft})}$$

$$E = 3.3014 \text{ ft}$$

a - Distance from resting surface to pivot point,

$$a = \frac{(4\,M_o\,L_e) + \left(3\,H_o\,L_e^2\right)}{(6\,M_o) + (4\,H_o\,L_e)}$$

$$a = \frac{(4 \times (0.076752 \text{ kipft/ft}) \times (4.75 \text{ ft})) + \left(3 \times (0.023248 \text{ kip/ft}) \times (4.75 \text{ ft})^2\right)}{(6 \times (0.076752 \text{ kipft/ft})) + (4 \times (0.023248 \text{ kip/ft}) \times (4.75 \text{ ft}))}$$

$$a = 3.3605 \text{ ft}$$

V_{max} - Max shear force located at depth a,

$$V_{max} = (H_o\, b) \left[1 - \left[3 \left(\frac{4\,E}{L_e} + 3\right) \left(\frac{a}{L_e}\right)^2\right] + \left[4 \left(\frac{3\,E}{L_e} + 2\right) \left(\frac{a}{L_e}\right)^3\right]\right]$$

$$V_{max} = ((0.023248 \text{ kip/ft}) \times (48 \text{ in})) \times \left[1 - \left[3 \times \left(\frac{4 \times (3.3014 \text{ ft})}{(4.75 \text{ ft})} + 3\right) \times \left(\frac{(3.3605 \text{ ft})}{(4.75 \text{ ft})}\right)^2\right] + \left[4 \times \left(\frac{3 \times (3.3014 \text{ ft})}{(4.75 \text{ ft})} + 2\right) \times \left(\frac{(3.3605 \text{ ft})}{(4.75 \text{ ft})}\right)^3\right]\right]$$

$$V_{max} = 0.17604 \text{ kip}$$

M_{max} - Max bending moment located at depth a/2,

$$M_{max} = (H_o\, b\, L_e)\left[\left(\frac{E}{L_e} + \frac{a}{2\, L_e}\right) - \left[\left(\frac{4\, E}{L_e} + 3\right)\left(\frac{a}{2\, L_e}\right)^3\right] + \left[\left(\frac{3\, E}{L_e} + 2\right)\left(\frac{a}{2\, L_e}\right)^4\right]\right]$$

$$M_{max} = ((0.023248 \text{ kip/ft}) \times (48 \text{ in}) \times (4.75 \text{ ft})) \times \left[\left(\frac{(3.3014 \text{ ft})}{(4.75 \text{ ft})} + \frac{(3.3605 \text{ ft})}{2 \times (4.75 \text{ ft})}\right) - \left[\left(\frac{4 \times (3.3014 \text{ ft})}{(4.75 \text{ ft})} + 3\right) \times \left(\frac{(3.3605 \text{ ft})}{2 \times (4.75 \text{ ft})}\right)^3\right] + \left[\left(\frac{3 \times (3.3014 \text{ ft})}{(4.75 \text{ ft})} + 2\right) \times \left(\frac{(3.3605 \text{ ft})}{2 \times (4.75 \text{ ft})}\right)^4\right]\right]$$

$$M_{max} = 0.3785 \text{ kipft}$$

Minimum Reinforcement Check (LRFD)

Parameters:

$f'_{ck} = 2.5 \text{ ksi}$ - Concrete strength,
$f_{yk} = 60 \text{ ksi}$ - Longitudinal reinforcement strength,
$\phi = 0.65$ - Reduction factor for axial strength,
Table 22.4.2.1 $\alpha = 0.8$ - Alpha factor for axial strength,
$A_g = 2304 \text{ in}^2$ - Gross area of concrete,

Longitudinal reinforcement:

Required reinforcement due to axial load, $A_{st,required}$
22.4.2.2, 10.6.1.1 $A_{st,required}$

$$A_{st,required} = Min\left[\frac{\frac{P}{\phi\, \alpha} - (0.85\, f'_{ck}\, A_g)}{f_{yk} - (0.85\, f'_{ck})}, (0.08\, A_g)\right]$$

$$A_{st,required} = Min\left[\frac{\frac{(7.751 \text{ kip})}{(0.65)\times(0.8)} - (0.85 \times (2.5 \text{ ksi}) \times (2304 \text{ in}^2))}{(60 \text{ ksi}) - (0.85 \times (2.5 \text{ ksi}))}, (0.08 \times (2304 \text{ in}^2))\right]$$

$$A_{st,required} = -84.339 \text{ in}^2$$

A_{min} - Governing minimum reinforcement area,

$$A_{min} = Max[A_{st,required}, (0.0018\, A_g)]$$

$$A_{min} = Max\left[(-84.339 \text{ in}^2), (0.0018 \times (2304 \text{ in}^2))\right]$$

$$A_{min} = 4.1472 \text{ in}^2$$

n_{rebar} - Required number of reinforcement,

$$n_{rebar} = \frac{A_{min}}{A_{rebar}}$$

$$n_{rebar} = \frac{(4.1472 \text{ in}^2)}{(0.3068 \text{ in}^2)}$$

$$n_{rebar} = 14$$

A_{st} - Actual total reinforcement area,

$$A_{st} = n_{rebar}\, \frac{\pi\, d_{bar}^2}{4}$$

$$A_{st} = (14) \times \frac{\pi \times (0.625 \text{ in})^2}{4}$$

$$A_{st} = 4.2951 \text{ in}^2$$

$Ratio$ - Capacity

$$Ratio = \frac{A_{min}}{A_{st}}$$

$$Ratio = \frac{(4.1472 \text{ in}^2)}{(4.2951 \text{ in}^2)}$$

$$Ratio = 0.96556$$

Status: **PASS**
Ratio: **0.970**

25.2.3 s_{rebar} - Minimum spacing of reinforcement,

$$s_{rebar} = Max\left[1.5, \left(1.5\ d_{bar}\right)\right]$$

$$s_{rebar} = Max\left[1.5, \left(1.5 \times (0.625\ \text{in})\right)\right]$$

$$s_{rebar} = 1.5\ \text{in}$$

Ties:

25.7.2.2 Since longitudinal reinforcement is $\leq$ No. 10ø: Use #3(0.375 in)

25.7.2.1 s_{ties} - Maximum spacing of ties,

$$s_{ties} = Min\left[\left(16\ d_{bar}\right), \left(48\ d_{ties}\right), Min\left(D, b\right)\right]$$

$$s_{ties} = Min\left[\left(16 \times (0.625\ \text{in})\right), \left(48 \times (0.375\ \text{in})\right), Min\left((48\ \text{in}), (48\ \text{in})\right)\right]$$

$$s_{ties} = 10\ \text{in}$$

Summary:

Main reinforcement: **14 - #5 (0.625 in)**
Ties: **#3(0.375 in) - 10 in**

Axial Compression Strength (ACI 318-19, LRFD)

22.4.2.2 ϕP_N - Allowable axial compressive strength

$$\phi P_N = \phi\ 0.80\ \left[\left(0.85\ f'_{ck}\ \left[A_g - A_{st}\right]\right) + \left(f_{yk}\ A_{st}\right)\right]$$

$$\phi P_N = (0.65) \times 0.80 \times \left[\left(0.85 \times (2.5\ \text{ksi}) \times \left[\left(2304\ \text{in}^2\right) - \left(4.2951\ \text{in}^2\right)\right]\right) + \left((60\ \text{ksi}) \times \left(4.2951\ \text{in}^2\right)\right)\right]$$

$$\phi P_N = 2675.2\ \text{kip}$$

$Ratio$ - Capacity

$$Ratio = \frac{P}{\phi P_N}$$

$$Ratio = \frac{(7.751\ \text{kip})}{(2675.2\ \text{kip})}$$

$$Ratio = 0.0028974$$

Status: **PASS**
Ratio: **0.000**

Shear Strength (ACI 318-19, LRFD)

Parameters:

$b_w = 48\ \text{in}$ - Effective width,

22.5.2.2 d - Effective depth

$$d = 0.80\ D$$

$$d = 0.80 \times (48\ \text{in})$$

$$d = 38.4\ \text{in}$$

22.5.5.1.3 λ_s - size effect modification factor

$$\lambda_s = MIN\left[\sqrt{\frac{2}{1 + \frac{d}{10}}}, 1\right]$$

$$\lambda_s = MIN\left[\sqrt{\frac{2}{1 + \frac{(38.4\ \text{in})}{10}}}, 1\right]$$

$$\lambda_s = 0.64282$$

The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5\ \text{ksi} \rightarrow 2500\ \text{psi}$,

22.5.5.1.1 $V_{c,max}$ - Max shear strength of concrete

$$V_{c,max} = 5\ \lambda_s\ \sqrt{f'_{ck}}\ b_w\ d$$

$$V_{c,max} = 5 \times (0.64282) \times \sqrt{(2500\ \text{psi})} \times (48\ \text{in}) \times (38.4\ \text{in})$$

$$V_{c,max} = 296.21 \text{ kip}$$

The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5 \text{ ksi} \rightarrow 2500 \text{ psi}$, $P = 7.751 \text{ kip} \rightarrow 7751 \text{ lbf}$,

22.5.5.1.1(a) $V_{c,a}$ - Shear strength of concrete (a)

$$V_{c,a} = \left[2\, \lambda_s \sqrt{f'_{ck}} + \frac{P}{6\, A_g}\right] b_w\, d$$

$$V_{c,a} = \left[2 \times (0.64282) \times \sqrt{(2500 \text{ psi})} + \frac{(7751 \text{ lbf})}{6 \times (2304 \text{ in}^2)}\right] \times (48 \text{ in}) \times (38.4 \text{ in})$$

$$V_{c,a} = 119.52 \text{ kip}$$

The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5 \text{ ksi} \rightarrow 2500 \text{ psi}$,

22.5.5.1.2 $V_{c,b}$ - Shear strength of concrete (b)

$$V_{c,b} = \left[2\, \lambda_s \sqrt{f'_{ck}} + \left(0.05\, f'_{ck}\right)\right] b_w\, d$$

$$V_{c,b} = \left[2 \times (0.64282) \times \sqrt{(2500 \text{ psi})} + (0.05 \times (2500 \text{ psi}))\right] \times (48 \text{ in}) \times (38.4 \text{ in})$$

$$V_{c,b} = 348.89 \text{ kip}$$

V_c - Governing shear strength of concrete

$$V_c = Min\left[V_{c,max}, V_{c,a}, V_{c,b}\right]$$

$$V_c = Min\left[(296.21 \text{ kip}), (119.52 \text{ kip}), (348.89 \text{ kip})\right]$$

$$V_c = 119.52 \text{ kip}$$

The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5 \text{ ksi} \rightarrow 2500 \text{ psi}$,

22.5.1.2 $V_{s,a}$ - Shear strength of steel (a)

$$V_{s,a} = 8 \sqrt{f'_{ck}}\, b_w\, d$$

$$V_{s,a} = 8 \times \sqrt{(2500 \text{ psi})} \times (48 \text{ in}) \times (38.4 \text{ in})$$

$$V_{s,a} = 737.28 \text{ kip}$$

A_v - Ties rebar area,

$$A_v = \frac{\pi\, d_{ties}^2}{4}$$

$$A_v = \frac{\pi \times (0.375 \text{ in})^2}{4}$$

$$A_v = 0.11045 \text{ in}^2$$

22.5.8.5.3 $V_{s,b}$ - Shear strength of steel (b)

$$V_{s,b} = \frac{2\, A_v\, f_{ywk}\, d}{s_{ties}}$$

$$V_{s,b} = \frac{2 \times \left(0.11045 \text{ in}^2\right) \times (60 \text{ ksi}) \times (38.4 \text{ in})}{(10 \text{ in})}$$

$$V_{s,b} = 50.894 \text{ kip}$$

V_s - Governing shear strength of steel

$$V_s = MIN\left[V_{s,a}, V_{s,b}\right]$$

$$V_s = MIN\left[(737.28 \text{ kip}), (50.894 \text{ kip})\right]$$

$$V_s = 50.894 \text{ kip}$$

22.5.1.1 ϕV_n - Allowable shear strength

$$\phi V_n = \phi\, \left(V_c + V_s\right)$$

$$\phi V_n = (0.65) \times ((119.52 \text{ kip}) + (50.894 \text{ kip}))$$

$$\phi V_n = 110.77 \text{ kip}$$

Considering x-direction:

$V_{max} = 3.6348 \text{ kip}$ - Maximum shear force in the x-direction,
$Ratio$ - Capacity

$$Ratio = \frac{V_{max}}{\phi V_n}$$

	$$Ratio = \frac{(3.6348\text{ kip})}{(110.77\text{ kip})}$$ $$Ratio = 0.032815$$	Status: **PASS** Ratio: **0.030**
	Considering z-direction: $V_{max} = 0.17604\text{ kip}$ - Maximum shear force in the z-direction, $Ratio$ - Capacity $$Ratio = \frac{V_{max}}{\phi V_n}$$ $$Ratio = \frac{(0.17604\text{ kip})}{(110.77\text{ kip})}$$ $$Ratio = 0.0015892$$	Status: **PASS** Ratio: **0.000**
14.5.2.1b	**Flexural Strength (ACI 318-19, LRFD)** S_m - Section modulus $$S_m = \frac{b\,D^2}{6}$$ $$S_m = \frac{(48\text{ in}) \times (48\text{ in})^2}{6}$$ $$S_m = 18432\text{ in}^3$$ $\lambda = 1$ - Concrete modification factor (Normal concrete), Allowable flexural strength: M_n shall be the lesser of: $\phi M_{n,1}$ $$\phi M_{n,1} = \phi \times 5 \times \lambda \times \sqrt{(f_c')} \times S_m$$ $$\phi M_{n,1} = 0.65 \times 5 \times 1 \times \sqrt{(2.5ksi)} \times 18432.001in^3$$ $$\phi M_{n,1} = 249.600kipft$$ $\phi M_{n,2}$ $$\phi M_{n,2} = \phi\,0.85\,f_{ck}'\,S_m$$ $$\phi M_{n,2} = (0.65) \times 0.85 \times (2.5\text{ ksi}) \times \left(18432\text{ in}^3\right)$$ $$\phi M_{n,2} = 2121.6\text{ kipft}$$ Therefore, ϕM_n - Allowable flexural strength, $$\phi M_n = MIN[\phi M_{n,1}, \phi M_{n,2}]$$ $$\phi M_n = MIN[(249.6\text{ kipft}), (2121.6\text{ kipft})]$$ $$\phi M_n = 249.6\text{ kipft}$$ **Considering x-direction:** $M_{max} = 8.5108\text{ kipft}$ - Maximum moment in the x-direction, $Ratio$ - Capacity $$Ratio = \frac{M_{max}}{\phi M_n}$$ $$Ratio = \frac{(8.5108\text{ kipft})}{(249.6\text{ kipft})}$$ $$Ratio = 0.034098$$	Status: **PASS** Ratio: **0.030**
	Considering z-direction: $M_{max} = 0.3785\text{ kipft}$ - Maximum moment in the z-direction, $Ratio$ - Capacity $$Ratio = \frac{M_{max}}{\phi M_n}$$	

	$$Ratio = \frac{(0.3785 \text{ kipft})}{(249.6 \text{ kipft})}$$ $$Ratio = 0.0015164$$	Status: **PASS** Ratio: **0.000**

REFERENCES	CALCULATIONS	RESULTS

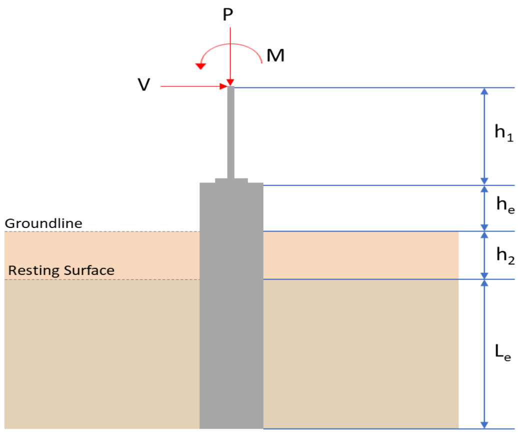
SkyCiv Foundation Design

Pile Foundation

Design Information :

Design code : IBC 2021 (International Building Code)
Unit System : Imperial

Pile Input



Geometry

Pile shape: rectangular
$b = 48\ \text{in}$ - Pile width
$D = 48\ \text{in}$ - Pile depth
$L = 4.75\ \text{ft}$ - Total pile length
$h_1 = 0\ \text{ft}$ - Lateral load height from the top of the pile,
$h_2 = 0\ \text{ft}$ - Depth to resisting surface
$h_e = 0\ \text{ft}$ - Length of pile above the ground

Tabulation of Soil Parameters

Layer	Label	Allowable Bearing Pressure (q_a) (psf)	Allowable Lateral Pressure (R) (psf/ft)
1	Sand, silty sand, clayey sand, silty gravel & clayey gravel	2000.000	150.000

Tabulation of Loads

Load Component	ASD	LRFD
P (kip)	4.946	7.751
V_x (kip)	-0.262	-0.438
V_z (kip)	-0.091	-0.146
M_x (kipft)	-0.300	-0.482
M_z (kipft)	8.461	14.505

Material Properties

$f'_{ck} = 2.5\ \text{ksi}$ - Concrete strength,

Required depth to resist lateral loads (ASD)

H - Point of application of the lateral load

$$H = h_1 + h_2 + h_e$$

$$H = (0\ \text{ft}) + (0\ \text{ft}) + (0\ \text{ft})$$

$$H = 0\ \text{ft}$$

Considering x-direction:

H_o - Lateral force per length of pile,

$$H_o = \frac{V_x}{1.57\ D}$$

$$H_o = \frac{(-0.262\ \text{kip})}{1.57 \times (48\ \text{in})}$$

$$H_o = -0.04172\ \text{kip/ft}$$

M_o - Moment per length of pile,

$$M_o = \frac{M_z + (V_x\, H)}{1.57\, D}$$

$$M_o = \frac{(8.461\ \text{kipft}) + ((-0.262\ \text{kip}) \times (0\ \text{ft}))}{1.57 \times (48\ \text{in})}$$

$$M_o = 1.3473\ \text{kipft/ft}$$

Required depth of embedment in earth:

$$L_x^3 - \left(14.14 \times \frac{H_o \times L_x}{R}\right) - \left(18.85 \times \frac{M_o}{R}\right) = 0$$

Solving the cubic equation:
$L_{e,x} = 4.5838\ \text{ft}$ - Required depth in x-direction,

Considering z-direction:

H_o - Lateral force per length of pile,

$$H_o = \frac{V_z}{1.57\, b}$$

$$H_o = \frac{(-0.091\ \text{kip})}{1.57 \times (48\ \text{in})}$$

$$H_o = -0.01449\ \text{kip/ft}$$

M_o - Moment per length of pile,

$$M_o = \frac{M_x + (V_z\, H)}{1.57\, b}$$

$$M_o = \frac{(0.3\ \text{kipft}) + ((-0.091\ \text{kip}) \times (0\ \text{ft}))}{1.57 \times (48\ \text{in})}$$

$$M_o = 0.047771\ \text{kipft/ft}$$

Required depth of embedment in earth:

$$L_z^3 - \left(14.14 \times \frac{H_o \times L_z}{R}\right) - \left(18.85 \times \frac{M_o}{R}\right) = 0$$

Solving the cubic equation:
$L_{e,z} = 1.3791\ \text{ft}$ - Required depth in z-direction,

Minimum embedded depth required:

$L_{e,req}$ - Depth of pile required,

$$L_{e,req} = MAX[L_{e,x}, L_{e,z}]$$

$$L_{e,req} = MAX[(4.5838\ \text{ft}), (1.3791\ \text{ft})]$$

$$L_{e,req} = 4.584\ \text{ft}$$

L_e - Actual embedded length of pile,

$$L_e = L - h_e - h_2$$

$$L_e = (4.75\ \text{ft}) - (0\ \text{ft}) - (0\ \text{ft})$$

$$L_e = 4.75\ \text{ft}$$

$Ratio$ - Embedded depth

$$Ratio = \frac{L_{e,req}}{L_e}$$

$$Ratio = \frac{(4.584\ \text{ft})}{(4.75\ \text{ft})}$$

$$Ratio = 0.96505$$

Status: **PASS**
Ratio: **0.970**

End-bearing Capacity (ASD)

A - Pile cross-section area

$$A = b\, D$$

$$A = (48\ \text{in}) \times (48\ \text{in})$$

$$A = 16\ \text{ft}^2$$

q - End-bearing pressure

$$q = \frac{P_v}{A}$$

$$q = \frac{(4.946\ \text{kip})}{(16\ \text{ft}^2)}$$

$$q = 0.30912\ \text{kip/ft}^2$$

Check bearing capacity ratio:

$Ratio$ - Capacity

$$Ratio = \frac{q}{q_a}$$

$$Ratio = \frac{(0.30912\ \text{kip/ft}^2)}{(2000\ \text{psf})}$$

$$Ratio = 0.15456$$

Status: **PASS**
Ratio: **0.150**

Czerniak

Lateral Soil Pressure (ASD):

L/D - Length to least lateral dimension ratio,

$$L/D = \frac{L}{D}$$

$$L/D = \frac{(4.75\ \text{ft})}{(48\ \text{in})}$$

$$L/D = 1.1875$$

Since L/D $\leq$ 10,

Pile is short.

Considering x-direction:

$H_o = -0.04172\ \text{kip/ft}$ - Lateral force per length of pile,
$M_o = 1.3473\ \text{kipft/ft}$ - Overturning moment per length of pile,
a - Distance from resting surface to pivot point,

$$a = \frac{(4\,M_o\,L_e) + \left(3\,H_o\,L_e^2\right)}{(6\,M_o) + (4\,H_o\,L_e)}$$

$$a = \frac{(4 \times (1.3473\ \text{kipft/ft}) \times (4.75\ \text{ft})) + \left(3 \times (-0.04172\ \text{kip/ft}) \times (4.75\ \text{ft})^2\right)}{(6 \times (1.3473\ \text{kipft/ft})) + (4 \times (-0.04172\ \text{kip/ft}) \times (4.75\ \text{ft}))}$$

$$a = 3.202\ \text{ft}$$

p - Earth pressure against the pile at distance a/2 from resting surface,

$$p = \frac{0.75\,[(4\,M_o) + (3\,H_o\,L_e)]^2}{L_e^2\,[(3\,M_o) + (2\,H_o\,L_e)]}$$

$$p = \frac{0.75 \times [(4 \times (1.3473\ \text{kipft/ft})) + (3 \times (-0.04172\ \text{kip/ft}) \times (4.75\ \text{ft}))]^2}{(4.75\ \text{ft})^2 \times [(3 \times (1.3473\ \text{kipft/ft})) + (2 \times (-0.04172\ \text{kip/ft}) \times (4.75\ \text{ft}))]}$$

$$p = 0.20962\ \text{kip/ft}^2$$

s - Earth pressure against the pile at distance L_e,

$$s = \frac{6\,[(2\,M_o) + (H_o\,L_e)]}{L_e^2}$$

$$s = \frac{6 \times [(2 \times (1.3473\ \text{kipft/ft})) + ((-0.04172\ \text{kip/ft}) \times (4.75\ \text{ft}))]}{(4.75\ \text{ft})^2}$$

$$s = 0.66387\ \text{kip/ft}^2$$

Check lateral soil pressure capacity:

p_a - Allowable lateral soil pressure at depth a/2,

$$p_a = R\,\frac{a}{2}$$

$$p_a = (150\ \text{psf/ft}) \times \frac{(3.202\ \text{ft})}{2}$$

$$p_a = 0.24015\ \text{kip/ft}^2$$

$Ratio$ - Lateral soil capacity

$$Ratio = \frac{p}{p_a}$$

$$Ratio = \frac{\left(0.20962\ \mathrm{kip/ft^2}\right)}{\left(0.24015\ \mathrm{kip/ft^2}\right)}$$

$$Ratio = 0.87286$$

Status: **PASS**
Ratio: **0.870**

p_s - Allowable lateral soil pressure at depth L_e,

$$p_s = R\,L_e$$

$$p_s = (150\ \mathrm{psf/ft}) \times (4.75\ \mathrm{ft})$$

$$p_s = 0.7125\ \mathrm{kip/ft^2}$$

$Ratio$ - Lateral soil capacity

$$Ratio = \frac{s}{p_s}$$

$$Ratio = \frac{\left(0.66387\ \mathrm{kip/ft^2}\right)}{\left(0.7125\ \mathrm{kip/ft^2}\right)}$$

$$Ratio = 0.93174$$

Status: **PASS**
Ratio: **0.930**

Considering z-direction:

$H_o = -0.01449\ \mathrm{kip/ft}$ - Lateral force per length of pile,
$M_o = 0.047771\ \mathrm{kipft/ft}$ - Overturning moment per length of pile,
a - Distance from resting surface to pivot point,

$$a = \frac{(4\,M_o\,L_e) + \left(3\,H_o\,L_e^2\right)}{(6\,M_o) + (4\,H_o\,L_e)}$$

$$a = \frac{(4 \times (0.047771\ \mathrm{kipft/ft}) \times (4.75\ \mathrm{ft})) + \left(3 \times (-0.01449\ \mathrm{kip/ft}) \times (4.75\ \mathrm{ft})^2\right)}{(6 \times (0.047771\ \mathrm{kipft/ft})) + (4 \times (-0.01449\ \mathrm{kip/ft}) \times (4.75\ \mathrm{ft}))}$$

$$a = 3.3606\ \mathrm{ft}$$

p - Earth pressure against the pile at distance a/2 from resting surface,

$$p = \frac{0.75\,[(4\,M_o) + (3\,H_o\,L_e)]^2}{L_e^2\,[(3\,M_o) + (2\,H_o\,L_e)]}$$

$$p = \frac{0.75 \times [(4 \times (0.047771\ \mathrm{kipft/ft})) + (3 \times (-0.01449\ \mathrm{kip/ft}) \times (4.75\ \mathrm{ft}))]^{\,2}}{(4.75\ \mathrm{ft})^2 \times [(3 \times (0.047771\ \mathrm{kipft/ft})) + (2 \times (-0.01449\ \mathrm{kip/ft}) \times (4.75\ \mathrm{ft}))]}$$

$$p = 0.0013957\ \mathrm{kip/ft^2}$$

s - Earth pressure against the pile at distance L_e,

$$s = \frac{6\,[(2\,M_o) + (H_o\,L_e)]}{L_e^2}$$

$$s = \frac{6 \times [(2 \times (0.047771\ \mathrm{kipft/ft})) + ((-0.01449\ \mathrm{kip/ft}) \times (4.75\ \mathrm{ft}))]}{(4.75\ \mathrm{ft})^2}$$

$$s = 0.0071034\ \mathrm{kip/ft^2}$$

Check lateral soil pressure capacity:

p_a - Allowable lateral soil pressure at depth a/2,

$$p_a = R\,\frac{a}{2}$$

$$p_a = (150\ \mathrm{psf/ft}) \times \frac{(3.3606\ \mathrm{ft})}{2}$$

$$p_a = 0.25205\ \mathrm{kip/ft^2}$$

$Ratio$ - Lateral soil capacity

$$Ratio = \frac{p}{p_a}$$

$$Ratio = \frac{\left(0.0013957\ \mathrm{kip/ft^2}\right)}{\left(0.25205\ \mathrm{kip/ft^2}\right)}$$

$$Ratio = 0.0055375$$

Status: **PASS**
Ratio: **0.010**

p_s - Allowable lateral soil pressure at depth L_e,

$$p_s = R\,L_e$$

$$p_s = (150\ \mathrm{psf/ft}) \times (4.75\ \mathrm{ft})$$

$$p_s = 0.7125\ \mathrm{kip/ft^2}$$

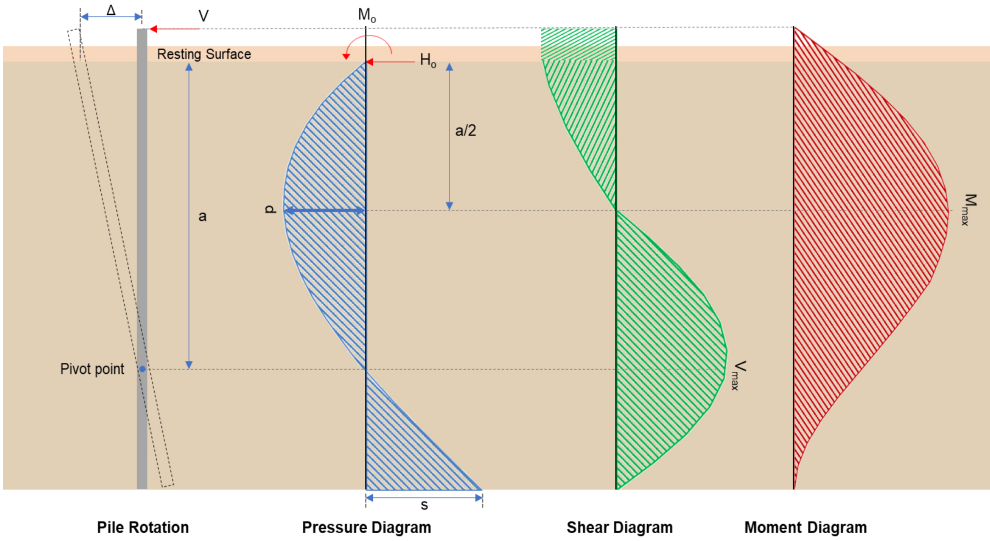
$Ratio$ - Lateral soil capacity

$$Ratio = \frac{s}{p_s}$$

$$Ratio = \frac{\left(0.0071034\ \mathrm{kip/ft^2}\right)}{\left(0.7125\ \mathrm{kip/ft^2}\right)}$$

$$Ratio = 0.0099697$$

Status: **PASS**
Ratio: **0.010**



Shear force and Bending moment (x-direction, LRFD)

H_o - Lateral force per length of pile,

$$H_o = \frac{V_x}{1.57\ D}$$

$$H_o = \frac{(-0.438\ \mathrm{kip})}{1.57 \times (48\ \mathrm{in})}$$

$$H_o = -0.069745\ \mathrm{kip/ft}$$

M_o - Moment per length of pile,

$$M_o = \frac{M_z + (V_x\ H)}{1.57\ D}$$

$$M_o = \frac{(14.505\ \mathrm{kipft}) + ((-0.438\ \mathrm{kip}) \times (0\ \mathrm{ft}))}{1.57 \times (48\ \mathrm{in})}$$

$$M_o = 2.3097\ \mathrm{kipft/ft}$$

E - Distance from lateral load to resisting surface,

$$E = \frac{M_o}{H_o}$$

$$E = \frac{(2.3097\ \mathrm{kipft/ft})}{(-0.069745\ \mathrm{kip/ft})}$$

$$E = 33.116\ \mathrm{ft}$$

a - Distance from resting surface to pivot point,

$$a = \frac{(4\ M_o\ L_e) + \left(3\ H_o\ L_e^2\right)}{(6\ M_o) + (4\ H_o\ L_e)}$$

$$a = \frac{(4 \times (2.3097\ \mathrm{kipft/ft}) \times (4.75\ \mathrm{ft})) + \left(3 \times (-0.069745\ \mathrm{kip/ft}) \times (4.75\ \mathrm{ft})^2\right)}{\cdots}$$

$$a = \frac{}{(6 \times (2.3097\ \text{kipft/ft})) + (4 \times (-0.069745\ \text{kip/ft}) \times (4.75\ \text{ft}))}$$

$$a = 3.2012\ \text{ft}$$

V_{max} - Max shear force located at depth a,

$$V_{max} = (H_o\, D) \left[1 - \left[3 \left(\frac{4\,E}{L_e} + 3\right) \left(\frac{a}{L_e}\right)^2\right] + \left[4 \left(\frac{3\,E}{L_e} + 2\right) \left(\frac{a}{L_e}\right)^3\right]\right]$$

$$V_{max} = ((-0.069745\ \text{kip/ft}) \times (48\ \text{in})) \times \left[1 - \left[3 \times \left(\frac{4 \times (33.116\ \text{ft})}{(4.75\ \text{ft})} + 3\right) \times \left(\frac{(3.2012\ \text{ft})}{(4.75\ \text{ft})}\right)^2\right] + \left[4 \times \left(\frac{3 \times (33.116\ \text{ft})}{(4.75\ \text{ft})} + 2\right) \times \left(\frac{(3.2012\ \text{ft})}{(4.75\ \text{ft})}\right)^3\right]\right]$$

$$V_{max} = 3.6348\ \text{kip}$$

M_{max} - Max bending moment located at depth a/2,

$$M_{max} = (H_o\, D\, L_e) \left[\left(\frac{E}{L_e} + \frac{a}{2\,L_e}\right) - \left[\left(\frac{4\,E}{L_e} + 3\right) \left(\frac{a}{2\,L_e}\right)^3\right] + \left[\left(\frac{3\,E}{L_e} + 2\right) \left(\frac{a}{2\,L_e}\right)^4\right]\right]$$

$$M_{max} = ((-0.069745\ \text{kip/ft}) \times (48\ \text{in}) \times (4.75\ \text{ft})) \times \left[\left(\frac{(33.116\ \text{ft})}{(4.75\ \text{ft})} + \frac{(3.2012\ \text{ft})}{2 \times (4.75\ \text{ft})}\right) - \left[\left(\frac{4 \times (33.116\ \text{ft})}{(4.75\ \text{ft})} + 3\right) \times \left(\frac{(3.2012\ \text{ft})}{2 \times (4.75\ \text{ft})}\right)^3\right] + \left[\left(\frac{3 \times (33.116\ \text{ft})}{(4.75\ \text{ft})} + 2\right) \times \left(\frac{(3.2012\ \text{ft})}{2 \times (4.75\ \text{ft})}\right)^4\right]\right]$$

$$M_{max} = 8.5108\ \text{kipft}$$

Shear force and Bending moment (z-direction, LRFD)

H_o - Lateral force per length of pile,

$$H_o = \frac{V_z}{1.57\,b}$$

$$H_o = \frac{(-0.146\ \text{kip})}{1.57 \times (48\ \text{in})}$$

$$H_o = -0.023248\ \text{kip/ft}$$

M_o - Moment per length of pile,

$$M_o = \frac{M_x + (V_z\,H)}{1.57\,b}$$

$$M_o = \frac{(0.482\ \text{kipft}) + ((-0.146\ \text{kip}) \times (0\ \text{ft}))}{1.57 \times (48\ \text{in})}$$

$$M_o = 0.076752\ \text{kipft/ft}$$

E - Distance from lateral load to resisting surface,

$$E = \frac{M_o}{H_o}$$

$$E = \frac{(0.076752\ \text{kipft/ft})}{(-0.023248\ \text{kip/ft})}$$

$$E = 3.3014\ \text{ft}$$

a - Distance from resting surface to pivot point,

$$a = \frac{(4\,M_o\,L_e) + \left(3\,H_o\,L_e^2\right)}{(6\,M_o) + (4\,H_o\,L_e)}$$

$$a = \frac{(4 \times (0.076752\ \text{kipft/ft}) \times (4.75\ \text{ft})) + \left(3 \times (-0.023248\ \text{kip/ft}) \times (4.75\ \text{ft})^2\right)}{(6 \times (0.076752\ \text{kipft/ft})) + (4 \times (-0.023248\ \text{kip/ft}) \times (4.75\ \text{ft}))}$$

$$a = 3.3605\ \text{ft}$$

V_{max} - Max shear force located at depth a,

$$V_{max} = (H_o\, b) \left[1 - \left[3 \left(\frac{4\,E}{L_e} + 3\right) \left(\frac{a}{L_e}\right)^2\right] + \left[4 \left(\frac{3\,E}{L_e} + 2\right) \left(\frac{a}{L_e}\right)^3\right]\right]$$

$$V_{max} = ((-0.023248\ \text{kip/ft}) \times (48\ \text{in})) \times \left[1 - \left[3 \times \left(\frac{4 \times (3.3014\ \text{ft})}{(4.75\ \text{ft})} + 3\right) \times \left(\frac{(3.3605\ \text{ft})}{(4.75\ \text{ft})}\right)^2\right] + \left[4 \times \left(\frac{3 \times (3.3014\ \text{ft})}{(4.75\ \text{ft})} + 2\right) \times \left(\frac{(3.3605\ \text{ft})}{(4.75\ \text{ft})}\right)^3\right]\right]$$

$$V_{max} = 0.17604\ \text{kip}$$

M_{max} - Max bending moment located at depth a/2,

$$M_{max} = (H_o\, b\, L_e)\left[\left(\frac{E}{L_e} + \frac{a}{2\,L_e}\right) - \left[\left(\frac{4\,E}{L_e} + 3\right)\left(\frac{a}{2\,L_e}\right)^3\right] + \left[\left(\frac{3\,E}{L_e} + 2\right)\left(\frac{a}{2\,L_e}\right)^4\right]\right]$$

$$M_{max} = ((-0.023248\ \text{kip/ft}) \times (48\ \text{in}) \times (4.75\ \text{ft})) \times \left[\left(\frac{(3.3014\ \text{ft})}{(4.75\ \text{ft})} + \frac{(3.3605\ \text{ft})}{2 \times (4.75\ \text{ft})}\right) - \left[\left(\frac{4 \times (3.3014\ \text{ft})}{(4.75\ \text{ft})} + 3\right) \times \left(\frac{(3.3605\ \text{ft})}{2 \times (4.75\ \text{ft})}\right)^3\right] + \left[\left(\frac{3 \times (3.3014\ \text{ft})}{(4.75\ \text{ft})} + 2\right) \times \left(\frac{(3.3605\ \text{ft})}{2 \times (4.75\ \text{ft})}\right)^4\right]\right]$$

$$M_{max} = 0.3785\ \text{kipft}$$

Minimum Reinforcement Check (LRFD)

Parameters:

$f'_{ck} = 2.5\ \text{ksi}$ - Concrete strength,
$f_{yk} = 60\ \text{ksi}$ - Longitudinal reinforcement strength,
$\phi = 0.65$ - Reduction factor for axial strength,
Table 22.4.2.1 $\alpha = 0.8$ - Alpha factor for axial strength,
$A_g = 2304\ \text{in}^2$ - Gross area of concrete,

Longitudinal reinforcement:

Required reinforcement due to axial load, $A_{st,required}$

22.4.2.2, 10.6.1.1 $A_{st,required}$

$$A_{st,required} = Min\left[\frac{\frac{P}{\phi\,\alpha} - (0.85\, f'_{ck}\, A_g)}{f_{yk} - (0.85\, f'_{ck})}, (0.08\, A_g)\right]$$

$$A_{st,required} = Min\left[\frac{\frac{(7.751\ \text{kip})}{(0.65) \times (0.8)} - (0.85 \times (2.5\ \text{ksi}) \times (2304\ \text{in}^2))}{(60\ \text{ksi}) - (0.85 \times (2.5\ \text{ksi}))}, (0.08 \times (2304\ \text{in}^2))\right]$$

$$A_{st,required} = -84.339\ \text{in}^2$$

A_{min} - Governing minimum reinforcement area,

$$A_{min} = Max\left[A_{st,required}, (0.0018\, A_g)\right]$$

$$A_{min} = Max\left[(-84.339\ \text{in}^2), (0.0018 \times (2304\ \text{in}^2))\right]$$

$$A_{min} = 4.1472\ \text{in}^2$$

n_{rebar} - Required number of reinforcement,

$$n_{rebar} = \frac{A_{min}}{A_{rebar}}$$

$$n_{rebar} = \frac{(4.1472\ \text{in}^2)}{(0.3068\ \text{in}^2)}$$

$$n_{rebar} = 14$$

A_{st} - Actual total reinforcement area,

$$A_{st} = n_{rebar}\,\frac{\pi\, d_{bar}^2}{4}$$

$$A_{st} = (14) \times \frac{\pi \times (0.625\ \text{in})^2}{4}$$

$$A_{st} = 4.2951\ \text{in}^2$$

$Ratio$ - Capacity

$$Ratio = \frac{A_{min}}{A_{st}}$$

$$Ratio = \frac{(4.1472\ \text{in}^2)}{(4.2951\ \text{in}^2)}$$

$$Ratio = 0.96556$$

Status: PASS
Ratio: 0.970

25.2.3 s_{rebar} - Minimum spacing of reinforcement,

$$s_{rebar} = Max\left[1.5, (1.5\, d_{bar})\right]$$

$$s_{rebar} = Max\left[1.5, (1.5 \times (0.625\text{ in}))\right]$$

$$s_{rebar} = 1.5\text{ in}$$

Ties:

25.7.2.2 Since longitudinal reinforcement is $\leq$ No. 10ø: Use #3(0.375 in)

25.7.2.1 s_{ties} - Maximum spacing of ties,

$$s_{ties} = Min\left[(16\, d_{bar}), (48\, d_{ties}), Min\,(D, b)\right]$$

$$s_{ties} = Min\left[(16 \times (0.625\text{ in})), (48 \times (0.375\text{ in})), Min\,((48\text{ in}), (48\text{ in}))\right]$$

$$s_{ties} = 10\text{ in}$$

Summary:

Main reinforcement: **14 - #5 (0.625 in)**
Ties: **#3(0.375 in) - 10 in**

Axial Compression Strength (ACI 318-19, LRFD)

22.4.2.2 ϕP_N - Allowable axial compressive strength

$$\phi P_N = \phi\, 0.80\, \left[\left(0.85\, f'_{ck}\, \left[A_g - A_{st}\right]\right) + \left(f_{yk}\, A_{st}\right)\right]$$

$$\phi P_N = (0.65) \times 0.80 \times \left[\left(0.85 \times (2.5\text{ ksi}) \times \left[\left(2304\text{ in}^2\right) - \left(4.2951\text{ in}^2\right)\right]\right) + \left(\left(60\text{ ksi}\right) \times \left(4.2951\text{ in}^2\right)\right)\right]$$

$$\phi P_N = 2675.2\text{ kip}$$

$Ratio$ - Capacity

$$Ratio = \frac{P}{\phi P_N}$$

$$Ratio = \frac{(7.751\text{ kip})}{(2675.2\text{ kip})}$$

$$Ratio = 0.0028974$$

Status: PASS
Ratio: 0.000

Shear Strength (ACI 318-19, LRFD)

Parameters:

$b_w = 48\text{ in}$ - Effective width,

22.5.2.2 d - Effective depth

$$d = 0.80\, D$$

$$d = 0.80 \times (48\text{ in})$$

$$d = 38.4\text{ in}$$

22.5.5.1.3 λ_s - size effect modification factor

$$\lambda_s = MIN\left[\sqrt{\frac{2}{1 + \frac{d}{10}}}, 1\right]$$

$$\lambda_s = MIN\left[\sqrt{\frac{2}{1 + \frac{(38.4\text{ in})}{10}}}, 1\right]$$

$$\lambda_s = 0.64282$$

The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5\text{ ksi} \rightarrow 2500\text{ psi}$,

22.5.5.1.1 $V_{c,max}$ - Max shear strength of concrete

$$V_{c,max} = 5\, \lambda_s\, \sqrt{f'_{ck}}\, b_w\, d$$

$$V_{c,max} = 5 \times (0.64282) \times \sqrt{(2500\text{ psi})} \times (48\text{ in}) \times (38.4\text{ in})$$

$$V_{c,max} = 296.21 \text{ kip}$$

The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5 \text{ ksi} \rightarrow 2500 \text{ psi}$, $P = 7.751 \text{ kip} \rightarrow 7751 \text{ lbf}$,

22.5.5.1.1(a) $V_{c,a}$ - Shear strength of concrete (a)

$$V_{c,a} = \left[2\, \lambda_s\, \sqrt{f'_{ck}} + \frac{P}{6\, A_g}\right]\, b_w\, d$$

$$V_{c,a} = \left[2 \times (0.64282) \times \sqrt{(2500 \text{ psi})} + \frac{(7751 \text{ lbf})}{6 \times (2304 \text{ in}^2)}\right] \times (48 \text{ in}) \times (38.4 \text{ in})$$

$$V_{c,a} = 119.52 \text{ kip}$$

The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5 \text{ ksi} \rightarrow 2500 \text{ psi}$,

22.5.5.1.2 $V_{c,b}$ - Shear strength of concrete (b)

$$V_{c,b} = \left[2\, \lambda_s\, \sqrt{f'_{ck}} + \left(0.05\, f'_{ck}\right)\right]\, b_w\, d$$

$$V_{c,b} = \left[2 \times (0.64282) \times \sqrt{(2500 \text{ psi})} + (0.05 \times (2500 \text{ psi}))\right] \times (48 \text{ in}) \times (38.4 \text{ in})$$

$$V_{c,b} = 348.89 \text{ kip}$$

V_c - Governing shear strength of concrete

$$V_c = Min\left[V_{c,max}, V_{c,a}, V_{c,b}\right]$$

$$V_c = Min\left[(296.21 \text{ kip}), (119.52 \text{ kip}), (348.89 \text{ kip})\right]$$

$$V_c = 119.52 \text{ kip}$$

The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5 \text{ ksi} \rightarrow 2500 \text{ psi}$,

22.5.1.2 $V_{s,a}$ - Shear strength of steel (a)

$$V_{s,a} = 8\, \sqrt{f'_{ck}}\, b_w\, d$$

$$V_{s,a} = 8 \times \sqrt{(2500 \text{ psi})} \times (48 \text{ in}) \times (38.4 \text{ in})$$

$$V_{s,a} = 737.28 \text{ kip}$$

A_v - Ties rebar area,

$$A_v = \frac{\pi\, d_{ties}^2}{4}$$

$$A_v = \frac{\pi \times (0.375 \text{ in})^2}{4}$$

$$A_v = 0.11045 \text{ in}^2$$

22.5.8.5.3 $V_{s,b}$ - Shear strength of steel (b)

$$V_{s,b} = \frac{2\, A_v\, f_{ywk}\, d}{s_{ties}}$$

$$V_{s,b} = \frac{2 \times \left(0.11045 \text{ in}^2\right) \times (60 \text{ ksi}) \times (38.4 \text{ in})}{(10 \text{ in})}$$

$$V_{s,b} = 50.894 \text{ kip}$$

V_s - Governing shear strength of steel

$$V_s = MIN\left[V_{s,a}, V_{s,b}\right]$$

$$V_s = MIN\left[(737.28 \text{ kip}), (50.894 \text{ kip})\right]$$

$$V_s = 50.894 \text{ kip}$$

22.5.1.1 ϕV_n - Allowable shear strength

$$\phi V_n = \phi\, \left(V_c + V_s\right)$$

$$\phi V_n = (0.65) \times ((119.52 \text{ kip}) + (50.894 \text{ kip}))$$

$$\phi V_n = 110.77 \text{ kip}$$

Considering x-direction:

$V_{max} = 3.6348 \text{ kip}$ - Maximum shear force in the x-direction,
$Ratio$ - Capacity

$$Ratio = \frac{V_{max}}{\phi V_n}$$

	$$Ratio = \frac{(3.6348 \text{ kip})}{(110.77 \text{ kip})}$$ $$Ratio = 0.032815$$	Status: **PASS** Ratio: **0.030**
	Considering z-direction: $V_{max} = 0.17604$ kip - Maximum shear force in the z-direction, $Ratio$ - Capacity $$Ratio = \frac{V_{max}}{\phi V_n}$$ $$Ratio = \frac{(0.17604 \text{ kip})}{(110.77 \text{ kip})}$$ $$Ratio = 0.0015892$$	Status: **PASS** Ratio: **0.000**
14.5.2.1b	**Flexural Strength (ACI 318-19, LRFD)** S_m - Section modulus $$S_m = \frac{b\,D^2}{6}$$ $$S_m = \frac{(48 \text{ in}) \times (48 \text{ in})^2}{6}$$ $$S_m = 18432 \text{ in}^3$$ $\lambda = 1$ - Concrete modification factor (Normal concrete), Allowable flexural strength: M_n shall be the lesser of: $\phi M_{n,1}$ $$\phi M_{n,1} = \phi \times 5 \times \lambda \times \sqrt{(f_c')} \times S_m$$ $$\phi M_{n,1} = 0.65 \times 5 \times 1 \times \sqrt{(2.5ksi)} \times 18432.001in^3$$ $$\phi M_{n,1} = 249.600kipft$$ $\phi M_{n,2}$ $$\phi M_{n,2} = \phi\, 0.85\, f_{ck}'\, S_m$$ $$\phi M_{n,2} = (0.65) \times 0.85 \times (2.5 \text{ ksi}) \times \left(18432 \text{ in}^3\right)$$ $$\phi M_{n,2} = 2121.6 \text{ kipft}$$ Therefore, ϕM_n - Allowable flexural strength, $$\phi M_n = MIN[\phi M_{n,1}, \phi M_{n,2}]$$ $$\phi M_n = MIN[(249.6 \text{ kipft}), (2121.6 \text{ kipft})]$$ $$\phi M_n = 249.6 \text{ kipft}$$ **Considering x-direction:** $M_{max} = 8.5108$ kipft - Maximum moment in the x-direction, $Ratio$ - Capacity $$Ratio = \frac{M_{max}}{\phi M_n}$$ $$Ratio = \frac{(8.5108 \text{ kipft})}{(249.6 \text{ kipft})}$$ $$Ratio = 0.034098$$	Status: **PASS** Ratio: **0.030**
	Considering z-direction: $M_{max} = 0.3785$ kipft - Maximum moment in the z-direction, $Ratio$ - Capacity $$Ratio = \frac{M_{max}}{\phi M_n}$$	

	$$Ratio = \frac{(0.3785 \text{ kipft})}{(249.6 \text{ kipft})}$$ $$Ratio = 0.0015164$$	Status: **PASS** Ratio: **0.000**

REFERENCES	CALCULATIONS	RESULTS

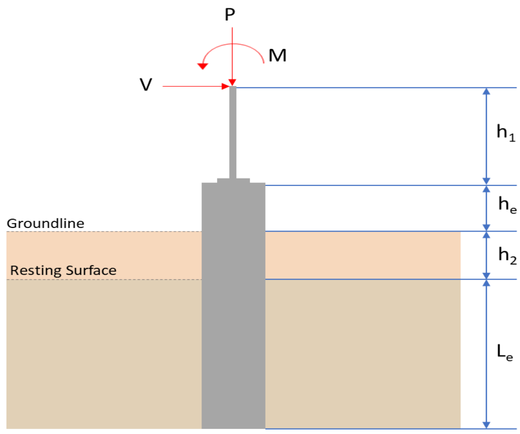
SkyCiv Foundation Design

Pile Foundation

Design Information :

Design code : IBC 2021 (International Building Code)
Unit System : Imperial

Pile Input



Geometry

Pile shape: rectangular
$b = 48$ in - Pile width
$D = 48$ in - Pile depth
$L = 5$ ft - Total pile length
$h_1 = 0$ ft - Lateral load height from the top of the pile,
$h_2 = 0$ ft - Depth to resisting surface
$h_e = 0$ ft - Length of pile above the ground

Tabulation of Soil Parameters

Layer	Label	Allowable Bearing Pressure (q_a) (psf)	Allowable Lateral Pressure (R) (psf/ft)
1	Sand, silty sand, clayey sand, silty gravel & clayey gravel	2000.000	150.000

Tabulation of Loads

Load Component	ASD	LRFD
P (kip)	5.709	8.968
V_x (kip)	-0.295	-0.491
V_z (kip)	-0.011	-0.017
M_x (kipft)	-0.038	-0.060
M_z (kipft)	9.173	15.741

Material Properties

$f'_{ck} = 2.5$ ksi - Concrete strength,

Required depth to resist lateral loads (ASD)

H - Point of application of the lateral load

$$H = h_1 + h_2 + h_e$$

$$H = (0 \text{ ft}) + (0 \text{ ft}) + (0 \text{ ft})$$

$$H = 0 \text{ ft}$$

Considering x-direction:

H_o - Lateral force per length of pile,

$$H_o = \frac{V_x}{1.57\, D}$$

$$H_o = \frac{(-0.295 \text{ kip})}{1.57 \times (48 \text{ in})}$$

$$H_o = -0.046975 \text{ kip/ft}$$

M_o - Moment per length of pile,

$$M_o = \frac{M_z + (V_x\, H)}{1.57\, D}$$

$$M_o = \frac{(9.173\ \text{kipft}) + ((-0.295\ \text{kip}) \times (0\ \text{ft}))}{1.57 \times (48\ \text{in})}$$

$$M_o = 1.4607\ \text{kipft/ft}$$

Required depth of embedment in earth:

$$L_x^3 - \left(14.14 \times \frac{H_o \times L_x}{R}\right) - \left(18.85 \times \frac{M_o}{R}\right) = 0$$

Solving the cubic equation:
$L_{e,x} = 4.6969\ \text{ft}$ - Required depth in x-direction,

Considering z-direction:

H_o - Lateral force per length of pile,

$$H_o = \frac{V_z}{1.57\, b}$$

$$H_o = \frac{(-0.011\ \text{kip})}{1.57 \times (48\ \text{in})}$$

$$H_o = -0.0017516\ \text{kip/ft}$$

M_o - Moment per length of pile,

$$M_o = \frac{M_x + (V_z\, H)}{1.57\, b}$$

$$M_o = \frac{(0.038\ \text{kipft}) + ((-0.011\ \text{kip}) \times (0\ \text{ft}))}{1.57 \times (48\ \text{in})}$$

$$M_o = 0.006051\ \text{kipft/ft}$$

Required depth of embedment in earth:

$$L_z^3 - \left(14.14 \times \frac{H_o \times L_z}{R}\right) - \left(18.85 \times \frac{M_o}{R}\right) = 0$$

Solving the cubic equation:
$L_{e,z} = 0.74062\ \text{ft}$ - Required depth in z-direction,

Minimum embedded depth required:

$L_{e,req}$ - Depth of pile required,

$$L_{e,req} = MAX[L_{e,x}, L_{e,z}]$$

$$L_{e,req} = MAX[(4.6969\ \text{ft}), (0.74062\ \text{ft})]$$

$$L_{e,req} = 4.697\ \text{ft}$$

L_e - Actual embedded length of pile,

$$L_e = L - h_e - h_2$$

$$L_e = (5\ \text{ft}) - (0\ \text{ft}) - (0\ \text{ft})$$

$$L_e = 5\ \text{ft}$$

$Ratio$ - Embedded depth

$$Ratio = \frac{L_{e,req}}{L_e}$$

$$Ratio = \frac{(4.697\ \text{ft})}{(5\ \text{ft})}$$

$$Ratio = 0.9394$$

Status: **PASS**
Ratio: **0.940**

End-bearing Capacity (ASD)

A - Pile cross-section area

$$A = b\, D$$

$$A = (48\ \text{in}) \times (48\ \text{in})$$

$$A = 16\ \text{ft}^2$$

q - End-bearing pressure

$$q = \frac{P_v}{A}$$

$$q = \frac{(5.709\ \text{kip})}{(16\ \text{ft}^2)}$$

$$q = 0.35681\ \text{kip/ft}^2$$

Check bearing capacity ratio:

$Ratio$ - Capacity

$$Ratio = \frac{q}{q_a}$$

$$Ratio = \frac{\left(0.35681\ \text{kip/ft}^2\right)}{(2000\ \text{psf})}$$

$$Ratio = 0.17841$$

Status: **PASS**
Ratio: **0.180**

Czerniak

Lateral Soil Pressure (ASD):

L/D - Length to least lateral dimension ratio,

$$L/D = \frac{L}{D}$$

$$L/D = \frac{(5\ \text{ft})}{(48\ \text{in})}$$

$$L/D = 1.25$$

Since L/D $\leq$ 10,

Pile is short.

Considering x-direction:

$H_o = -0.046975\ \text{kip/ft}$ - Lateral force per length of pile,
$M_o = 1.4607\ \text{kipft/ft}$ - Overturning moment per length of pile,
a - Distance from resting surface to pivot point,

$$a = \frac{(4\,M_o\,L_e) + \left(3\,H_o\,L_e^2\right)}{(6\,M_o) + (4\,H_o\,L_e)}$$

$$a = \frac{(4 \times (1.4607\ \text{kipft/ft}) \times (5\ \text{ft})) + \left(3 \times (-0.046975\ \text{kip/ft}) \times (5\ \text{ft})^2\right)}{(6 \times (1.4607\ \text{kipft/ft})) + (4 \times (-0.046975\ \text{kip/ft}) \times (5\ \text{ft}))}$$

$$a = 3.3737\ \text{ft}$$

p - Earth pressure against the pile at distance a/2 from resting surface,

$$p = \frac{0.75\,[(4\,M_o) + (3\,H_o\,L_e)]^2}{L_e^2\,[(3\,M_o) + (2\,H_o\,L_e)]}$$

$$p = \frac{0.75 \times [(4 \times (1.4607\ \text{kipft/ft})) + (3 \times (-0.046975\ \text{kip/ft}) \times (5\ \text{ft}))]^{\ 2}}{(5\ \text{ft})^2 \times [(3 \times (1.4607\ \text{kipft/ft})) + (2 \times (-0.046975\ \text{kip/ft}) \times (5\ \text{ft}))]}$$

$$p = 0.20244\ \text{kip/ft}^2$$

s - Earth pressure against the pile at distance L_e,

$$s = \frac{6\,[(2\,M_o) + (H_o\,L_e)]}{L_e^2}$$

$$s = \frac{6 \times [(2 \times (1.4607\ \text{kipft/ft})) + ((-0.046975\ \text{kip/ft}) \times (5\ \text{ft}))]}{(5\ \text{ft})^2}$$

$$s = 0.64475\ \text{kip/ft}^2$$

Check lateral soil pressure capacity:

p_a - Allowable lateral soil pressure at depth a/2,

$$p_a = R\,\frac{a}{2}$$

$$p_a = (150\ \text{psf/ft}) \times \frac{(3.3737\ \text{ft})}{2}$$

$$p_a = 0.25303\ \text{kip/ft}^2$$

$Ratio$ - Lateral soil capacity

$$Ratio = \frac{p}{p_a}$$

$$Ratio = \frac{(0.20244\ \mathrm{kip/ft^2})}{(0.25303\ \mathrm{kip/ft^2})}$$

$$Ratio = 0.80007$$

Status: **PASS**
Ratio: **0.800**

p_s - Allowable lateral soil pressure at depth L_e,

$$p_s = R\,L_e$$

$$p_s = (150\ \mathrm{psf/ft}) \times (5\ \mathrm{ft})$$

$$p_s = 0.75\ \mathrm{kip/ft^2}$$

$Ratio$ - Lateral soil capacity

$$Ratio = \frac{s}{p_s}$$

$$Ratio = \frac{(0.64475\ \mathrm{kip/ft^2})}{(0.75\ \mathrm{kip/ft^2})}$$

$$Ratio = 0.85967$$

Status: **PASS**
Ratio: **0.860**

Considering z-direction:

$H_o = -0.0017516\ \mathrm{kip/ft}$ - Lateral force per length of pile,
$M_o = 0.006051\ \mathrm{kipft/ft}$ - Overturning moment per length of pile,
a - Distance from resting surface to pivot point,

$$a = \frac{(4\,M_o\,L_e) + (3\,H_o\,L_e^2)}{(6\,M_o) + (4\,H_o\,L_e)}$$

$$a = \frac{(4 \times (0.006051\ \mathrm{kipft/ft}) \times (5\ \mathrm{ft})) + \left(3 \times (-0.0017516\ \mathrm{kip/ft}) \times (5\ \mathrm{ft})^2\right)}{(6 \times (0.006051\ \mathrm{kipft/ft})) + (4 \times (-0.0017516\ \mathrm{kip/ft}) \times (5\ \mathrm{ft}))}$$

$$a = 3.5379\ \mathrm{ft}$$

p - Earth pressure against the pile at distance a/2 from resting surface,

$$p = \frac{0.75\,[(4\,M_o) + (3\,H_o\,L_e)]^2}{L_e^2\,[(3\,M_o) + (2\,H_o\,L_e)]}$$

$$p = \frac{0.75 \times [(4 \times (0.006051\ \mathrm{kipft/ft})) + (3 \times (-0.0017516\ \mathrm{kip/ft}) \times (5\ \mathrm{ft}))]^{\ 2}}{(5\ \mathrm{ft})^2 \times [(3 \times (0.006051\ \mathrm{kipft/ft})) + (2 \times (-0.0017516\ \mathrm{kip/ft}) \times (5\ \mathrm{ft}))]}$$

$$p = 0.00020183\ \mathrm{kip/ft^2}$$

s - Earth pressure against the pile at distance L_e,

$$s = \frac{6\,[(2\,M_o) + (H_o\,L_e)]}{L_e^2}$$

$$s = \frac{6 \times [(2 \times (0.006051\ \mathrm{kipft/ft})) + ((-0.0017516\ \mathrm{kip/ft}) \times (5\ \mathrm{ft}))]}{(5\ \mathrm{ft})^2}$$

$$s = 0.00080255\ \mathrm{kip/ft^2}$$

Check lateral soil pressure capacity:

p_a - Allowable lateral soil pressure at depth a/2,

$$p_a = R\,\frac{a}{2}$$

$$p_a = (150\ \mathrm{psf/ft}) \times \frac{(3.5379\ \mathrm{ft})}{2}$$

$$p_a = 0.26535\ \mathrm{kip/ft^2}$$

$Ratio$ - Lateral soil capacity

$$Ratio = \frac{p}{p_a}$$

$$Ratio = \frac{(0.00020183\ \mathrm{kip/ft^2})}{(0.26535\ \mathrm{kip/ft^2})}$$

$$Ratio = 0.00076064$$

Status: **PASS**
Ratio: **0.000**

p_s - Allowable lateral soil pressure at depth L_e,

$$p_s = R\,L_e$$

$$p_s = (150\ \mathrm{psf/ft}) \times (5\ \mathrm{ft})$$

$$p_s = 0.75\ \mathrm{kip/ft^2}$$

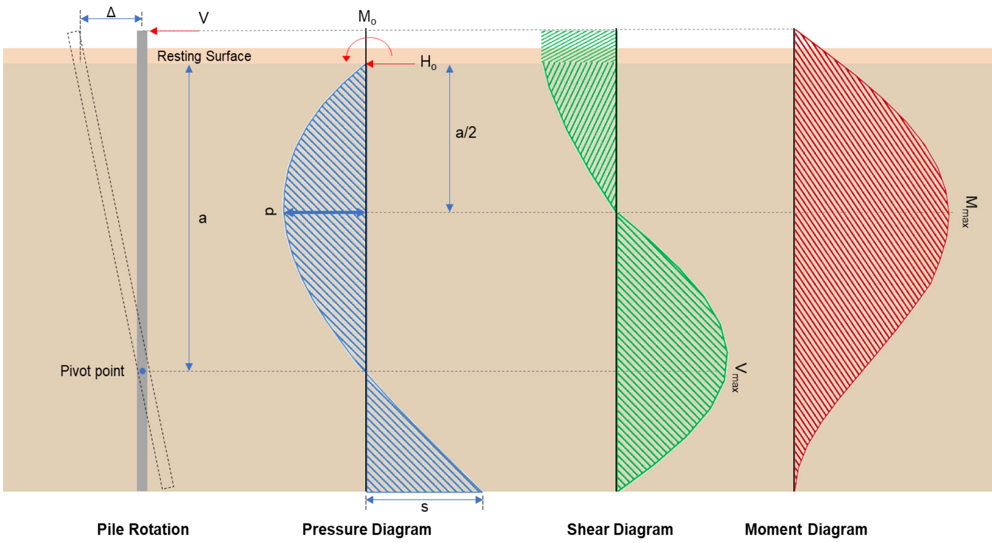
$Ratio$ - Lateral soil capacity

$$Ratio = \frac{s}{p_s}$$

$$Ratio = \frac{\left(0.00080255\ \mathrm{kip/ft^2}\right)}{\left(0.75\ \mathrm{kip/ft^2}\right)}$$

$$Ratio = 0.0010701$$

Status: **PASS**
Ratio: **0.000**



Shear force and Bending moment (x-direction, LRFD)

H_o - Lateral force per length of pile,

$$H_o = \frac{V_x}{1.57\,D}$$

$$H_o = \frac{(-0.491\ \mathrm{kip})}{1.57 \times (48\ \mathrm{in})}$$

$$H_o = -0.078185\ \mathrm{kip/ft}$$

M_o - Moment per length of pile,

$$M_o = \frac{M_z + (V_x\,H)}{1.57\,D}$$

$$M_o = \frac{(15.741\ \mathrm{kipft}) + ((-0.491\ \mathrm{kip}) \times (0\ \mathrm{ft}))}{1.57 \times (48\ \mathrm{in})}$$

$$M_o = 2.5065\ \mathrm{kipft/ft}$$

E - Distance from lateral load to resisting surface,

$$E = \frac{M_o}{H_o}$$

$$E = \frac{(2.5065\ \mathrm{kipft/ft})}{(-0.078185\ \mathrm{kip/ft})}$$

$$E = 32.059\ \mathrm{ft}$$

a - Distance from resting surface to pivot point,

$$a = \frac{(4\,M_o\,L_e) + \left(3\,H_o\,L_e^2\right)}{(6\,M_o) + (4\,H_o\,L_e)}$$

$$a = \frac{(4 \times (2.5065\ \mathrm{kipft/ft}) \times (5\ \mathrm{ft})) + \left(3 \times (-0.078185\ \mathrm{kip/ft}) \times (5\ \mathrm{ft})^2\right)}{\ldots}$$

$$a = \frac{}{(6 \times (2.5065\ \text{kipft/ft})) + (4 \times (-0.078185\ \text{kip/ft}) \times (5\ \text{ft}))}$$

$$a = 3.3726\ \text{ft}$$

V_{max} - Max shear force located at depth a,

$$V_{max} = (H_o\, D) \left[1 - \left[3 \left(\frac{4\,E}{L_e} + 3\right) \left(\frac{a}{L_e}\right)^2\right] + \left[4 \left(\frac{3\,E}{L_e} + 2\right) \left(\frac{a}{L_e}\right)^3\right]\right]$$

$$V_{max} = ((-0.078185\ \text{kip/ft}) \times (48\ \text{in})) \times \left[1 - \left[3 \times \left(\frac{4 \times (32.059\ \text{ft})}{(5\ \text{ft})} + 3\right) \times \left(\frac{(3.3726\ \text{ft})}{(5\ \text{ft})}\right)^2\right] + \left[4 \times \left(\frac{3 \times (32.059\ \text{ft})}{(5\ \text{ft})} + 2\right) \times \left(\frac{(3.3726\ \text{ft})}{(5\ \text{ft})}\right)^3\right]\right]$$

$$V_{max} = 3.7634\ \text{kip}$$

M_{max} - Max bending moment located at depth a/2,

$$M_{max} = (H_o\, D\, L_e) \left[\left(\frac{E}{L_e} + \frac{a}{2\,L_e}\right) - \left[\left(\frac{4\,E}{L_e} + 3\right) \left(\frac{a}{2\,L_e}\right)^3\right] + \left[\left(\frac{3\,E}{L_e} + 2\right) \left(\frac{a}{2\,L_e}\right)^4\right]\right]$$

$$M_{max} = ((-0.078185\ \text{kip/ft}) \times (48\ \text{in}) \times (5\ \text{ft})) \times \left[\left(\frac{(32.059\ \text{ft})}{(5\ \text{ft})} + \frac{(3.3726\ \text{ft})}{2 \times (5\ \text{ft})}\right) - \left[\left(\frac{4 \times (32.059\ \text{ft})}{(5\ \text{ft})} + 3\right) \times \left(\frac{(3.3726\ \text{ft})}{2 \times (5\ \text{ft})}\right)^3\right] + \left[\left(\frac{3 \times (32.059\ \text{ft})}{(5\ \text{ft})} + 2\right) \times \left(\frac{(3.3726\ \text{ft})}{2 \times (5\ \text{ft})}\right)^4\right]\right]$$

$$M_{max} = 9.2647\ \text{kipft}$$

Shear force and Bending moment (z-direction, LRFD)

H_o - Lateral force per length of pile,

$$H_o = \frac{V_z}{1.57\,b}$$

$$H_o = \frac{(-0.017\ \text{kip})}{1.57 \times (48\ \text{in})}$$

$$H_o = -0.002707\ \text{kip/ft}$$

M_o - Moment per length of pile,

$$M_o = \frac{M_x + (V_z\, H)}{1.57\,b}$$

$$M_o = \frac{(0.06\ \text{kipft}) + ((-0.017\ \text{kip}) \times (0\ \text{ft}))}{1.57 \times (48\ \text{in})}$$

$$M_o = 0.0095541\ \text{kipft/ft}$$

E - Distance from lateral load to resisting surface,

$$E = \frac{M_o}{H_o}$$

$$E = \frac{(0.0095541\ \text{kipft/ft})}{(-0.002707\ \text{kip/ft})}$$

$$E = 3.5294\ \text{ft}$$

a - Distance from resting surface to pivot point,

$$a = \frac{(4\,M_o\,L_e) + \left(3\,H_o\,L_e^2\right)}{(6\,M_o) + (4\,H_o\,L_e)}$$

$$a = \frac{(4 \times (0.0095541\ \text{kipft/ft}) \times (5\ \text{ft})) + \left(3 \times (-0.002707\ \text{kip/ft}) \times (5\ \text{ft})^2\right)}{(6 \times (0.0095541\ \text{kipft/ft})) + (4 \times (-0.002707\ \text{kip/ft}) \times (5\ \text{ft}))}$$

$$a = 3.5357\ \text{ft}$$

V_{max} - Max shear force located at depth a,

$$V_{max} = (H_o\, b) \left[1 - \left[3 \left(\frac{4\,E}{L_e} + 3\right) \left(\frac{a}{L_e}\right)^2\right] + \left[4 \left(\frac{3\,E}{L_e} + 2\right) \left(\frac{a}{L_e}\right)^3\right]\right]$$

$$V_{max} = ((-0.002707\ \text{kip/ft}) \times (48\ \text{in})) \times \left[1 - \left[3 \times \left(\frac{4 \times (3.5294\ \text{ft})}{(5\ \text{ft})} + 3\right) \times \left(\frac{(3.5357\ \text{ft})}{(5\ \text{ft})}\right)^2\right] + \left[4 \times \left(\frac{3 \times (3.5294\ \text{ft})}{(5\ \text{ft})} + 2\right) \times \left(\frac{(3.5357\ \text{ft})}{(5\ \text{ft})}\right)^3\right]\right]$$

$$V_{max} = 0.020704\ \text{kip}$$

M_{max} - Max bending moment located at depth a/2,

$$M_{max} = (H_o\, b\, L_e) \left[\left(\frac{E}{L_e} + \frac{a}{2\, L_e}\right) - \left[\left(\frac{4\, E}{L_e} + 3\right) \left(\frac{a}{2\, L_e}\right)^3\right] + \left[\left(\frac{3\, E}{L_e} + 2\right) \left(\frac{a}{2\, L_e}\right)^4\right]\right]$$

$$M_{max} = ((-0.002707\ \text{kip/ft}) \times (48\ \text{in}) \times (5\ \text{ft})) \times \left[\left(\frac{(3.5294\ \text{ft})}{(5\ \text{ft})} + \frac{(3.5357\ \text{ft})}{2 \times (5\ \text{ft})}\right) - \left[\left(\frac{4 \times (3.5294\ \text{ft})}{(5\ \text{ft})} + 3\right) \times \left(\frac{(3.5357\ \text{ft})}{2 \times (5\ \text{ft})}\right)^3\right] + \left[\left(\frac{3 \times (3.5294\ \text{ft})}{(5\ \text{ft})} + 2\right) \times \left(\frac{(3.5357\ \text{ft})}{2 \times (5\ \text{ft})}\right)^4\right]\right]$$

$$M_{max} = 0.046907\ \text{kipft}$$

Minimum Reinforcement Check (LRFD)

Parameters:

$f'_{ck} = 2.5\ \text{ksi}$ - Concrete strength,
$f_{yk} = 60\ \text{ksi}$ - Longitudinal reinforcement strength,
$\phi = 0.65$ - Reduction factor for axial strength,
Table 22.4.2.1 $\alpha = 0.8$ - Alpha factor for axial strength,
$A_g = 2304\ \text{in}^2$ - Gross area of concrete,

Longitudinal reinforcement:

Required reinforcement due to axial load, $A_{st,required}$

22.4.2.2, 10.6.1.1 $A_{st,required}$

$$A_{st,required} = Min\left[\frac{\frac{P}{\phi\, \alpha} - (0.85\, f'_{ck}\, A_g)}{f_{yk} - (0.85\, f'_{ck})}, (0.08\, A_g)\right]$$

$$A_{st,required} = Min\left[\frac{\frac{(8.968\ \text{kip})}{(0.65) \times (0.8)} - (0.85 \times (2.5\ \text{ksi}) \times (2304\ \text{in}^2))}{(60\ \text{ksi}) - (0.85 \times (2.5\ \text{ksi}))}, (0.08 \times (2304\ \text{in}^2))\right]$$

$$A_{st,required} = -84.298\ \text{in}^2$$

A_{min} - Governing minimum reinforcement area,

$$A_{min} = Max\left[A_{st,required}, (0.0018\, A_g)\right]$$

$$A_{min} = Max\left[(-84.298\ \text{in}^2), (0.0018 \times (2304\ \text{in}^2))\right]$$

$$A_{min} = 4.1472\ \text{in}^2$$

n_{rebar} - Required number of reinforcement,

$$n_{rebar} = \frac{A_{min}}{A_{rebar}}$$

$$n_{rebar} = \frac{(4.1472\ \text{in}^2)}{(0.3068\ \text{in}^2)}$$

$$n_{rebar} = 14$$

A_{st} - Actual total reinforcement area,

$$A_{st} = n_{rebar}\, \frac{\pi\, d_{bar}^2}{4}$$

$$A_{st} = (14) \times \frac{\pi \times (0.625\ \text{in})^2}{4}$$

$$A_{st} = 4.2951\ \text{in}^2$$

$Ratio$ - Capacity

$$Ratio = \frac{A_{min}}{A_{st}}$$

$$Ratio = \frac{(4.1472\ \text{in}^2)}{(4.2951\ \text{in}^2)}$$

$$Ratio = 0.96556$$

Status: PASS
Ratio: 0.970

25.2.3 s_{rebar} - Minimum spacing of reinforcement,

$$s_{rebar} = Max\left[1.5, (1.5\ d_{bar})\right]$$

$$s_{rebar} = Max\left[1.5, (1.5 \times (0.625\text{ in}))\right]$$

$$s_{rebar} = 1.5\text{ in}$$

Ties:

25.7.2.2 Since longitudinal reinforcement is $\leq$ No. 10ø: Use #3(0.375 in)

25.7.2.1 s_{ties} - Maximum spacing of ties,

$$s_{ties} = Min\left[(16\ d_{bar}), (48\ d_{ties}), Min(D, b)\right]$$

$$s_{ties} = Min\left[(16 \times (0.625\text{ in})), (48 \times (0.375\text{ in})), Min((48\text{ in}), (48\text{ in}))\right]$$

$$s_{ties} = 10\text{ in}$$

Summary:

Main reinforcement: **14 - #5 (0.625 in)**
Ties: **#3(0.375 in) - 10 in**

Axial Compression Strength (ACI 318-19, LRFD)

22.4.2.2 ϕP_N - Allowable axial compressive strength

$$\phi P_N = \phi\ 0.80\ \left[\left(0.85\ f'_{ck}\ \left[A_g - A_{st}\right]\right) + \left(f_{yk}\ A_{st}\right)\right]$$

$$\phi P_N = (0.65) \times 0.80 \times \left[\left(0.85 \times (2.5\text{ ksi}) \times \left[\left(2304\text{ in}^2\right) - \left(4.2951\text{ in}^2\right)\right]\right) + \left((60\text{ ksi}) \times \left(4.2951\text{ in}^2\right)\right)\right]$$

$$\phi P_N = 2675.2\text{ kip}$$

$Ratio$ - Capacity

$$Ratio = \frac{P}{\phi P_N}$$

$$Ratio = \frac{(8.968\text{ kip})}{(2675.2\text{ kip})}$$

$$Ratio = 0.0033523$$

Status: PASS
Ratio: 0.000

Shear Strength (ACI 318-19, LRFD)

Parameters:

$b_w = 48\text{ in}$ - Effective width,

22.5.2.2 d - Effective depth

$$d = 0.80\ D$$

$$d = 0.80 \times (48\text{ in})$$

$$d = 38.4\text{ in}$$

22.5.5.1.3 λ_s - size effect modification factor

$$\lambda_s = MIN\left[\sqrt{\frac{2}{1 + \frac{d}{10}}}, 1\right]$$

$$\lambda_s = MIN\left[\sqrt{\frac{2}{1 + \frac{(38.4\text{ in})}{10}}}, 1\right]$$

$$\lambda_s = 0.64282$$

The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5\text{ ksi} \rightarrow 2500\text{ psi}$,

22.5.5.1.1 $V_{c,max}$ - Max shear strength of concrete

$$V_{c,max} = 5\ \lambda_s\ \sqrt{f'_{ck}}\ b_w\ d$$

$$V_{c,max} = 5 \times (0.64282) \times \sqrt{(2500\text{ psi})} \times (48\text{ in}) \times (38.4\text{ in})$$

$$V_{c,max} = 296.21 \text{ kip}$$

The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5 \text{ ksi} \rightarrow 2500 \text{ psi}$, $P = 8.968 \text{ kip} \rightarrow 8968 \text{ lbf}$,

22.5.5.1.1(a) $V_{c,a}$ - Shear strength of concrete (a)

$$V_{c,a} = \left[2\,\lambda_s\,\sqrt{f'_{ck}} + \frac{P}{6\,A_g}\right]\,b_w\,d$$

$$V_{c,a} = \left[2 \times (0.64282) \times \sqrt{(2500 \text{ psi})} + \frac{(8968 \text{ lbf})}{6 \times (2304 \text{ in}^2)}\right] \times (48 \text{ in}) \times (38.4 \text{ in})$$

$$V_{c,a} = 119.68 \text{ kip}$$

The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5 \text{ ksi} \rightarrow 2500 \text{ psi}$,

22.5.5.1.2 $V_{c,b}$ - Shear strength of concrete (b)

$$V_{c,b} = \left[2\,\lambda_s\,\sqrt{f'_{ck}} + \left(0.05\,f'_{ck}\right)\right]\,b_w\,d$$

$$V_{c,b} = \left[2 \times (0.64282) \times \sqrt{(2500 \text{ psi})} + (0.05 \times (2500 \text{ psi}))\right] \times (48 \text{ in}) \times (38.4 \text{ in})$$

$$V_{c,b} = 348.89 \text{ kip}$$

V_c - Governing shear strength of concrete

$$V_c = Min\left[V_{c,max}, V_{c,a}, V_{c,b}\right]$$

$$V_c = Min\left[(296.21 \text{ kip}), (119.68 \text{ kip}), (348.89 \text{ kip})\right]$$

$$V_c = 119.68 \text{ kip}$$

The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5 \text{ ksi} \rightarrow 2500 \text{ psi}$,

22.5.1.2 $V_{s,a}$ - Shear strength of steel (a)

$$V_{s,a} = 8\,\sqrt{f'_{ck}}\,b_w\,d$$

$$V_{s,a} = 8 \times \sqrt{(2500 \text{ psi})} \times (48 \text{ in}) \times (38.4 \text{ in})$$

$$V_{s,a} = 737.28 \text{ kip}$$

A_v - Ties rebar area,

$$A_v = \frac{\pi\,d_{ties}^2}{4}$$

$$A_v = \frac{\pi \times (0.375 \text{ in})^2}{4}$$

$$A_v = 0.11045 \text{ in}^2$$

22.5.8.5.3 $V_{s,b}$ - Shear strength of steel (b)

$$V_{s,b} = \frac{2\,A_v\,f_{ywk}\,d}{s_{ties}}$$

$$V_{s,b} = \frac{2 \times \left(0.11045 \text{ in}^2\right) \times (60 \text{ ksi}) \times (38.4 \text{ in})}{(10 \text{ in})}$$

$$V_{s,b} = 50.894 \text{ kip}$$

V_s - Governing shear strength of steel

$$V_s = MIN\left[V_{s,a}, V_{s,b}\right]$$

$$V_s = MIN\left[(737.28 \text{ kip}), (50.894 \text{ kip})\right]$$

$$V_s = 50.894 \text{ kip}$$

22.5.1.1 ϕV_n - Allowable shear strength

$$\phi V_n = \phi\,\left(V_c + V_s\right)$$

$$\phi V_n = (0.65) \times ((119.68 \text{ kip}) + (50.894 \text{ kip}))$$

$$\phi V_n = 110.87 \text{ kip}$$

Considering x-direction:

$V_{max} = 3.7634 \text{ kip}$ - Maximum shear force in the x-direction,
$Ratio$ - Capacity

$$Ratio = \frac{V_{max}}{\phi V_n}$$

	$$Ratio = \frac{(3.7634\ \text{kip})}{(110.87\ \text{kip})}$$ $$Ratio = 0.033943$$	Status: **PASS** Ratio: **0.030**
	Considering z-direction: $V_{max} = 0.020704\ \text{kip}$ - Maximum shear force in the z-direction, $Ratio$ - Capacity $$Ratio = \frac{V_{max}}{\phi V_n}$$ $$Ratio = \frac{(0.020704\ \text{kip})}{(110.87\ \text{kip})}$$ $$Ratio = 0.00018673$$	Status: **PASS** Ratio: **0.000**
14.5.2.1b	**Flexural Strength (ACI 318-19, LRFD)** S_m - Section modulus $$S_m = \frac{b\,D^2}{6}$$ $$S_m = \frac{(48\ \text{in}) \times (48\ \text{in})^2}{6}$$ $$S_m = 18432\ \text{in}^3$$ $\lambda = 1$ - Concrete modification factor (Normal concrete), Allowable flexural strength: M_n shall be the lesser of: $\phi M_{n,1}$ $$\phi M_{n,1} = \phi \times 5 \times \lambda \times \sqrt{(f'_c)} \times S_m$$ $$\phi M_{n,1} = 0.65 \times 5 \times 1 \times \sqrt{(2.5ksi)} \times 18432.001in^3$$ $$\phi M_{n,1} = 249.600kipft$$ $\phi M_{n,2}$ $$\phi M_{n,2} = \phi\ 0.85\ f'_{ck}\ S_m$$ $$\phi M_{n,2} = (0.65) \times 0.85 \times (2.5\ \text{ksi}) \times \left(18432\ \text{in}^3\right)$$ $$\phi M_{n,2} = 2121.6\ \text{kipft}$$ Therefore, ϕM_n - Allowable flexural strength, $$\phi M_n = MIN[\phi M_{n,1}, \phi M_{n,2}]$$ $$\phi M_n = MIN[(249.6\ \text{kipft}), (2121.6\ \text{kipft})]$$ $$\phi M_n = 249.6\ \text{kipft}$$ **Considering x-direction:** $M_{max} = 9.2647\ \text{kipft}$ - Maximum moment in the x-direction, $Ratio$ - Capacity $$Ratio = \frac{M_{max}}{\phi M_n}$$ $$Ratio = \frac{(9.2647\ \text{kipft})}{(249.6\ \text{kipft})}$$ $$Ratio = 0.037118$$	Status: **PASS** Ratio: **0.040**
	Considering z-direction: $M_{max} = 0.046907\ \text{kipft}$ - Maximum moment in the z-direction, $Ratio$ - Capacity $$Ratio = \frac{M_{max}}{\phi M_n}$$	

	$$Ratio = \frac{(0.046907 \text{ kipft})}{(249.6 \text{ kipft})}$$ $$Ratio = 0.00018793$$	Status: **PASS** Ratio: **0.000**

REFERENCES	CALCULATIONS	RESULTS

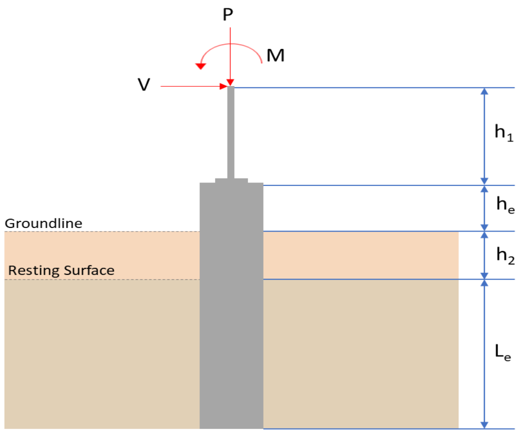
SkyCiv Foundation Design

Pile Foundation

Design Information :

Design code : IBC 2021 (International Building Code)
Unit System : Imperial

Pile Input



Geometry

Pile shape: rectangular

$b = 48$ in - Pile width

$D = 48$ in - Pile depth

$L = 5$ ft - Total pile length

$h_1 = 0$ ft - Lateral load height from the top of the pile,

$h_2 = 0$ ft - Depth to resisting surface

$h_e = 0$ ft - Length of pile above the ground

Tabulation of Soil Parameters

Layer	Label	Allowable Bearing Pressure (q_a) (psf)	Allowable Lateral Pressure (R) (psf/ft)
1	Sand, silty sand, clayey sand, silty gravel & clayey gravel	2000.000	150.000

Tabulation of Loads

Load Component	ASD	LRFD
P (kip)	5.624	8.832
V_x (kip)	-0.293	-0.489
V_z (kip)	0.000	0.000
M_x (kipft)	0.000	0.000
M_z (kipft)	9.330	16.021

Material Properties

$f'_{ck} = 2.5$ ksi - Concrete strength,

Required depth to resist lateral loads (ASD)

H - Point of application of the lateral load

$$H = h_1 + h_2 + h_e$$

$$H = (0\text{ ft}) + (0\text{ ft}) + (0\text{ ft})$$

$$H = 0\text{ ft}$$

Considering x-direction:

H_o - Lateral force per length of pile,

$$H_o = \frac{V_x}{1.57\,D}$$

$$H_o = \frac{(-0.293\text{ kip})}{1.57 \times (48\text{ in})}$$

$$H_o = -0.046656\text{ kip/ft}$$

M_o - Moment per length of pile,

$$M_o = \frac{M_z + (V_x\, H)}{1.57\, D}$$

$$M_o = \frac{(9.33 \text{ kipft}) + ((-0.293 \text{ kip}) \times (0 \text{ ft}))}{1.57 \times (48 \text{ in})}$$

$$M_o = 1.4857 \text{ kipft/ft}$$

Required depth of embedment in earth:

$$L_x^3 - \left(14.14 \times \frac{H_o \times L_x}{R}\right) - \left(18.85 \times \frac{M_o}{R}\right) = 0$$

Solving the cubic equation:
$L_{e,x} = 4.727 \text{ ft}$ - Required depth in x-direction,

Considering z-direction:

$L_{e,z} = 0 \text{ ft}$ - Required depth in z-direction,

Minimum embedded depth required:

$L_{e,req}$ - Depth of pile required,

$$L_{e,req} = MAX[L_{e,x}, L_{e,z}]$$

$$L_{e,req} = MAX[(4.727 \text{ ft}), (0 \text{ ft})]$$

$$L_{e,req} = 4.727 \text{ ft}$$

L_e - Actual embedded length of pile,

$$L_e = L - h_e - h_2$$

$$L_e = (5 \text{ ft}) - (0 \text{ ft}) - (0 \text{ ft})$$

$$L_e = 5 \text{ ft}$$

$Ratio$ - Embedded depth

$$Ratio = \frac{L_{e,req}}{L_e}$$

$$Ratio = \frac{(4.727 \text{ ft})}{(5 \text{ ft})}$$

$$Ratio = 0.9454$$

Status: **PASS**
Ratio: **0.950**

End-bearing Capacity (ASD)

A - Pile cross-section area

$$A = b\, D$$

$$A = (48 \text{ in}) \times (48 \text{ in})$$

$$A = 16 \text{ ft}^2$$

q - End-bearing pressure

$$q = \frac{P_v}{A}$$

$$q = \frac{(5.624 \text{ kip})}{(16 \text{ ft}^2)}$$

$$q = 0.3515 \text{ kip/ft}^2$$

Check bearing capacity ratio:

$Ratio$ - Capacity

$$Ratio = \frac{q}{q_a}$$

$$Ratio = \frac{(0.3515 \text{ kip/ft}^2)}{(2000 \text{ psf})}$$

$$Ratio = 0.17575$$

Status: **PASS**
Ratio: **0.180**

Czerniak

Lateral Soil Pressure (ASD):

L/D - Length to least lateral dimension ratio,

$$L/D = \frac{L}{D}$$

$$L/D = \frac{(5\ \mathrm{ft})}{(48\ \mathrm{in})}$$

$$L/D = 1.25$$

Since L/D $\leq$ 10,

Pile is short.

Considering x-direction:

$H_o = -0.046656\ \mathrm{kip/ft}$ - Lateral force per length of pile,
$M_o = 1.4857\ \mathrm{kipft/ft}$ - Overturning moment per length of pile,
a - Distance from resting surface to pivot point,

$$a = \frac{(4\, M_o\, L_e) + \left(3\, H_o\, L_e^2\right)}{(6\, M_o) + (4\, H_o\, L_e)}$$

$$a = \frac{(4 \times (1.4857\ \mathrm{kipft/ft}) \times (5\ \mathrm{ft})) + \left(3 \times (-0.046656\ \mathrm{kip/ft}) \times (5\ \mathrm{ft})^2\right)}{(6 \times (1.4857\ \mathrm{kipft/ft})) + (4 \times (-0.046656\ \mathrm{kip/ft}) \times (5\ \mathrm{ft}))}$$

$$a = 3.3728\ \mathrm{ft}$$

p - Earth pressure against the pile at distance a/2 from resting surface,

$$p = \frac{0.75\ [(4\, M_o) + (3\, H_o\, L_e)]^2}{L_e^2\ [(3\, M_o) + (2\, H_o\, L_e)]}$$

$$p = \frac{0.75 \times [(4 \times (1.4857\ \mathrm{kipft/ft})) + (3 \times (-0.046656\ \mathrm{kip/ft}) \times (5\ \mathrm{ft}))]^{\ 2}}{(5\ \mathrm{ft})^2 \times [(3 \times (1.4857\ \mathrm{kipft/ft})) + (2 \times (-0.046656\ \mathrm{kip/ft}) \times (5\ \mathrm{ft}))]}$$

$$p = 0.20665\ \mathrm{kip/ft^2}$$

s - Earth pressure against the pile at distance L_e,

$$s = \frac{6\ [(2\, M_o) + (H_o\, L_e)]}{L_e^2}$$

$$s = \frac{6 \times [(2 \times (1.4857\ \mathrm{kipft/ft})) + ((-0.046656\ \mathrm{kip/ft}) \times (5\ \mathrm{ft}))]}{(5\ \mathrm{ft})^2}$$

$$s = 0.65713\ \mathrm{kip/ft^2}$$

Check lateral soil pressure capacity:

p_a - Allowable lateral soil pressure at depth a/2,

$$p_a = R\, \frac{a}{2}$$

$$p_a = (150\ \mathrm{psf/ft}) \times \frac{(3.3728\ \mathrm{ft})}{2}$$

$$p_a = 0.25296\ \mathrm{kip/ft^2}$$

$Ratio$ - Lateral soil capacity

$$Ratio = \frac{p}{p_a}$$

$$Ratio = \frac{\left(0.20665\ \mathrm{kip/ft^2}\right)}{\left(0.25296\ \mathrm{kip/ft^2}\right)}$$

$$Ratio = 0.81692$$

Status: **PASS**
Ratio: **0.820**

p_s - Allowable lateral soil pressure at depth L_e,

$$p_s = R\, L_e$$

$$p_s = (150\ \mathrm{psf/ft}) \times (5\ \mathrm{ft})$$

$$p_s = 0.75\ \mathrm{kip/ft^2}$$

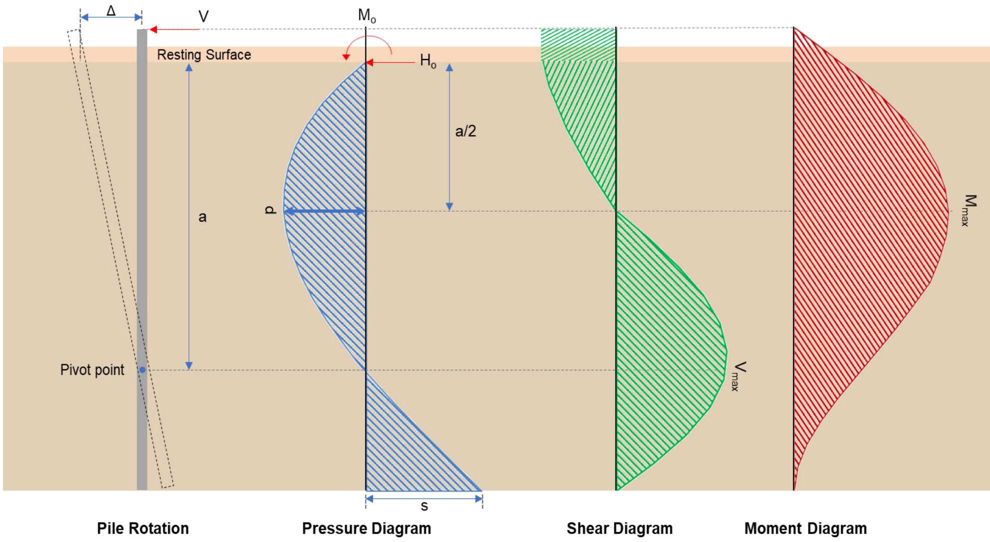
$Ratio$ - Lateral soil capacity

$$Ratio = \frac{s}{p_s}$$

$$Ratio = \frac{\left(0.65713\ \mathrm{kip/ft^2}\right)}{\left(0.75\ \mathrm{kip/ft^2}\right)}$$

$$Ratio = 0.87618$$

Status: **PASS**
Ratio: **0.880**



Shear force and Bending moment (x-direction, LRFD)

H_o - Lateral force per length of pile,

$$H_o = \frac{V_x}{1.57\,D}$$

$$H_o = \frac{(-0.489\ \mathrm{kip})}{1.57 \times (48\ \mathrm{in})}$$

$$H_o = -0.077866\ \mathrm{kip/ft}$$

M_o - Moment per length of pile,

$$M_o = \frac{M_z + (V_x\,H)}{1.57\,D}$$

$$M_o = \frac{(16.021\ \mathrm{kipft}) + ((-0.489\ \mathrm{kip}) \times (0\ \mathrm{ft}))}{1.57 \times (48\ \mathrm{in})}$$

$$M_o = 2.5511\ \mathrm{kipft/ft}$$

E - Distance from lateral load to resisting surface,

$$E = \frac{M_o}{H_o}$$

$$E = \frac{(2.5511\ \mathrm{kipft/ft})}{(-0.077866\ \mathrm{kip/ft})}$$

$$E = 32.763\ \mathrm{ft}$$

a - Distance from resting surface to pivot point,

$$a = \frac{(4\,M_o\,L_e) + \left(3\,H_o\,L_e^2\right)}{(6\,M_o) + (4\,H_o\,L_e)}$$

$$a = \frac{(4 \times (2.5511\ \mathrm{kipft/ft}) \times (5\ \mathrm{ft})) + \left(3 \times (-0.077866\ \mathrm{kip/ft}) \times (5\ \mathrm{ft})^2\right)}{(6 \times (2.5511\ \mathrm{kipft/ft})) + (4 \times (-0.077866\ \mathrm{kip/ft}) \times (5\ \mathrm{ft}))}$$

$$a = 3.3718\ \mathrm{ft}$$

V_{max} - Max shear force located at depth a,

$$V_{max} = (H_o\,D)\left[1 - \left[3\left(\frac{4\,E}{L_e} + 3\right)\left(\frac{a}{L_e}\right)^2\right] + \left[4\left(\frac{3\,E}{L_e} + 2\right)\left(\frac{a}{L_e}\right)^3\right]\right]$$

$$V_{max} = ((-0.077866\ \mathrm{kip/ft}) \times (48\ \mathrm{in})) \times \left[1 - \left[3 \times \left(\frac{4 \times (32.763\ \mathrm{ft})}{(5\ \mathrm{ft})} + 3\right) \times \left(\frac{(3.3718\ \mathrm{ft})}{(5\ \mathrm{ft})}\right)^2\right] + \left[4 \times \left(\frac{3 \times (32.763\ \mathrm{ft})}{(5\ \mathrm{ft})} + 2\right) \times \left(\frac{(3.3718\ \mathrm{ft})}{(5\ \mathrm{ft})}\right)^3\right]\right]$$

$$V_{max} = 2.826\ \mathrm{kip}$$

$$V_{max} = 3.826 \text{ kip}$$

M_{max} - Max bending moment located at depth a/2,

$$M_{max} = (H_o\, D\, L_e)\left[\left(\frac{E}{L_e} + \frac{a}{2\, L_e}\right) - \left[\left(\frac{4\, E}{L_e} + 3\right)\left(\frac{a}{2\, L_e}\right)^3\right] + \left[\left(\frac{3\, E}{L_e} + 2\right)\left(\frac{a}{2\, L_e}\right)^4\right]\right]$$

$$M_{max} = ((-0.077866 \text{ kip/ft}) \times (48 \text{ in}) \times (5 \text{ ft})) \times \left[\left(\frac{(32.763 \text{ ft})}{(5 \text{ ft})} + \frac{(3.3718 \text{ ft})}{2 \times (5 \text{ ft})}\right) - \left[\left(\frac{4 \times (32.763 \text{ ft})}{(5 \text{ ft})} + 3\right) \times \left(\frac{(3.3718 \text{ ft})}{2 \times (5 \text{ ft})}\right)^3\right] + \left[\left(\frac{3 \times (32.763 \text{ ft})}{(5 \text{ ft})} + 2\right) \times \left(\frac{(3.3718 \text{ ft})}{2 \times (5 \text{ ft})}\right)^4\right]\right]$$

$$M_{max} = 9.4217 \text{ kipft}$$

Minimum Reinforcement Check (LRFD)

Parameters:

$f'_{ck} = 2.5 \text{ ksi}$ - Concrete strength,
$f_{yk} = 60 \text{ ksi}$ - Longitudinal reinforcement strength,
$\phi = 0.65$ - Reduction factor for axial strength,
Table 22.4.2.1 $\alpha = 0.8$ - Alpha factor for axial strength,
$A_g = 2304 \text{ in}^2$ - Gross area of concrete,

Longitudinal reinforcement:

Required reinforcement due to axial load, $A_{st,required}$
22.4.2.2, 10.6.1.1 $A_{st,required}$

$$A_{st,required} = Min\left[\frac{\frac{P}{\phi\,\alpha} - (0.85\, f'_{ck}\, A_g)}{f_{yk} - (0.85\, f'_{ck})}, (0.08\, A_g)\right]$$

$$A_{st,required} = Min\left[\frac{\frac{(8.832 \text{ kip})}{(0.65)\times(0.8)} - (0.85 \times (2.5 \text{ ksi}) \times (2304 \text{ in}^2))}{(60 \text{ ksi}) - (0.85 \times (2.5 \text{ ksi}))}, (0.08 \times (2304 \text{ in}^2))\right]$$

$$A_{st,required} = -84.303 \text{ in}^2$$

A_{min} - Governing minimum reinforcement area,

$$A_{min} = Max[A_{st,required}, (0.0018\, A_g)]$$

$$A_{min} = Max[(-84.303 \text{ in}^2), (0.0018 \times (2304 \text{ in}^2))]$$

$$A_{min} = 4.1472 \text{ in}^2$$

n_{rebar} - Required number of reinforcement,

$$n_{rebar} = \frac{A_{min}}{A_{rebar}}$$

$$n_{rebar} = \frac{(4.1472 \text{ in}^2)}{(0.3068 \text{ in}^2)}$$

$$n_{rebar} = 14$$

A_{st} - Actual total reinforcement area,

$$A_{st} = n_{rebar}\,\frac{\pi\, d_{bar}^2}{4}$$

$$A_{st} = (14) \times \frac{\pi \times (0.625 \text{ in})^2}{4}$$

$$A_{st} = 4.2951 \text{ in}^2$$

$Ratio$ - Capacity

$$Ratio = \frac{A_{min}}{A_{st}}$$

$$Ratio = \frac{(4.1472 \text{ in}^2)}{(4.2951 \text{ in}^2)}$$

$$Ratio = 0.96556$$

Status: **PASS**
Ratio: **0.970**

25.2.3 s_{rebar} - Minimum spacing of reinforcement,

$$s_{rebar} = Max[1.5, (1.5\, d_{bar})]$$

$$s_{rebar} = Max\left[1.5, (1.5 \times (0.625\ \text{in}))\right]$$

$$s_{rebar} = 1.5\ \text{in}$$

Ties:

25.7.2.2 Since longitudinal reinforcement is $\leq$ No. 10ø: Use #3(0.375 in)

25.7.2.1 s_{ties} - Maximum spacing of ties,

$$s_{ties} = Min\left[(16\, d_{bar}), (48\, d_{ties}), Min\,(D, b)\right]$$

$$s_{ties} = Min\left[(16 \times (0.625\ \text{in})), (48 \times (0.375\ \text{in})), Min\left((48\ \text{in}), (48\ \text{in})\right)\right]$$

$$s_{ties} = 10\ \text{in}$$

Summary:

Main reinforcement: **14 - #5 (0.625 in)**
Ties: **#3(0.375 in) - 10 in**

Axial Compression Strength (ACI 318-19, LRFD)

22.4.2.2 ϕP_N - Allowable axial compressive strength

$$\phi P_N = \phi\, 0.80\ \left[\left(0.85\, f'_{ck}\ [A_g - A_{st}]\right) + (f_{yk}\, A_{st})\right]$$

$$\phi P_N = (0.65) \times 0.80 \times \left[\left(0.85 \times (2.5\ \text{ksi}) \times \left[\left(2304\ \text{in}^2\right) - \left(4.2951\ \text{in}^2\right)\right]\right) + \left((60\ \text{ksi}) \times \left(4.2951\ \text{in}^2\right)\right)\right]$$

$$\phi P_N = 2675.2\ \text{kip}$$

$Ratio$ - Capacity

$$Ratio = \frac{P}{\phi P_N}$$

$$Ratio = \frac{(8.832\ \text{kip})}{(2675.2\ \text{kip})}$$

$$Ratio = 0.0033015$$

Status: **PASS**
Ratio: **0.000**

Shear Strength (ACI 318-19, LRFD)

Parameters:

$b_w = 48\ \text{in}$ - Effective width,

22.5.2.2 d - Effective depth

$$d = 0.80\ D$$

$$d = 0.80 \times (48\ \text{in})$$

$$d = 38.4\ \text{in}$$

22.5.5.1.3 λ_s - size effect modification factor

$$\lambda_s = MIN\left[\sqrt{\frac{2}{1 + \frac{d}{10}}}, 1\right]$$

$$\lambda_s = MIN\left[\sqrt{\frac{2}{1 + \frac{(38.4\ \text{in})}{10}}}, 1\right]$$

$$\lambda_s = 0.64282$$

The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5\ \text{ksi} \rightarrow 2500\ \text{psi}$,

22.5.5.1.1 $V_{c,max}$ - Max shear strength of concrete

$$V_{c,max} = 5\, \lambda_s\, \sqrt{f'_{ck}}\, b_w\, d$$

$$V_{c,max} = 5 \times (0.64282) \times \sqrt{(2500\ \text{psi})} \times (48\ \text{in}) \times (38.4\ \text{in})$$

$$V_{c,max} = 296.21\ \text{kip}$$

The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5\ \text{ksi} \rightarrow 2500\ \text{psi}$, $P = 8.832\ \text{kip} \rightarrow 8832\ \text{lbf}$,

22.5.5.1.1(a) $V_{c,a}$ - Shear strength of concrete (a)

$$V_{c,a} = \left[2\, \lambda_s\, \sqrt{f'_{ck}} + \frac{P}{6\, A_g}\right]\ b_w\, d$$

$$V_{c,a} = \left[2 \times (0.64282) \times \sqrt{(2500\ \text{psi})} + \frac{(8832\ \text{lbf})}{6 \times (2304\ \text{in}^2)}\right] \times (48\ \text{in}) \times (38.4\ \text{in})$$

$$V_{c,a} = 119.66\ \text{kip}$$

The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5\ \text{ksi} \rightarrow 2500\ \text{psi}$,

22.5.5.1.2 $V_{c,b}$ - Shear strength of concrete (b)

$$V_{c,b} = \left[2\ \lambda_s\ \sqrt{f'_{ck}} + \left(0.05\ f'_{ck}\right)\right]\ b_w\ d$$

$$V_{c,b} = \left[2 \times (0.64282) \times \sqrt{(2500\ \text{psi})} + (0.05 \times (2500\ \text{psi}))\right] \times (48\ \text{in}) \times (38.4\ \text{in})$$

$$V_{c,b} = 348.89\ \text{kip}$$

V_c - Governing shear strength of concrete

$$V_c = Min\left[V_{c,max}, V_{c,a}, V_{c,b}\right]$$

$$V_c = Min\left[(296.21\ \text{kip}), (119.66\ \text{kip}), (348.89\ \text{kip})\right]$$

$$V_c = 119.66\ \text{kip}$$

The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5\ \text{ksi} \rightarrow 2500\ \text{psi}$,

22.5.1.2 $V_{s,a}$ - Shear strength of steel (a)

$$V_{s,a} = 8\ \sqrt{f'_{ck}}\ b_w\ d$$

$$V_{s,a} = 8 \times \sqrt{(2500\ \text{psi})} \times (48\ \text{in}) \times (38.4\ \text{in})$$

$$V_{s,a} = 737.28\ \text{kip}$$

A_v - Ties rebar area,

$$A_v = \frac{\pi\ d_{ties}^2}{4}$$

$$A_v = \frac{\pi \times (0.375\ \text{in})^2}{4}$$

$$A_v = 0.11045\ \text{in}^2$$

22.5.8.5.3 $V_{s,b}$ - Shear strength of steel (b)

$$V_{s,b} = \frac{2\ A_v\ f_{ywk}\ d}{s_{ties}}$$

$$V_{s,b} = \frac{2 \times \left(0.11045\ \text{in}^2\right) \times (60\ \text{ksi}) \times (38.4\ \text{in})}{(10\ \text{in})}$$

$$V_{s,b} = 50.894\ \text{kip}$$

V_s - Governing shear strength of steel

$$V_s = MIN\left[V_{s,a}, V_{s,b}\right]$$

$$V_s = MIN\left[(737.28\ \text{kip}), (50.894\ \text{kip})\right]$$

$$V_s = 50.894\ \text{kip}$$

22.5.1.1 ϕV_n - Allowable shear strength

$$\phi V_n = \phi\ (V_c + V_s)$$

$$\phi V_n = (0.65) \times ((119.66\ \text{kip}) + (50.894\ \text{kip}))$$

$$\phi V_n = 110.86\ \text{kip}$$

Considering x-direction:

$V_{max} = 3.826\ \text{kip}$ - Maximum shear force in the x-direction,
$Ratio$ - Capacity

$$Ratio = \frac{V_{max}}{\phi V_n}$$

$$Ratio = \frac{(3.826\ \text{kip})}{(110.86\ \text{kip})}$$

$$Ratio = 0.034511$$

Status: **PASS**
Ratio: **0.030**

Flexural Strength (ACI 318-19, LRFD)

S_m - Section modulus

$$S_m = \frac{b\,D^2}{6}$$

$$S_m = \frac{(48\ \text{in}) \times (48\ \text{in})^2}{6}$$

$$S_m = 18432\ \text{in}^3$$

$\lambda = 1$ - Concrete modification factor (Normal concrete),
Allowable flexural strength:
M_n shall be the lesser of:
$\phi M_{n,1}$

$$\phi M_{n,1} = \phi \times 5 \times \lambda \times \sqrt{(f_c')} \times S_m$$

$$\phi M_{n,1} = 0.65 \times 5 \times 1 \times \sqrt{(2.5ksi)} \times 18432.001 in^3$$

$$\phi M_{n,1} = 249.600 kipft$$

14.5.2.1b $\phi M_{n,2}$

$$\phi M_{n,2} = \phi\ 0.85\ f_{ck}'\ S_m$$

$$\phi M_{n,2} = (0.65) \times 0.85 \times (2.5\ \text{ksi}) \times \left(18432\ \text{in}^3\right)$$

$$\phi M_{n,2} = 2121.6\ \text{kipft}$$

Therefore,
ϕM_n - Allowable flexural strength,

$$\phi M_n = MIN[\phi M_{n,1}, \phi M_{n,2}]$$

$$\phi M_n = MIN[(249.6\ \text{kipft}), (2121.6\ \text{kipft})]$$

$$\phi M_n = 249.6\ \text{kipft}$$

Considering x-direction:

$M_{max} = 9.4217\ \text{kipft}$ - Maximum moment in the x-direction,
$Ratio$ - Capacity

$$Ratio = \frac{M_{max}}{\phi M_n}$$

$$Ratio = \frac{(9.4217\ \text{kipft})}{(249.6\ \text{kipft})}$$

$$Ratio = 0.037747$$

Status: **PASS**
Ratio: **0.040**

REFERENCES	CALCULATIONS	RESULTS

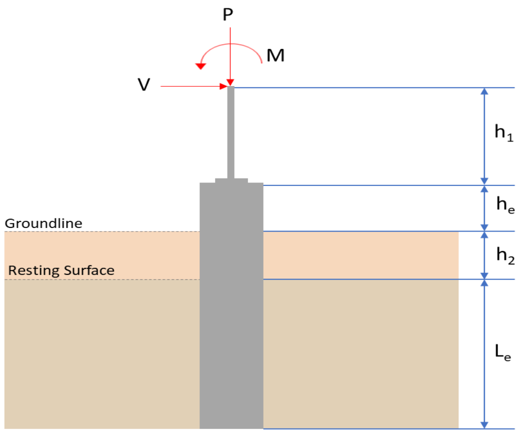
SkyCiv Foundation Design

Pile Foundation

Design Information :

Design code : IBC 2021 (International Building Code)
Unit System : Imperial

Pile Input



Geometry

Pile shape: rectangular
$b = 48$ in - Pile width
$D = 48$ in - Pile depth
$L = 5$ ft - Total pile length
$h_1 = 0$ ft - Lateral load height from the top of the pile,
$h_2 = 0$ ft - Depth to resisting surface
$h_e = 0$ ft - Length of pile above the ground

Tabulation of Soil Parameters

Layer	Label	Allowable Bearing Pressure (q_a) (psf)	Allowable Lateral Pressure (R) (psf/ft)
1	Sand, silty sand, clayey sand, silty gravel & clayey gravel	2000.000	150.000

Tabulation of Loads

Load Component	ASD	LRFD
P (kip)	5.709	8.968
V_x (kip)	-0.295	-0.491
V_z (kip)	0.011	0.017
M_x (kipft)	0.038	0.060
M_z (kipft)	9.173	15.741

Material Properties

$f'_{ck} = 2.5$ ksi - Concrete strength,

Required depth to resist lateral loads (ASD)

H - Point of application of the lateral load

$$H = h_1 + h_2 + h_e$$

$$H = (0 \text{ ft}) + (0 \text{ ft}) + (0 \text{ ft})$$

$$H = 0 \text{ ft}$$

Considering x-direction:

H_o - Lateral force per length of pile,

$$H_o = \frac{V_x}{1.57\ D}$$

$$H_o = \frac{(-0.295 \text{ kip})}{1.57 \times (48 \text{ in})}$$

$$H_o = -0.046975 \text{ kip/ft}$$

M_o - Moment per length of pile,

$$M_o = \frac{M_z + (V_x\, H)}{1.57\, D}$$

$$M_o = \frac{(9.173\ \text{kipft}) + ((-0.295\ \text{kip}) \times (0\ \text{ft}))}{1.57 \times (48\ \text{in})}$$

$$M_o = 1.4607\ \text{kipft/ft}$$

Required depth of embedment in earth:

$$L_x^3 - \left(14.14 \times \frac{H_o \times L_x}{R}\right) - \left(18.85 \times \frac{M_o}{R}\right) = 0$$

Solving the cubic equation:
$L_{e,x} = 4.6969\ \text{ft}$ - Required depth in x-direction,

Considering z-direction:

H_o - Lateral force per length of pile,

$$H_o = \frac{V_z}{1.57\, b}$$

$$H_o = \frac{(0.011\ \text{kip})}{1.57 \times (48\ \text{in})}$$

$$H_o = 0.0017516\ \text{kip/ft}$$

M_o - Moment per length of pile,

$$M_o = \frac{M_x + (V_z\, H)}{1.57\, b}$$

$$M_o = \frac{(0.038\ \text{kipft}) + ((0.011\ \text{kip}) \times (0\ \text{ft}))}{1.57 \times (48\ \text{in})}$$

$$M_o = 0.006051\ \text{kipft/ft}$$

Required depth of embedment in earth:

$$L_z^3 - \left(14.14 \times \frac{H_o \times L_z}{R}\right) - \left(18.85 \times \frac{M_o}{R}\right) = 0$$

Solving the cubic equation:
$L_{e,z} = 0.82968\ \text{ft}$ - Required depth in z-direction,

Minimum embedded depth required:

$L_{e,req}$ - Depth of pile required,

$$L_{e,req} = MAX[L_{e,x}, L_{e,z}]$$

$$L_{e,req} = MAX[(4.6969\ \text{ft}), (0.82968\ \text{ft})]$$

$$L_{e,req} = 4.697\ \text{ft}$$

L_e - Actual embedded length of pile,

$$L_e = L - h_e - h_2$$

$$L_e = (5\ \text{ft}) - (0\ \text{ft}) - (0\ \text{ft})$$

$$L_e = 5\ \text{ft}$$

$Ratio$ - Embedded depth

$$Ratio = \frac{L_{e,req}}{L_e}$$

$$Ratio = \frac{(4.697\ \text{ft})}{(5\ \text{ft})}$$

$$Ratio = 0.9394$$

Status: **PASS**
Ratio: **0.940**

End-bearing Capacity (ASD)

A - Pile cross-section area

$$A = b\, D$$

$$A = (48\ \text{in}) \times (48\ \text{in})$$

$$A = 16\ \text{ft}^2$$

q - End-bearing pressure

$$q = \frac{P_v}{A}$$

$$q = \frac{(5.709 \text{ kip})}{(16 \text{ ft}^2)}$$

$$q = 0.35681 \text{ kip/ft}^2$$

Check bearing capacity ratio:

$Ratio$ - Capacity

$$Ratio = \frac{q}{q_a}$$

$$Ratio = \frac{\left(0.35681 \text{ kip/ft}^2\right)}{(2000 \text{ psf})}$$

$$Ratio = 0.17841$$

Status: **PASS**
Ratio: **0.180**

Czerniak

Lateral Soil Pressure (ASD):

L/D - Length to least lateral dimension ratio,

$$L/D = \frac{L}{D}$$

$$L/D = \frac{(5 \text{ ft})}{(48 \text{ in})}$$

$$L/D = 1.25$$

Since L/D $\leq$ 10,

Pile is short.

Considering x-direction:

$H_o = -0.046975 \text{ kip/ft}$ - Lateral force per length of pile,
$M_o = 1.4607 \text{ kipft/ft}$ - Overturning moment per length of pile,
a - Distance from resting surface to pivot point,

$$a = \frac{(4\, M_o\, L_e) + \left(3\, H_o\, L_e^2\right)}{(6\, M_o) + (4\, H_o\, L_e)}$$

$$a = \frac{(4 \times (1.4607 \text{ kipft/ft}) \times (5 \text{ ft})) + \left(3 \times (-0.046975 \text{ kip/ft}) \times (5 \text{ ft})^2\right)}{(6 \times (1.4607 \text{ kipft/ft})) + (4 \times (-0.046975 \text{ kip/ft}) \times (5 \text{ ft}))}$$

$$a = 3.3737 \text{ ft}$$

p - Earth pressure against the pile at distance a/2 from resting surface,

$$p = \frac{0.75\, [(4\, M_o) + (3\, H_o\, L_e)]^2}{L_e^2\, [(3\, M_o) + (2\, H_o\, L_e)]}$$

$$p = \frac{0.75 \times [(4 \times (1.4607 \text{ kipft/ft})) + (3 \times (-0.046975 \text{ kip/ft}) \times (5 \text{ ft}))]^{\;2}}{(5 \text{ ft})^2 \times [(3 \times (1.4607 \text{ kipft/ft})) + (2 \times (-0.046975 \text{ kip/ft}) \times (5 \text{ ft}))]}$$

$$p = 0.20244 \text{ kip/ft}^2$$

s - Earth pressure against the pile at distance L_e,

$$s = \frac{6\, [(2\, M_o) + (H_o\, L_e)]}{L_e^2}$$

$$s = \frac{6 \times [(2 \times (1.4607 \text{ kipft/ft})) + ((-0.046975 \text{ kip/ft}) \times (5 \text{ ft}))]}{(5 \text{ ft})^2}$$

$$s = 0.64475 \text{ kip/ft}^2$$

Check lateral soil pressure capacity:

p_a - Allowable lateral soil pressure at depth a/2,

$$p_a = R\, \frac{a}{2}$$

$$p_a = (150 \text{ psf/ft}) \times \frac{(3.3737 \text{ ft})}{2}$$

$$p_a = 0.25303 \text{ kip/ft}^2$$

$Ratio$ - Lateral soil capacity

$$Ratio = \frac{p}{p_a}$$

$$Ratio = \frac{\left(0.20244\ \mathrm{kip/ft^2}\right)}{\left(0.25303\ \mathrm{kip/ft^2}\right)}$$

$$Ratio = 0.80007$$

Status: **PASS**
Ratio: **0.800**

p_s - Allowable lateral soil pressure at depth L_e,

$$p_s = R\,L_e$$

$$p_s = (150\ \mathrm{psf/ft}) \times (5\ \mathrm{ft})$$

$$p_s = 0.75\ \mathrm{kip/ft^2}$$

$Ratio$ - Lateral soil capacity

$$Ratio = \frac{s}{p_s}$$

$$Ratio = \frac{\left(0.64475\ \mathrm{kip/ft^2}\right)}{\left(0.75\ \mathrm{kip/ft^2}\right)}$$

$$Ratio = 0.85967$$

Status: **PASS**
Ratio: **0.860**

Considering z-direction:

$H_o = 0.0017516\ \mathrm{kip/ft}$ - Lateral force per length of pile,
$M_o = 0.006051\ \mathrm{kipft/ft}$ - Overturning moment per length of pile,
a - Distance from resting surface to pivot point,

$$a = \frac{(4\,M_o\,L_e) + \left(3\,H_o\,L_e^2\right)}{(6\,M_o) + (4\,H_o\,L_e)}$$

$$a = \frac{(4 \times (0.006051\ \mathrm{kipft/ft}) \times (5\ \mathrm{ft})) + \left(3 \times (0.0017516\ \mathrm{kip/ft}) \times (5\ \mathrm{ft})^2\right)}{(6 \times (0.006051\ \mathrm{kipft/ft})) + (4 \times (0.0017516\ \mathrm{kip/ft}) \times (5\ \mathrm{ft}))}$$

$$a = 3.5379\ \mathrm{ft}$$

p - Earth pressure against the pile at distance a/2 from resting surface,

$$p = \frac{0.75\,[(4\,M_o) + (3\,H_o\,L_e)]^2}{L_e^2\,[(3\,M_o) + (2\,H_o\,L_e)]}$$

$$p = \frac{0.75 \times [(4 \times (0.006051\ \mathrm{kipft/ft})) + (3 \times (0.0017516\ \mathrm{kip/ft}) \times (5\ \mathrm{ft}))]^{\ 2}}{(5\ \mathrm{ft})^2 \times [(3 \times (0.006051\ \mathrm{kipft/ft})) + (2 \times (0.0017516\ \mathrm{kip/ft}) \times (5\ \mathrm{ft}))]}$$

$$p = 0.002143\ \mathrm{kip/ft^2}$$

s - Earth pressure against the pile at distance L_e,

$$s = \frac{6\,[(2\,M_o) + (H_o\,L_e)]}{L_e^2}$$

$$s = \frac{6 \times [(2 \times (0.006051\ \mathrm{kipft/ft})) + ((0.0017516\ \mathrm{kip/ft}) \times (5\ \mathrm{ft}))]}{(5\ \mathrm{ft})^2}$$

$$s = 0.0050064\ \mathrm{kip/ft^2}$$

Check lateral soil pressure capacity:

p_a - Allowable lateral soil pressure at depth a/2,

$$p_a = R\,\frac{a}{2}$$

$$p_a = (150\ \mathrm{psf/ft}) \times \frac{(3.5379\ \mathrm{ft})}{2}$$

$$p_a = 0.26535\ \mathrm{kip/ft^2}$$

$Ratio$ - Lateral soil capacity

$$Ratio = \frac{p}{p_a}$$

$$Ratio = \frac{\left(0.002143\ \mathrm{kip/ft^2}\right)}{\left(0.26535\ \mathrm{kip/ft^2}\right)}$$

$$Ratio = 0.0080764$$

Status: **PASS**
Ratio: **0.010**

p_s - Allowable lateral soil pressure at depth L_e,

$$p_s = R\,L_e$$

$$p_s = (150\ \mathrm{psf/ft}) \times (5\ \mathrm{ft})$$

$$p_s = 0.75\ \mathrm{kip/ft^2}$$

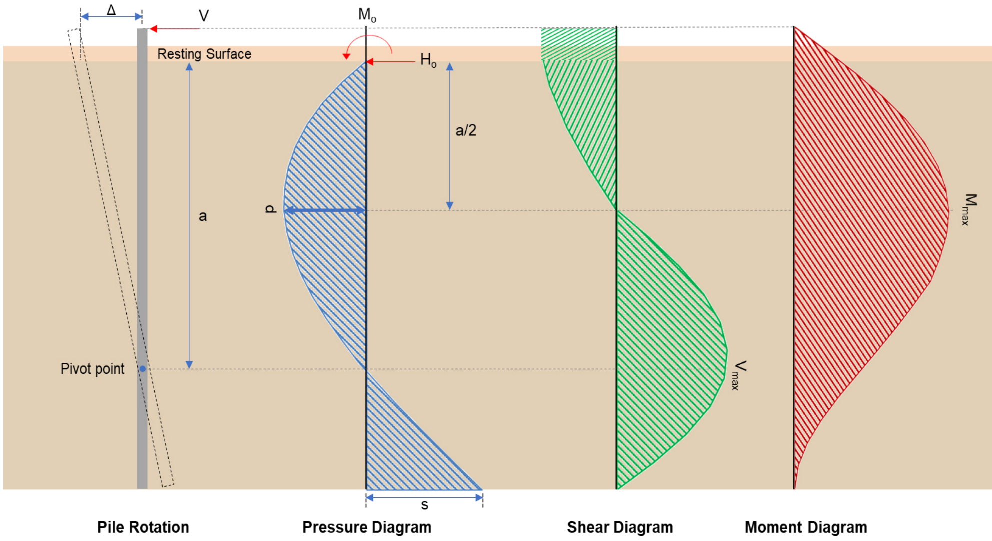
$Ratio$ - Lateral soil capacity

$$Ratio = \frac{s}{p_s}$$

$$Ratio = \frac{(0.0050064\ \mathrm{kip/ft^2})}{(0.75\ \mathrm{kip/ft^2})}$$

$$Ratio = 0.0066752$$

Status: **PASS**
Ratio: **0.010**



Shear force and Bending moment (x-direction, LRFD)

H_o - Lateral force per length of pile,

$$H_o = \frac{V_x}{1.57\,D}$$

$$H_o = \frac{(-0.491\ \mathrm{kip})}{1.57 \times (48\ \mathrm{in})}$$

$$H_o = -0.078185\ \mathrm{kip/ft}$$

M_o - Moment per length of pile,

$$M_o = \frac{M_z + (V_x\,H)}{1.57\,D}$$

$$M_o = \frac{(15.741\ \mathrm{kipft}) + ((-0.491\ \mathrm{kip}) \times (0\ \mathrm{ft}))}{1.57 \times (48\ \mathrm{in})}$$

$$M_o = 2.5065\ \mathrm{kipft/ft}$$

E - Distance from lateral load to resisting surface,

$$E = \frac{M_o}{H_o}$$

$$E = \frac{(2.5065\ \mathrm{kipft/ft})}{(-0.078185\ \mathrm{kip/ft})}$$

$$E = 32.059\ \mathrm{ft}$$

a - Distance from resting surface to pivot point,

$$a = \frac{(4\,M_o\,L_e) + \left(3\,H_o\,L_e^2\right)}{(6\,M_o) + (4\,H_o\,L_e)}$$

$$a = \frac{(4 \times (2.5065\ \mathrm{kipft/ft}) \times (5\ \mathrm{ft})) + \left(3 \times (-0.078185\ \mathrm{kip/ft}) \times (5\ \mathrm{ft})^2\right)}{\ldots}$$

$$a = \frac{}{(6 \times (2.5065\ \text{kipft/ft})) + (4 \times (-0.078185\ \text{kip/ft}) \times (5\ \text{ft}))}$$

$$a = 3.3726\ \text{ft}$$

V_{max} - Max shear force located at depth a,

$$V_{max} = (H_o\, D) \left[1 - \left[3 \left(\frac{4\,E}{L_e} + 3\right) \left(\frac{a}{L_e}\right)^2\right] + \left[4 \left(\frac{3\,E}{L_e} + 2\right) \left(\frac{a}{L_e}\right)^3\right]\right]$$

$$V_{max} = ((-0.078185\ \text{kip/ft}) \times (48\ \text{in})) \times \left[1 - \left[3 \times \left(\frac{4 \times (32.059\ \text{ft})}{(5\ \text{ft})} + 3\right) \times \left(\frac{(3.3726\ \text{ft})}{(5\ \text{ft})}\right)^2\right] + \left[4 \times \left(\frac{3 \times (32.059\ \text{ft})}{(5\ \text{ft})} + 2\right) \times \left(\frac{(3.3726\ \text{ft})}{(5\ \text{ft})}\right)^3\right]\right]$$

$$V_{max} = 3.7634\ \text{kip}$$

M_{max} - Max bending moment located at depth a/2,

$$M_{max} = (H_o\, D\, L_e) \left[\left(\frac{E}{L_e} + \frac{a}{2\,L_e}\right) - \left[\left(\frac{4\,E}{L_e} + 3\right) \left(\frac{a}{2\,L_e}\right)^3\right] + \left[\left(\frac{3\,E}{L_e} + 2\right) \left(\frac{a}{2\,L_e}\right)^4\right]\right]$$

$$M_{max} = ((-0.078185\ \text{kip/ft}) \times (48\ \text{in}) \times (5\ \text{ft})) \times \left[\left(\frac{(32.059\ \text{ft})}{(5\ \text{ft})} + \frac{(3.3726\ \text{ft})}{2 \times (5\ \text{ft})}\right) - \left[\left(\frac{4 \times (32.059\ \text{ft})}{(5\ \text{ft})} + 3\right) \times \left(\frac{(3.3726\ \text{ft})}{2 \times (5\ \text{ft})}\right)^3\right] + \left[\left(\frac{3 \times (32.059\ \text{ft})}{(5\ \text{ft})} + 2\right) \times \left(\frac{(3.3726\ \text{ft})}{2 \times (5\ \text{ft})}\right)^4\right]\right]$$

$$M_{max} = 9.2647\ \text{kipft}$$

Shear force and Bending moment (z-direction, LRFD)

H_o - Lateral force per length of pile,

$$H_o = \frac{V_z}{1.57\,b}$$

$$H_o = \frac{(0.017\ \text{kip})}{1.57 \times (48\ \text{in})}$$

$$H_o = 0.002707\ \text{kip/ft}$$

M_o - Moment per length of pile,

$$M_o = \frac{M_x + (V_z\, H)}{1.57\,b}$$

$$M_o = \frac{(0.06\ \text{kipft}) + ((0.017\ \text{kip}) \times (0\ \text{ft}))}{1.57 \times (48\ \text{in})}$$

$$M_o = 0.0095541\ \text{kipft/ft}$$

E - Distance from lateral load to resisting surface,

$$E = \frac{M_o}{H_o}$$

$$E = \frac{(0.0095541\ \text{kipft/ft})}{(0.002707\ \text{kip/ft})}$$

$$E = 3.5294\ \text{ft}$$

a - Distance from resting surface to pivot point,

$$a = \frac{(4\,M_o\,L_e) + \left(3\,H_o\,L_e^2\right)}{(6\,M_o) + (4\,H_o\,L_e)}$$

$$a = \frac{(4 \times (0.0095541\ \text{kipft/ft}) \times (5\ \text{ft})) + \left(3 \times (0.002707\ \text{kip/ft}) \times (5\ \text{ft})^2\right)}{(6 \times (0.0095541\ \text{kipft/ft})) + (4 \times (0.002707\ \text{kip/ft}) \times (5\ \text{ft}))}$$

$$a = 3.5357\ \text{ft}$$

V_{max} - Max shear force located at depth a,

$$V_{max} = (H_o\, b) \left[1 - \left[3 \left(\frac{4\,E}{L_e} + 3\right) \left(\frac{a}{L_e}\right)^2\right] + \left[4 \left(\frac{3\,E}{L_e} + 2\right) \left(\frac{a}{L_e}\right)^3\right]\right]$$

$$V_{max} = ((0.002707 \text{ kip/ft}) \times (48 \text{ in})) \times \left[1 - \left[3 \times \left(\frac{4 \times (3.5294 \text{ ft})}{(5 \text{ ft})} + 3\right) \times \left(\frac{(3.5357 \text{ ft})}{(5 \text{ ft})}\right)^2\right] + \left[4 \times \left(\frac{3 \times (3.5294 \text{ ft})}{(5 \text{ ft})} + 2\right) \times \left(\frac{(3.5357 \text{ ft})}{(5 \text{ ft})}\right)^3\right]\right]$$

$$V_{max} = 0.020704 \text{ kip}$$

M_{max} - Max bending moment located at depth a/2,

$$M_{max} = (H_o\, b\, L_e) \left[\left(\frac{E}{L_e} + \frac{a}{2\, L_e}\right) - \left[\left(\frac{4\, E}{L_e} + 3\right) \left(\frac{a}{2\, L_e}\right)^3\right] + \left[\left(\frac{3\, E}{L_e} + 2\right) \left(\frac{a}{2\, L_e}\right)^4\right]\right]$$

$$M_{max} = ((0.002707 \text{ kip/ft}) \times (48 \text{ in}) \times (5 \text{ ft})) \times \left[\left(\frac{(3.5294 \text{ ft})}{(5 \text{ ft})} + \frac{(3.5357 \text{ ft})}{2 \times (5 \text{ ft})}\right) - \left[\left(\frac{4 \times (3.5294 \text{ ft})}{(5 \text{ ft})} + 3\right) \times \left(\frac{(3.5357 \text{ ft})}{2 \times (5 \text{ ft})}\right)^3\right] + \left[\left(\frac{3 \times (3.5294 \text{ ft})}{(5 \text{ ft})} + 2\right) \times \left(\frac{(3.5357 \text{ ft})}{2 \times (5 \text{ ft})}\right)^4\right]\right]$$

$$M_{max} = 0.046907 \text{ kipft}$$

Minimum Reinforcement Check (LRFD)

Parameters:

$f'_{ck} = 2.5 \text{ ksi}$ - Concrete strength,
$f_{yk} = 60 \text{ ksi}$ - Longitudinal reinforcement strength,
$\phi = 0.65$ - Reduction factor for axial strength,
Table 22.4.2.1 $\alpha = 0.8$ - Alpha factor for axial strength,
$A_g = 2304 \text{ in}^2$ - Gross area of concrete,

Longitudinal reinforcement:

Required reinforcement due to axial load, $A_{st,required}$

22.4.2.2, 10.6.1.1 $A_{st,required}$

$$A_{st,required} = Min\left[\frac{\frac{P}{\phi\, \alpha} - (0.85\, f'_{ck}\, A_g)}{f_{yk} - (0.85\, f'_{ck})}, (0.08\, A_g)\right]$$

$$A_{st,required} = Min\left[\frac{\frac{(8.968 \text{ kip})}{(0.65) \times (0.8)} - (0.85 \times (2.5 \text{ ksi}) \times (2304 \text{ in}^2))}{(60 \text{ ksi}) - (0.85 \times (2.5 \text{ ksi}))}, (0.08 \times (2304 \text{ in}^2))\right]$$

$$A_{st,required} = -84.298 \text{ in}^2$$

A_{min} - Governing minimum reinforcement area,

$$A_{min} = Max[A_{st,required}, (0.0018\, A_g)]$$

$$A_{min} = Max[(-84.298 \text{ in}^2), (0.0018 \times (2304 \text{ in}^2))]$$

$$A_{min} = 4.1472 \text{ in}^2$$

n_{rebar} - Required number of reinforcement,

$$n_{rebar} = \frac{A_{min}}{A_{rebar}}$$

$$n_{rebar} = \frac{(4.1472 \text{ in}^2)}{(0.3068 \text{ in}^2)}$$

$$n_{rebar} = 14$$

A_{st} - Actual total reinforcement area,

$$A_{st} = n_{rebar}\, \frac{\pi\, d_{bar}^2}{4}$$

$$A_{st} = (14) \times \frac{\pi \times (0.625 \text{ in})^2}{4}$$

$$A_{st} = 4.2951 \text{ in}^2$$

$Ratio$ - Capacity

$$Ratio = \frac{A_{min}}{A_{st}}$$

$$Ratio = \frac{(4.1472 \text{ in}^2)}{(4.2951 \text{ in}^2)}$$

$$Ratio = 0.96556$$

Status: **PASS**
Ratio: **0.970**

25.2.3 s_{rebar} - Minimum spacing of reinforcement,

$$s_{rebar} = Max\left[1.5, (1.5\ d_{bar})\right]$$

$$s_{rebar} = Max\left[1.5, (1.5 \times (0.625\ \text{in}))\right]$$

$$s_{rebar} = 1.5\ \text{in}$$

Ties:

25.7.2.2 Since longitudinal reinforcement is $\leq$ No. 10⌀: Use #3(0.375 in)

25.7.2.1 s_{ties} - Maximum spacing of ties,

$$s_{ties} = Min\left[(16\ d_{bar}), (48\ d_{ties}), Min\,(D, b)\right]$$

$$s_{ties} = Min\left[(16 \times (0.625\ \text{in})), (48 \times (0.375\ \text{in})), Min\,((48\ \text{in}), (48\ \text{in}))\right]$$

$$s_{ties} = 10\ \text{in}$$

Summary:

Main reinforcement: **14 - #5 (0.625 in)**
Ties: **#3(0.375 in) - 10 in**

Axial Compression Strength (ACI 318-19, LRFD)

22.4.2.2 ϕP_N - Allowable axial compressive strength

$$\phi P_N = \phi\ 0.80\ \left[\left(0.85\ f'_{ck}\ [A_g - A_{st}]\right) + (f_{yk}\ A_{st})\right]$$

$$\phi P_N = (0.65) \times 0.80 \times \left[\left(0.85 \times (2.5\ \text{ksi}) \times \left[\left(2304\ \text{in}^2\right) - \left(4.2951\ \text{in}^2\right)\right]\right) + \left((60\ \text{ksi}) \times \left(4.2951\ \text{in}^2\right)\right)\right]$$

$$\phi P_N = 2675.2\ \text{kip}$$

$Ratio$ - Capacity

$$Ratio = \frac{P}{\phi P_N}$$

$$Ratio = \frac{(8.968\ \text{kip})}{(2675.2\ \text{kip})}$$

$$Ratio = 0.0033523$$

Status: **PASS**
Ratio: **0.000**

Shear Strength (ACI 318-19, LRFD)

Parameters:

$b_w = 48\ \text{in}$ - Effective width,

22.5.2.2 d - Effective depth

$$d = 0.80\ D$$

$$d = 0.80 \times (48\ \text{in})$$

$$d = 38.4\ \text{in}$$

22.5.5.1.3 λ_s - size effect modification factor

$$\lambda_s = MIN\left[\sqrt{\frac{2}{1 + \frac{d}{10}}}, 1\right]$$

$$\lambda_s = MIN\left[\sqrt{\frac{2}{1 + \frac{(38.4\ \text{in})}{10}}}, 1\right]$$

$$\lambda_s = 0.64282$$

The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5\ \text{ksi} \rightarrow 2500\ \text{psi}$,

22.5.5.1.1 $V_{c,max}$ - Max shear strength of concrete

$$V_{c,max} = 5\ \lambda_s\ \sqrt{f'_{ck}}\ b_w\ d$$

$$V_{c,max} = 5 \times (0.64282) \times \sqrt{(2500\ \text{psi})} \times (48\ \text{in}) \times (38.4\ \text{in})$$

$$V_{c,max} = 296.21 \text{ kip}$$

The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5 \text{ ksi} \rightarrow 2500 \text{ psi}$, $P = 8.968 \text{ kip} \rightarrow 8968 \text{ lbf}$,

22.5.5.1.1(a) $V_{c,a}$ - Shear strength of concrete (a)

$$V_{c,a} = \left[2\,\lambda_s\,\sqrt{f'_{ck}} + \frac{P}{6\,A_g}\right]\,b_w\,d$$

$$V_{c,a} = \left[2 \times (0.64282) \times \sqrt{(2500 \text{ psi})} + \frac{(8968 \text{ lbf})}{6 \times (2304 \text{ in}^2)}\right] \times (48 \text{ in}) \times (38.4 \text{ in})$$

$$V_{c,a} = 119.68 \text{ kip}$$

The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5 \text{ ksi} \rightarrow 2500 \text{ psi}$,

22.5.5.1.2 $V_{c,b}$ - Shear strength of concrete (b)

$$V_{c,b} = \left[2\,\lambda_s\,\sqrt{f'_{ck}} + \left(0.05\,f'_{ck}\right)\right]\,b_w\,d$$

$$V_{c,b} = \left[2 \times (0.64282) \times \sqrt{(2500 \text{ psi})} + (0.05 \times (2500 \text{ psi}))\right] \times (48 \text{ in}) \times (38.4 \text{ in})$$

$$V_{c,b} = 348.89 \text{ kip}$$

V_c - Governing shear strength of concrete

$$V_c = Min\left[V_{c,max}, V_{c,a}, V_{c,b}\right]$$

$$V_c = Min\left[(296.21 \text{ kip}), (119.68 \text{ kip}), (348.89 \text{ kip})\right]$$

$$V_c = 119.68 \text{ kip}$$

The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5 \text{ ksi} \rightarrow 2500 \text{ psi}$,

22.5.1.2 $V_{s,a}$ - Shear strength of steel (a)

$$V_{s,a} = 8\,\sqrt{f'_{ck}}\,b_w\,d$$

$$V_{s,a} = 8 \times \sqrt{(2500 \text{ psi})} \times (48 \text{ in}) \times (38.4 \text{ in})$$

$$V_{s,a} = 737.28 \text{ kip}$$

A_v - Ties rebar area,

$$A_v = \frac{\pi\,d_{ties}^2}{4}$$

$$A_v = \frac{\pi \times (0.375 \text{ in})^2}{4}$$

$$A_v = 0.11045 \text{ in}^2$$

22.5.8.5.3 $V_{s,b}$ - Shear strength of steel (b)

$$V_{s,b} = \frac{2\,A_v\,f_{ywk}\,d}{s_{ties}}$$

$$V_{s,b} = \frac{2 \times \left(0.11045 \text{ in}^2\right) \times (60 \text{ ksi}) \times (38.4 \text{ in})}{(10 \text{ in})}$$

$$V_{s,b} = 50.894 \text{ kip}$$

V_s - Governing shear strength of steel

$$V_s = MIN\left[V_{s,a}, V_{s,b}\right]$$

$$V_s = MIN\left[(737.28 \text{ kip}), (50.894 \text{ kip})\right]$$

$$V_s = 50.894 \text{ kip}$$

22.5.1.1 ϕV_n - Allowable shear strength

$$\phi V_n = \phi\,\left(V_c + V_s\right)$$

$$\phi V_n = (0.65) \times ((119.68 \text{ kip}) + (50.894 \text{ kip}))$$

$$\phi V_n = 110.87 \text{ kip}$$

Considering x-direction:

$V_{max} = 3.7634 \text{ kip}$ - Maximum shear force in the x-direction,
$Ratio$ - Capacity

$$Ratio = \frac{V_{max}}{\phi V_n}$$

$$Ratio = \frac{(3.7634 \text{ kip})}{(110.87 \text{ kip})}$$

$$Ratio = 0.033943$$

Status: **PASS**
Ratio: **0.030**

Considering z-direction:

$V_{max} = 0.020704 \text{ kip}$ - Maximum shear force in the z-direction,
$Ratio$ - Capacity

$$Ratio = \frac{V_{max}}{\phi V_n}$$

$$Ratio = \frac{(0.020704 \text{ kip})}{(110.87 \text{ kip})}$$

$$Ratio = 0.00018673$$

Status: **PASS**
Ratio: **0.000**

Flexural Strength (ACI 318-19, LRFD)

S_m - Section modulus

$$S_m = \frac{b\, D^2}{6}$$

$$S_m = \frac{(48 \text{ in}) \times (48 \text{ in})^2}{6}$$

$$S_m = 18432 \text{ in}^3$$

$\lambda = 1$ - Concrete modification factor (Normal concrete),
Allowable flexural strength:
M_n shall be the lesser of:
$\phi M_{n,1}$

$$\phi M_{n,1} = \phi \times 5 \times \lambda \times \sqrt{(f_c')} \times S_m$$

$$\phi M_{n,1} = 0.65 \times 5 \times 1 \times \sqrt{(2.5ksi)} \times 18432.001 in^3$$

$$\phi M_{n,1} = 249.600 kipft$$

14.5.2.1b $\phi M_{n,2}$

$$\phi M_{n,2} = \phi\, 0.85\, f_{ck}'\, S_m$$

$$\phi M_{n,2} = (0.65) \times 0.85 \times (2.5 \text{ ksi}) \times \left(18432 \text{ in}^3\right)$$

$$\phi M_{n,2} = 2121.6 \text{ kipft}$$

Therefore,
ϕM_n - Allowable flexural strength,

$$\phi M_n = MIN[\phi M_{n,1}, \phi M_{n,2}]$$

$$\phi M_n = MIN[(249.6 \text{ kipft}), (2121.6 \text{ kipft})]$$

$$\phi M_n = 249.6 \text{ kipft}$$

Considering x-direction:

$M_{max} = 9.2647 \text{ kipft}$ - Maximum moment in the x-direction,
$Ratio$ - Capacity

$$Ratio = \frac{M_{max}}{\phi M_n}$$

$$Ratio = \frac{(9.2647 \text{ kipft})}{(249.6 \text{ kipft})}$$

$$Ratio = 0.037118$$

Status: **PASS**
Ratio: **0.040**

Considering z-direction:

$M_{max} = 0.046907 \text{ kipft}$ - Maximum moment in the z-direction,
$Ratio$ - Capacity

$$Ratio = \frac{M_{max}}{\phi M_n}$$

	$$Ratio = \frac{(0.046907 \text{ kipft})}{(249.6 \text{ kipft})}$$ $$Ratio = 0.00018793$$	Status: **PASS** Ratio: **0.000**