

Your Project Calculations



Project Name: MTSOLAR_24LG7L1KIDJIF

S3D Model Link:

[https://platform.skyciv.com/structural?](https://platform.skyciv.com/structural?preload_name=MTSOLAR_24LG7L1KIDJIF&preload_path=Shared%20Enterprise%20Folder/MT_Solar_Projects/8_2023)

[preload_name=MTSOLAR_24LG7L1KIDJIF&preload_path=Shared%20Enterprise%20Folder/MT_Solar_Projects/8_2023](https://platform.skyciv.com/structural?preload_name=MTSOLAR_24LG7L1KIDJIF&preload_path=Shared%20Enterprise%20Folder/MT_Solar_Projects/8_2023)

Public Model Link:

https://platform.skyciv.com/structural-viewer?project_id=MxvahVCjmnYIFcThztAmnWPwpytpqQB7tBL8HJyGpiRj0byOU1le8RNN6DZYn1d

Array Specification

Product:	Beam
Unique ID:	3P-19.75-6TOP-HD-45-L-4Hx10W-46HD
Duty Classification:	HD
Module Width:	40.00 in
Module Length:	65.00in
Number of Rows:	4
Number of Columns:	10
Total Number of Modules:	40
Desired Tilt Angle:	5
Front Edge Clearance:	10
Total Array Height at Tilt:	11.17 ft
Total Frame Length:	54.50 ft
Frame Weight:	2337 lbs
Array Dimensions N/S:	13.50 ft
Array Dimensions E/W:	55.00 ft
Rail Length:	162.00 in
Rail Spacing:	2.71 ft
Rail Check:	Not Checked

Support Specifications

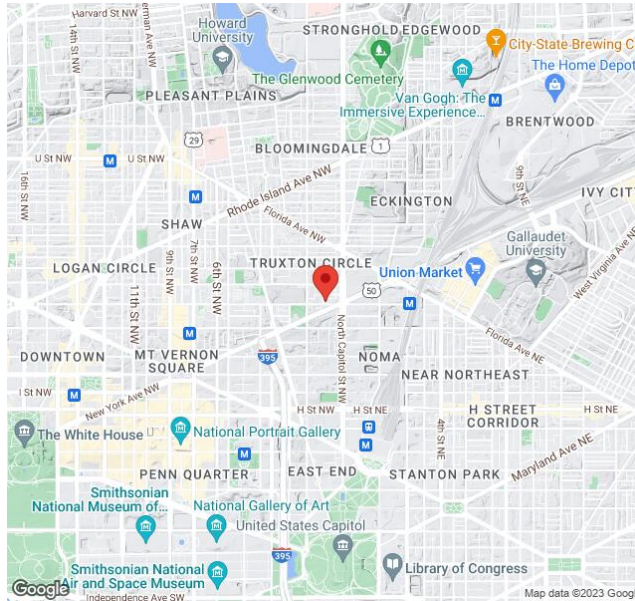
Pole Size:	6in Pipe Sch 40
Pole Length above Grade:	10.59 ft
Number of Poles:	3
Pole Spacing:	19.75 ft

Foundation Specifications

Foundation Type:	Square
Foundation Dimensions:	48 x 48 in
Foundation Depth (below grade):	Pile 1: 4.50 ft Pile 2: 4.75 ft Pile 3: 4.50 ft
Foundation Volume:	8.148 y ³
Foundation Result:	PASSED
Mount Twist:	0.024087 kip

Site Info

Risk Category:	I
Exposure:	C
Soil Classification:	sand
Site Location:	31 N St NW, Washington, DC 20001, USA
Wind Speed:	105 mph
Snow Load:	25 psf
Design Uplift Pressure:	Multiple pressures
Design Downforce Pressure:	Multiple pressures
Design Snow Pressure:	0.015120 ksf



Design Disclaimer

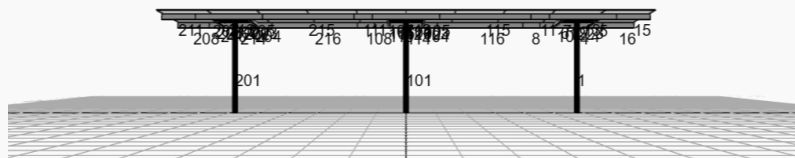
This software should be used for preliminary designs and should not be used as a final design unless reviewed, verified and designed by a qualified structural engineer.

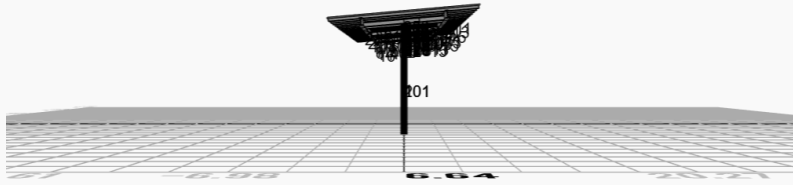
AutoDesigner Input

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  "exposure_category": "C",
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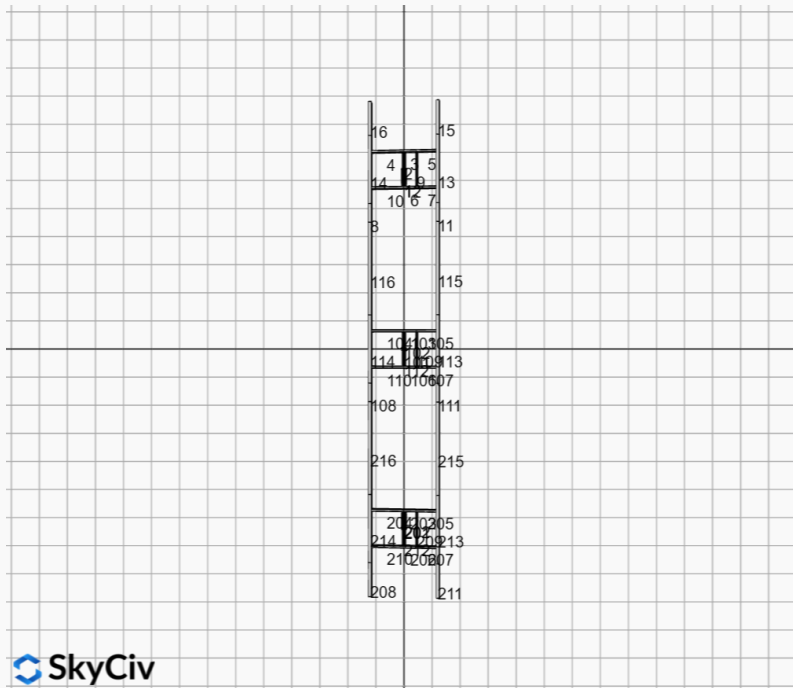
Design Notes:

- AISC Deflection checks are set to L/1 due to structure design intent
- Foundation Design and Sizing is approximate only

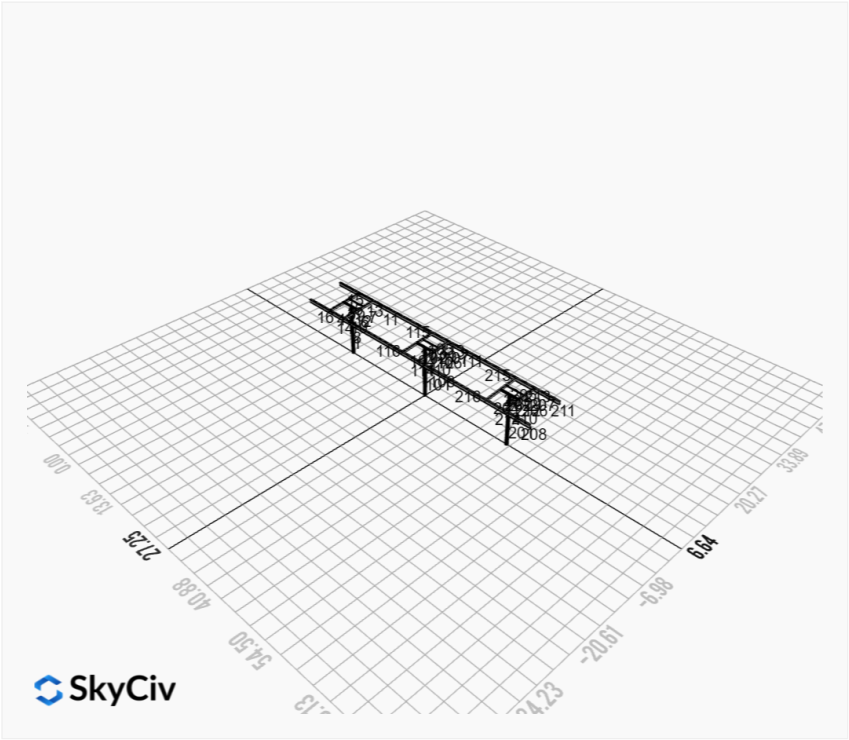




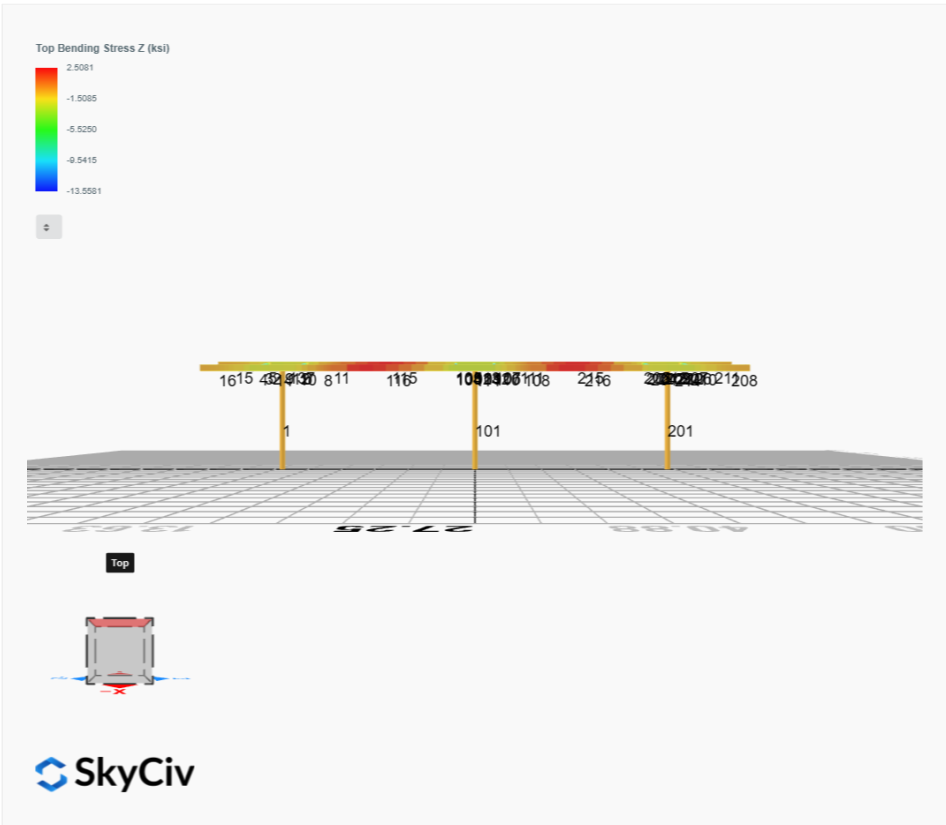
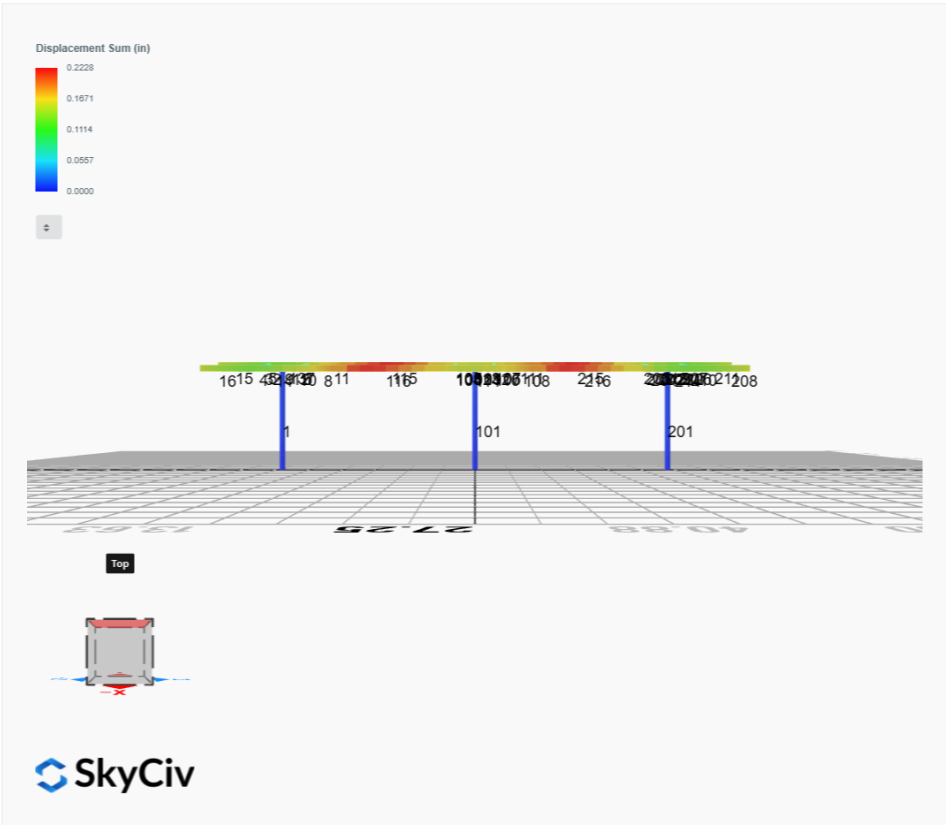
 SkyCiv

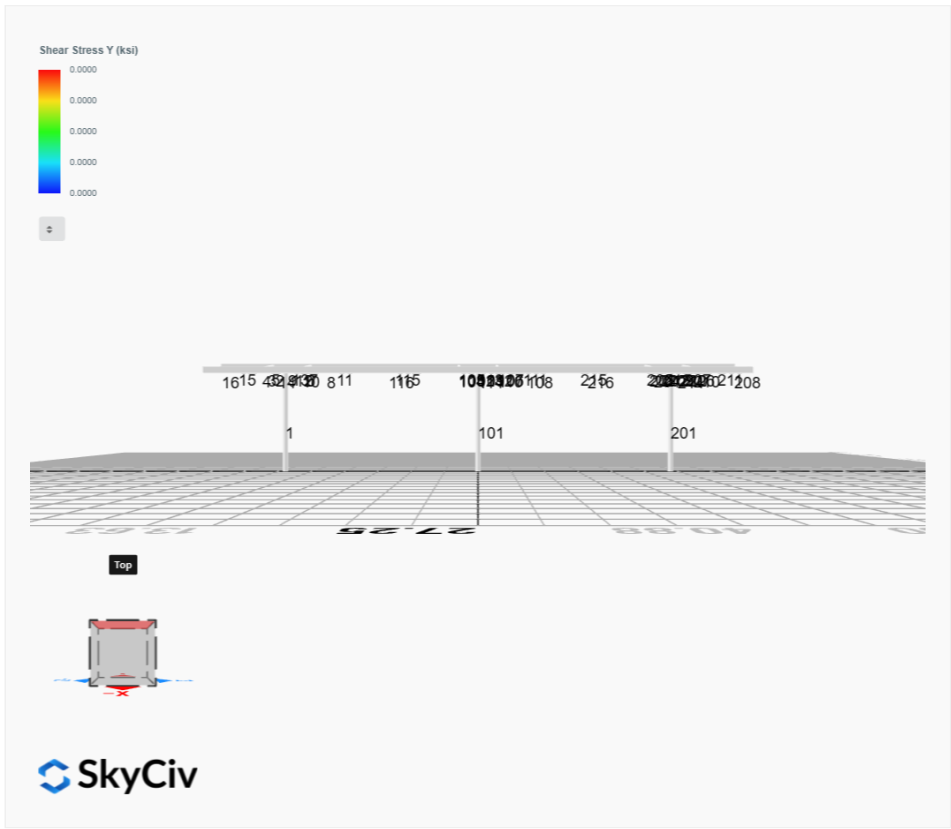
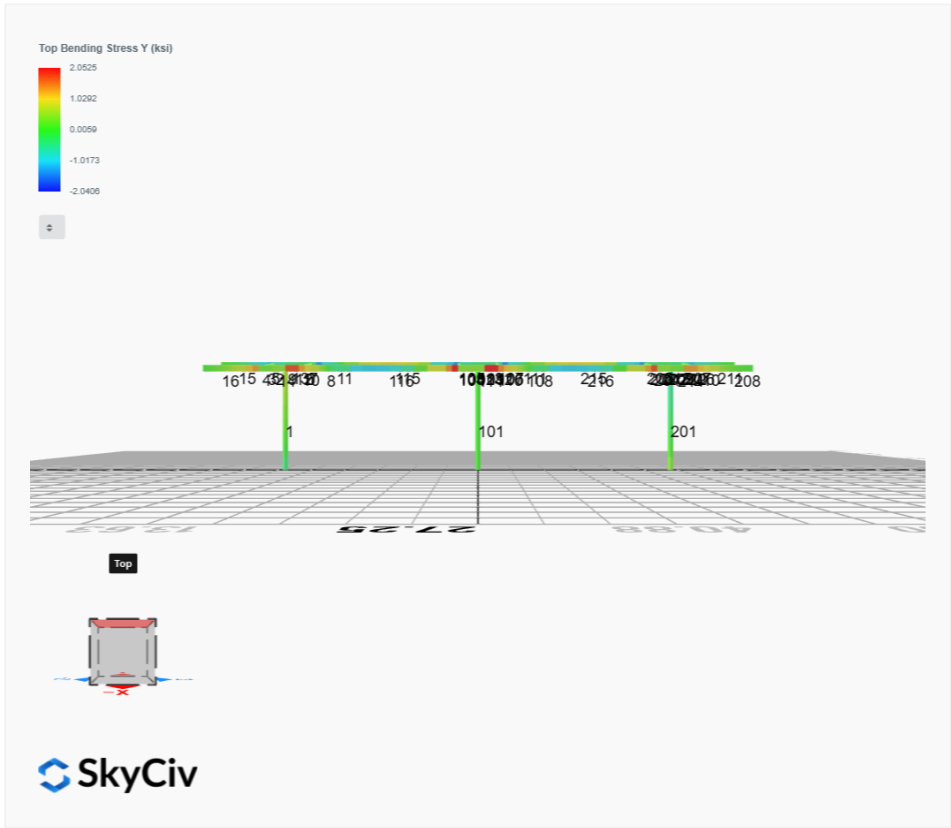


 SkyCiv



FEM Results (Envelope Worst Case for each member)







Reaction Forces for Foundation 1 (Node ID#1), (kip, kip-ft)

ASD Load Combination Results

Name	Fx	Fy	Fz	Mx	My	Mz
ULS: 1. D	0.0015	1.8784	0.0224	0.0742	-0.0017	0.0161
ULS: 2. D + L	0.0015	1.8784	0.0224	0.0742	-0.0017	0.0161
ULS: 3. D + (S or Lr or R)	0.0050	5.3573	0.0761	0.2519	-0.0058	-0.0116
ULS: 3. D + (S or Lr or R)	0.0015	1.8784	0.0224	0.0742	-0.0017	0.0161
ULS: 4. D + 0.75L + 0.75(S or Lr or R)	0.0041	4.4876	0.0626	0.2075	-0.0047	-0.0047
ULS: 4. D + 0.75L + 0.75(S or Lr or R)	0.0015	1.8784	0.0224	0.0742	-0.0017	0.0161
ULS: 5b. D + 0.7E	0.0015	1.8784	0.0224	0.0742	-0.0017	0.0161
ULS: 6b. D + 0.75L + 0.75(0.7)E + 0.75S	0.0041	4.4876	0.0626	0.2075	-0.0047	-0.0047
ULS: 8. 0.6D + 0.7E	0.0009	1.1270	0.0135	0.0445	-0.0010	0.0097
ULS: 5a. D + 0.6W_Wind downforce Case A only	-0.2239	4.4049	0.0622	0.2054	-0.0135	2.9790
ULS: 5a. D + 0.6W_Wind downforce Case B only	-0.2239	4.4049	0.0622	0.2054	-0.0135	2.9790
ULS: 5a. D + 0.6W_Wind uplift Case A only	0.0580	1.1978	0.0130	0.0432	-0.0006	2.0225
ULS: 5a. D + 0.6W_Wind uplift Case B only	0.1528	0.2722	-0.0053	-0.0163	0.0098	-7.3050
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case A only	-0.1650	6.3825	0.0925	0.3059	-0.0136	2.2175
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case B only	-0.1650	6.3825	0.0925	0.3059	-0.0136	2.2175
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case A only	0.0465	3.9771	0.0556	0.1842	-0.0039	1.5001
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case B only	0.1176	3.2829	0.0419	0.1396	0.0039	-5.4955
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case A only	-0.1676	3.7733	0.0523	0.1726	-0.0106	2.2383
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case B only	-0.1676	3.7733	0.0523	0.1726	-0.0106	2.2383
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case A only	0.0438	1.3680	0.0154	0.0509	-0.0009	1.5209
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case B only	0.1149	0.6738	0.0017	0.0063	0.0069	-5.4747
ULS: 7. 0.6D + 0.6W_Wind downforce Case A only	-0.2245	3.6535	0.0533	0.1757	-0.0129	2.9725
ULS: 7. 0.6D + 0.6W_Wind downforce Case B only	-0.2245	3.6535	0.0533	0.1757	-0.0129	2.9725
ULS: 7. 0.6D + 0.6W_Wind uplift Case A only	0.0574	0.4464	0.0041	0.0135	0.0001	2.0160
ULS: 7. 0.6D + 0.6W_Wind uplift Case B only	0.1522	-0.4792	-0.0142	-0.0459	0.0105	-7.3115

Worst Case Reactions LRFD

These calculations are taken directly from the FEA via SkyCiv and are used in the Concrete Checks of the Foundation Module.
Note: Worst case values are assumed as downforce wind load cases.

Result	Value (kip, kip-ft)
Axial	9.9257
Shear X	-0.3757
Shear Z	0.1464
Moment X	0.4863
Moment Y (Twist)	0.0241
Moment Z	12.6697

Worst Case Reactions ASD

These results are taken from the worst case values in the above table and are used in the Soil Checks in the Foundation Module.
Note: Worst case values are assumed as downforce wind load cases.

Result	Value (kip, kip-ft)
Axial	6.3825
Shear X	-0.2245
Shear Z	0.0925
Moment X	0.3059
Moment Y (Twist)	0.0136
Moment Z	7.3115

Reaction Forces for Foundation 2 (Node ID#101), (kip, kip-ft)

ASD Load Combination Results

Name	Fx	Fy	Fz	Mx	My	Mz
ULS: 1. D	-0.0029	2.1497	-0.0000	0.0000	0.0000	0.0546
ULS: 2. D + L	-0.0029	2.1497	-0.0000	0.0000	0.0000	0.0546
ULS: 3. D + (S or Lr or R)	-0.0099	6.2740	0.0000	0.0000	0.0000	0.1199
ULS: 3. D + (S or Lr or R)	-0.0029	2.1497	-0.0000	0.0000	0.0000	0.0546
ULS: 4. D + 0.75L + 0.75(S or Lr or R)	-0.0082	5.2430	0.0000	0.0000	0.0000	0.1036
ULS: 4. D + 0.75L + 0.75(S or Lr or R)	-0.0029	2.1497	-0.0000	0.0000	0.0000	0.0546
ULS: 5b. D + 0.7E	-0.0029	2.1497	-0.0000	0.0000	0.0000	0.0546

Name	Fx	Fy	Fz	Mx	My	Mz
ULS: 6b. D + 0.75L + 0.75(0.7)E + 0.75S	-0.0082	5.2430	0.0000	0.0000	0.0000	0.1036
ULS: 8. 0.6D + 0.7E	-0.0018	1.2898	-0.0000	0.0000	0.0000	0.0328
ULS: 5a. D + 0.6W_Wind downforce Case A only	-0.2561	5.1434	-0.0000	0.0000	0.0000	3.3204
ULS: 5a. D + 0.6W_Wind downforce Case B only	-0.2561	5.1434	-0.0000	0.0000	0.0000	3.3204
ULS: 5a. D + 0.6W_Wind uplift Case A only	0.0741	1.3396	-0.0000	0.0000	0.0000	2.1232
ULS: 5a. D + 0.6W_Wind uplift Case B only	0.1415	0.2531	-0.0000	0.0000	0.0000	-7.7169
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case A only	-0.1981	7.4882	0.0000	0.0000	0.0000	2.5529
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case B only	-0.1981	7.4882	0.0000	0.0000	0.0000	2.5529
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case A only	0.0496	4.6354	0.0000	0.0000	0.0000	1.6550
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case B only	0.1001	3.8205	0.0000	0.0000	0.0000	-5.7250
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case A only	-0.1928	4.3950	-0.0000	0.0000	0.0000	2.5040
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case B only	-0.1928	4.3950	-0.0000	0.0000	0.0000	2.5040
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case A only	0.0548	1.5421	-0.0000	0.0000	0.0000	1.6060
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case B only	0.1054	0.7273	-0.0000	0.0000	0.0000	-5.7740
ULS: 7. 0.6D + 0.6W_Wind downforce Case A only	-0.2549	4.2835	-0.0000	0.0000	0.0000	3.2986
ULS: 7. 0.6D + 0.6W_Wind downforce Case B only	-0.2549	4.2835	-0.0000	0.0000	0.0000	3.2986
ULS: 7. 0.6D + 0.6W_Wind uplift Case A only	0.0752	0.4797	-0.0000	0.0000	0.0000	2.1013
ULS: 7. 0.6D + 0.6W_Wind uplift Case B only	0.1426	-0.6067	-0.0000	0.0000	0.0000	-7.7387

Worst Case Reactions LRFD

These calculations are taken directly from the FEA via SkyCiv and are used in the Concrete Checks of the Foundation Module.
Note: Worst case values are assumed as downforce wind load cases.

Result	Value (kip, kip-ft)
Axial	11.6735
Shear X	-0.4281
Shear Z	-0.0000
Moment X	0.0000
Moment Y (Twist)	0.0000
Moment Z	13.3839

Worst Case Reactions ASD

These results are taken from the worst case values in the above table and are used in the Soil Checks in the Foundation Module.
Note: Worst case values are assumed as downforce wind load cases.

Result	Value (kip, kip-ft)
Axial	7.4882
Shear X	-0.2561
Shear Z	-0.0000
Moment X	0.0000
Moment Y (Twist)	0.0000
Moment Z	7.7387

Reaction Forces for Foundation 3 (Node ID#201), (kip, kip-ft)

ASD Load Combination Results

Name	Fx	Fy	Fz	Mx	My	Mz
ULS: 1. D	0.0015	1.8784	-0.0224	-0.0742	0.0017	0.0161
ULS: 2. D + L	0.0015	1.8784	-0.0224	-0.0742	0.0017	0.0161
ULS: 3. D + (S or Lr or R)	0.0050	5.3573	-0.0761	-0.2519	0.0058	-0.0116
ULS: 3. D + (S or Lr or R)	0.0015	1.8784	-0.0224	-0.0742	0.0017	0.0161
ULS: 4. D + 0.75L + 0.75(S or Lr or R)	0.0041	4.4876	-0.0626	-0.2075	0.0047	-0.0047
ULS: 4. D + 0.75L + 0.75(S or Lr or R)	0.0015	1.8784	-0.0224	-0.0742	0.0017	0.0161
ULS: 5b. D + 0.7E	0.0015	1.8784	-0.0224	-0.0742	0.0017	0.0161
ULS: 6b. D + 0.75L + 0.75(0.7)E + 0.75S	0.0041	4.4876	-0.0626	-0.2075	0.0047	-0.0047
ULS: 8. 0.6D + 0.7E	0.0009	1.1270	-0.0135	-0.0445	0.0010	0.0097
ULS: 5a. D + 0.6W_Wind downforce Case A only	-0.2239	4.4049	-0.0622	-0.2054	0.0135	2.9790
ULS: 5a. D + 0.6W_Wind downforce Case B only	-0.2239	4.4049	-0.0622	-0.2054	0.0135	2.9790
ULS: 5a. D + 0.6W_Wind uplift Case A only	0.0580	1.1978	-0.0130	-0.0432	0.0006	2.0225
ULS: 5a. D + 0.6W_Wind uplift Case B only	0.1528	0.2722	0.0053	0.0163	-0.0098	-7.3050
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case A only	-0.1650	6.3825	-0.0925	-0.3059	0.0136	2.2175
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case B only	-0.1650	6.3825	-0.0925	-0.3059	0.0136	2.2175
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case A only	0.0465	3.9771	-0.0556	-0.1842	0.0039	1.5001
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case B only	0.1176	3.2829	-0.0419	-0.1396	-0.0039	-5.4955

Name	Fx	Fy	Fz	Mx	My	Mz
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case A only	-0.1676	3.7733	-0.0523	-0.1726	0.0106	2.2383
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case B only	-0.1676	3.7733	-0.0523	-0.1726	0.0106	2.2383
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case A only	0.0438	1.3680	-0.0154	-0.0509	0.0009	1.5209
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case B only	0.1149	0.6738	-0.0017	-0.0063	-0.0069	-5.4747
ULS: 7. 0.6D + 0.6W_Wind downforce Case A only	-0.2245	3.6535	-0.0533	-0.1757	0.0129	2.9725
ULS: 7. 0.6D + 0.6W_Wind downforce Case B only	-0.2245	3.6535	-0.0533	-0.1757	0.0129	2.9725
ULS: 7. 0.6D + 0.6W_Wind uplift Case A only	0.0574	0.4464	-0.0041	-0.0135	-0.0001	2.0160
ULS: 7. 0.6D + 0.6W_Wind uplift Case B only	0.1522	-0.4792	0.0142	0.0459	-0.0105	-7.3115

Worst Case Reactions LRFD

These calculations are taken directly from the FEA via SkyCiv and are used in the Concrete Checks of the Foundation Module.
Note: Worst case values are assumed as downforce wind load cases.

Result	Value (kip, kip-ft)
Axial	9.9257
Shear X	-0.3757
Shear Z	-0.1464
Moment X	-0.4863
Moment Y (Twist)	0.0241
Moment Z	12.6698

Worst Case Reactions ASD

These results are taken from the worst case values in the above table and are used in the Soil Checks in the Foundation Module.
Note: Worst case values are assumed as downforce wind load cases.

Result	Value (kip, kip-ft)
Axial	6.3825
Shear X	-0.2245
Shear Z	-0.0925
Moment X	-0.3059
Moment Y (Twist)	0.0136
Moment Z	7.3115

Project Details

Design Code: AISC 360-16 LRFD
 Provision: LRFD
 Country: United States

User Name: sales@mtsolar.us
 Project Name: MTSOLAR_24LG7L1KIDJIF
 Unit System: imperial



Design Input Information

Design Factors			
Φ_t	Φ_c	Φ_b	Φ_v
0.9	0.9	0.9	0.9

Design Materials			
ID	E (ksi)	F_y (ksi)	F_u (ksi)
1	29000	50	65

Section Dimensions								
ID	Name	d (in)	t_w (in)					
2	2in Pipe Sch 80	2.38	0.22					
5	4in Pipe Sch 80	4.50	0.34					
7	6in Pipe Sch 40	6.63	0.28					
ID	Name	d (in)	b (in)	t_w (in)	t_b (in)	r (in)		
16	HSS5x3x16	5.00	3.00	0.17	0.17	0.17		
ID	Name	d (in)	t_w (in)	b_t (in)	b_b (in)	t_t (in)	t_b (in)	r (in)
19	W8x10	7.89	0.17	3.94	3.94	0.20	0.20	0.30

Section Properties								
ID	Name	A (in ²)	J (in ⁴)	I_{yp} (in ⁴)	I_{zp} (in ⁴)	I_w (in ⁶)	S_{yp} (in ³)	S_{zp} (in ³)
2	2in Pipe Sch 80	1.48	1.74	0.87	0.87	0.00	1.02	1.02
5	4in Pipe Sch 80	4.41	19.22	9.61	9.61	0.00	5.85	5.85

7	6in Pipe Sch 40	5.58	56.28	28.14	28.14	0.00	11.28	11.28
16	HSS5x3x3/16	2.58	8.64	3.85	8.53	92.39	2.96	4.21
19	W8x10	2.96	0.04	2.09	30.80	30.90	1.66	8.87

Member Properties								
Member ID	Section ID	K _z L (ft)	K _y L (ft)	L _b (ft)	C _b	L S T	L S C	L D
1	7	22.24	22.24	10.59	-	300	200	1
2	5	4.20	4.20	2.00	-	300	200	1
3	16	0.92	0.92	1.42	1.19,1.18,1.19,1.18,1.18,1.19,1.18,1.18,1.16,1.18,1.18,1.19,1.17,1.18,1.18,1.18,1.18,1.18,1.19,1.15,1.18,1.18,1.19,1.17	300	200	1
4	16	2.44	2.44	3.75	1.69,1.68,1.69,1.67,1.68,1.69,1.67,1.67,1.70,1.68,1.67,1.67,1.59,1.69,1.67,1.67,1.67,1.67,1.68,1.73,1.69,1.67,1.67,1.64,1.69	300	200	1
5	16	1.52	1.52	2.33	1.68,1.67,1.68,1.67,1.68,1.68,1.67,1.67,1.67,1.65,1.67,1.67,1.68,1.66,1.67,1.67,1.67,1.67,1.67,1.67,1.68,1.64,1.67,1.67,1.68,1.66	300	200	1
6	16	0.92	0.92	1.42	1.19,1.18,1.19,1.18,1.19,1.19,1.18,1.18,1.18,1.17,1.18,1.18,1.19,1.18,1.18,1.18,1.18,1.18,1.18,1.19,1.16,1.18,1.18,1.19,1.18	300	200	1
7	16	1.52	1.52	2.33	1.68,1.67,1.68,1.67,1.68,1.68,1.67,1.67,1.67,1.65,1.67,1.67,1.68,1.66,1.67,1.67,1.67,1.67,1.67,1.67,1.68,1.64,1.67,1.67,1.68,1.66	300	200	1
8	19	1.33	1.33	2.05	1.68,1.68,1.68,1.68,1.68,1.68,1.67,1.67,1.51,1.89,1.66,1.66,2.09,2.07,1.67,1.67,1.66,1.72,1.67,1.67,1.51,1.88,1.66,1.66,2.02,2.10	300	200	1
9	2	2.60	2.60	4.00	-	300	200	1
10	16	2.44	2.44	3.75	1.69,1.68,1.69,1.67,1.68,1.69,1.67,1.67,1.70,1.68,1.67,1.67,1.60,1.69,1.67,1.67,1.67,1.67,1.68,1.72,1.69,1.67,1.67,1.64,1.69	300	200	1
11	19	1.33	1.33	2.05	1.69,1.69,1.69,1.69,1.69,1.69,1.71,1.71,1.77,2.08,1.71,1.71,1.87,1.91,1.70,1.70,1.71,1.63,1.71,1.71,1.77,2.08,1.71,1.71,1.94,1.88	300	200	1
12	5	1.30	1.30	2.00	-	300	200	1
13	19	4.88	4.00	7.50	1.12,1.12,1.12,1.12,1.12,1.12,1.12,1.12,1.12,1.22,1.12,1.12,1.13,1.13,1.12,1.12,1.12,1.11,1.11,2.1,1.12,1.12,1.23,1.12,1.12,1.13,1.13	300	200	1
14	19	4.88	4.00	7.50	1.11,1.11,1.11,1.12,1.11,1.11,1.11,1.11,1.11,1.09,1.13,1.11,1.11,1.42,1.20,1.12,1.12,1.11,1.12,1.11,1.11,1.09,1.13,1.11,1.11,1.15,1.33	300	200	1
15	19	7.88	7.88	3.75	2.33,2.33	300	200	1
16	19	7.88	7.88	3.75	2.33,2.33	300	200	1
101	7	22.24	22.24	10.59	-	300	200	1
102	5	1.30	1.30	2.00	-	300	200	1
103	16	0.92	0.92	1.42	1.19,1.18,1.19,1.18,1.18,1.19,1.18,1.18,1.17,1.18,1.18,1.19,1.17,1.18,1.18,1.18,1.18,1.18,1.18,1.19,1.16,1.18,1.18,1.19,1.17	300	200	1
104	16	2.44	2.44	3.75	1.68,1.68,1.68,1.67,1.68,1.68,1.67,1.67,1.69,1.68,1.67,1.67,1.59,1.69,1.67,1.67,1.67,1.67,1.68,1.71,1.69,1.67,1.67,1.64,1.69	300	200	1
105	16	1.52	1.52	2.33	1.68,1.67,1.68,1.67,1.67,1.68,1.67,1.67,1.67,1.65,1.67,1.67,1.68,1.66,1.67,1.67,1.67,1.67,1.67,1.67,1.68,1.64,1.67,1.67,1.68,1.66	300	200	1
106	16	0.92	0.92	1.42	1.19,1.18,1.19,1.18,1.18,1.19,1.18,1.18,1.18,1.17,1.18,1.18,1.19,1.17,1.18,1.18,1.18,1.18,1.18,1.19,1.16,1.18,1.18,1.19,1.17	300	200	1
107	16	1.52	1.52	2.33	1.68,1.67,1.68,1.67,1.67,1.68,1.67,1.67,1.67,1.65,1.67,1.67,1.68,1.66,1.67,1.67,1.67,1.67,1.67,1.67,1.68,1.64,1.67,1.67,1.68,1.66	300	200	1

Member Design Capacity

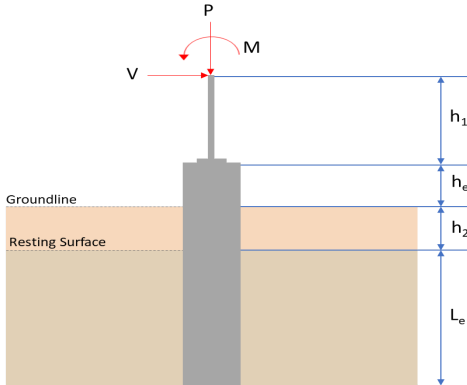
Member ID	$\Phi_t P_n$ (kip)	$\Phi_c P_n$ (kip)	$\Phi_b M_{zn}$ (k-ft)	$\Phi_b M_{yn}$ (k-ft)	$\Phi_v V_{yn}$ (kip)	$\Phi_v V_{zn}$ (kip)
1	251.16	89.30	42.30	42.30	75.35	75.35
2	198.33	182.14	21.95	21.95	59.50	59.50
3	116.10	115.41	15.79	11.10	42.08	23.28
4	116.10	111.33	15.79	11.10	42.08	23.28
5	116.10	114.23	15.79	11.10	42.08	23.28
6	116.10	115.41	15.79	11.10	42.08	23.28
7	116.10	114.23	15.79	11.10	42.08	23.28
8	133.20	126.01	32.87	6.12	40.24	43.62
9	66.48	58.89	3.82	3.82	19.94	19.94
10	116.10	111.33	15.79	11.10	42.08	23.28
11	133.20	126.01	32.87	6.12	40.24	43.62
12	198.33	196.72	21.95	21.95	59.50	59.50
13	133.20	104.94	25.44	6.12	40.24	43.62
14	133.20	104.94	24.98	6.12	40.24	43.62
15	133.20	52.83	32.87	6.12	40.24	43.62
16	133.20	52.83	32.87	6.12	40.24	43.62
101	251.16	89.30	42.30	42.30	75.35	75.35
102	198.33	196.72	21.95	21.95	59.50	59.50
103	116.10	115.41	15.79	11.10	42.08	23.28
104	116.10	111.33	15.79	11.10	42.08	23.28
105	116.10	114.23	15.79	11.10	42.08	23.28
106	116.10	115.41	15.79	11.10	42.08	23.28
107	116.10	114.23	15.79	11.10	42.08	23.28
108	133.20	126.01	32.87	6.12	40.24	43.62
109	66.48	58.89	3.82	3.82	19.94	19.94
110	116.10	111.33	15.79	11.10	42.08	23.28
111	133.20	126.01	32.87	6.12	40.24	43.62
112	198.33	196.72	21.95	21.95	59.50	59.50
113	133.20	104.94	23.60	6.12	40.24	43.62
114	133.20	104.94	23.60	6.12	40.24	43.62
115	133.20	69.16	17.02	6.12	40.24	43.62
116	133.20	69.16	16.87	6.12	40.24	43.62
201	251.16	89.30	42.30	42.30	75.35	75.35
202	198.33	196.72	21.95	21.95	59.50	59.50
203	116.10	115.41	15.79	11.10	42.08	23.28
204	116.10	111.33	15.79	11.10	42.08	23.28
205	116.10	114.23	15.79	11.10	42.08	23.28
206	116.10	115.41	15.79	11.10	42.08	23.28
207	116.10	114.23	15.79	11.10	42.08	23.28
208	133.20	52.83	32.87	6.12	40.24	43.62
209	66.48	58.89	3.82	3.82	19.94	19.94
210	116.10	111.33	15.79	11.10	42.08	23.28
211	133.20	52.83	32.87	6.12	40.24	43.62
212	198.33	182.14	21.95	21.95	59.50	59.50
213	133.20	104.94	25.44	6.12	40.24	43.62
214	133.20	104.94	24.98	6.12	40.24	43.62
215	133.20	69.16	17.18	6.12	40.24	43.62
216	133.20	69.16	17.18	6.12	40.24	43.62

Design Ratio

Member ID	P	M _z	M _y	V _y	V _z	(P,M _z ,M _y)	Worst LC	KL/r	δ	Status
1	0.111	0.300	0.025	0.005	0.002	0.308	#16	0.594	Not Required	Pass
2	0.001	0.365	0.018	0.078	0.003	0.381	#21	0.114	Not Required	Pass
3	0.002	0.547	0.004	0.055	0.001	0.549	#21	0.045	Not Required	Pass
4	0.001	0.534	0.023	0.054	0.005	0.554	#21	0.080	Not Required	Pass
5	0.001	0.339	0.017	0.055	0.004	0.340	#21	0.074	Not Required	Pass
6	0.001	0.596	0.017	0.061	0.004	0.614	#21	0.045	Not Required	Pass
7	0.002	0.369	0.031	0.060	0.008	0.379	#21	0.074	Not Required	Pass
8	0.000	0.074	0.026	0.039	0.003	0.086	#21	0.095	Not Required	Pass
9	0.002	0.068	0.014	0.001	0.001	0.083	#21	0.204	Not Required	Pass
10	0.002	0.579	0.025	0.058	0.005	0.589	#21	0.080	Not Required	Pass
11	0.001	0.075	0.028	0.041	0.003	0.085	#21	0.095	Not Required	Pass
12	0.000	0.413	0.020	0.085	0.003	0.429	#21	0.053	Not Required	Pass
13	0.001	0.182	0.066	0.053	0.003	0.210	#21	0.286	Not Required	Pass
14	0.001	0.182	0.065	0.051	0.003	0.206	#21	0.190	Not Required	Pass
15	0.000	0.059	0.021	0.026	0.002	0.081	#21	Not Required	Not Required	Pass
16	0.000	0.058	0.021	0.025	0.002	0.080	#21	Not Required	Not Required	Pass
101	0.131	0.316	0.000	0.006	0.000	0.325	#16	0.594	Not Required	Pass
102	0.001	0.460	0.022	0.096	0.004	0.480	#21	0.053	Not Required	Pass
103	0.002	0.674	0.010	0.068	0.002	0.685	#21	0.045	Not Required	Pass
104	0.002	0.661	0.027	0.067	0.006	0.680	#21	0.080	Not Required	Pass
105	0.002	0.418	0.028	0.067	0.007	0.425	#21	0.074	Not Required	Pass
106	0.002	0.674	0.010	0.068	0.002	0.685	#21	0.045	Not Required	Pass
107	0.002	0.418	0.028	0.067	0.007	0.425	#21	0.074	Not Required	Pass
108	0.000	0.054	0.027	0.043	0.003	0.064	#21	0.095	Not Required	Pass
109	0.002	0.072	0.008	0.001	0.000	0.081	#21	0.204	Not Required	Pass
110	0.002	0.661	0.027	0.067	0.006	0.680	#21	0.080	Not Required	Pass
111	0.001	0.058	0.026	0.044	0.003	0.064	#21	0.095	Not Required	Pass
112	0.001	0.460	0.022	0.096	0.004	0.480	#21	0.053	Not Required	Pass
113	0.001	0.215	0.065	0.056	0.003	0.261	#21	0.286	Not Required	Pass
114	0.002	0.222	0.065	0.055	0.003	0.264	#21	0.286	Not Required	Pass
115	0.001	0.250	0.034	0.044	0.003	0.284	#21	0.473	Not Required	Pass
116	0.001	0.244	0.035	0.043	0.003	0.279	#21	0.473	Not Required	Pass
201	0.111	0.300	0.025	0.005	0.002	0.308	#16	0.594	Not Required	Pass
202	0.000	0.413	0.020	0.085	0.003	0.429	#21	0.053	Not Required	Pass
203	0.001	0.596	0.017	0.061	0.004	0.614	#21	0.045	Not Required	Pass
204	0.002	0.579	0.025	0.058	0.005	0.589	#21	0.080	Not Required	Pass
205	0.002	0.369	0.031	0.060	0.008	0.379	#21	0.074	Not Required	Pass
206	0.002	0.547	0.004	0.055	0.001	0.549	#21	0.045	Not Required	Pass
207	0.001	0.339	0.017	0.055	0.004	0.340	#21	0.074	Not Required	Pass
208	0.000	0.058	0.021	0.025	0.002	0.080	#21	Not Required	Not Required	Pass
209	0.002	0.068	0.014	0.001	0.001	0.083	#21	0.204	Not Required	Pass
210	0.001	0.534	0.023	0.054	0.005	0.554	#21	0.080	Not Required	Pass
211	0.000	0.059	0.021	0.026	0.002	0.081	#21	Not Required	Not Required	Pass
212	0.001	0.365	0.018	0.078	0.003	0.381	#21	0.114	Not Required	Pass
213	0.001	0.182	0.066	0.053	0.003	0.210	#21	0.190	Not Required	Pass
214	0.001	0.182	0.065	0.051	0.003	0.206	#21	0.286	Not Required	Pass
215	0.001	0.257	0.034	0.041	0.003	0.291	#21	0.473	Not Required	Pass
216	0.001	0.250	0.034	0.039	0.003	0.285	#21	0.473	Not Required	Pass

Definitions

Φ_t	Safety factor for tensile
Φ_c	Safety factor for compression
Φ_b	Safety factor for flexure
Φ_v	Safety factor for shear
E	Modulus of elasticity
F_y	Specified minimum yield stress
F_u	Specified minimum tensile strength
A	Cross-sectional area
J	Torsional constant
I_{yp}	Moment of inertia about the Y axes
I_{zp}	Moment of inertia about the Z axes
I_w	Warping constant
S_{yp}	Plastic section modulus about the Y axis
S_{zp}	Plastic section modulus about the Z axis
KL	Effective length
C_b	Buckling modification factor (from all load combinations)
L_b	Length between braced points
LST	Limited slenderness for tension
LSC	Limited slenderness for compression
LD	Limited deflection
P_n	Nominal axial strength (tension/compression)
M_n	Nominal flexural strength (about Z/Y axis)
V_n	Nominal shear strength (along Z/Y axis)
P	Design ratio in case of axial force
M_z	Design ratio in case of bending about Z axis
M_y	Design ratio in case of bending about Y axis
V_y	Design ratio in case of shear along Y axis
V_z	Design ratio in case of shear along Z axis
(P, M_z , M_y)	Design ratio in case of axial force and bending action
KL/r	Design ratio in case of section slenderness
δ	Design ratio in case of member deflection
OK	Capacity is provided
NG	Capacity is not provided

REFERENCES	CALCULATIONS	RESULTS																										
	SkyCiv Foundation Design Pile Foundation Design Information : Design code : IBC 2021 (International Building Code) Unit System : Imperial																											
	Pile Input  Geometry Pile shape: rectangular b = 48 in - Pile width D = 48 in - Pile depth L = 4.5 ft - Total pile length h1 = 0 ft - Lateral load height from the top of the pile, h2 = 0 ft - Depth to resisting surface he = 0 ft - Length of pile above the ground Tabulation of Soil Parameters <table><thead><tr><th>Layer</th><th>Label</th><th>Allowable Bearing Pressure (qa) (psf)</th><th>Allowable Lateral Pressure (R) (psf/ft)</th></tr></thead><tbody><tr><td>1</td><td>Sand, silty sand, clayey sand, silty gravel & clayey gravel</td><td>2000.000</td><td>150.000</td></tr></tbody></table> Tabulation of Loads <table><thead><tr><th>Load Component</th><th>ASD</th><th>LRFD</th></tr></thead><tbody><tr><td>P (kip)</td><td>6.382</td><td>9.926</td></tr><tr><td>Vx (kip)</td><td>-0.225</td><td>-0.376</td></tr><tr><td>Vz (kip)</td><td>0.093</td><td>0.146</td></tr><tr><td>Mx (kipft)</td><td>0.306</td><td>0.486</td></tr><tr><td>Mz (kipft)</td><td>7.311</td><td>12.670</td></tr></tbody></table> Material Properties f'ck = 2.5 ksi - Concrete strength,	Layer	Label	Allowable Bearing Pressure (qa) (psf)	Allowable Lateral Pressure (R) (psf/ft)	1	Sand, silty sand, clayey sand, silty gravel & clayey gravel	2000.000	150.000	Load Component	ASD	LRFD	P (kip)	6.382	9.926	Vx (kip)	-0.225	-0.376	Vz (kip)	0.093	0.146	Mx (kipft)	0.306	0.486	Mz (kipft)	7.311	12.670	
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Mz (kipft)	7.311	12.670																										
	Required depth to resist lateral loads (ASD) H - Point of application of the lateral load H = h1 + h2 + he H = (0 ft) + (0 ft) + (0 ft) H = 0 ft Considering x-direction: Ho - Lateral force per length of pile, Ho = Vz / (1.57 D) Ho = (-0.225 kip) / (1.57 x (48 in)) Ho = -0.035828 kip/ft Mo - Moment per length of pile, Mo = (Mz + (Vx H)) / (1.57 D)																											

	$M_o = \frac{(7.311 \text{ kipft}) + ((-0.225 \text{ kip}) \times (0 \text{ ft}))}{1.57 \times (48 \text{ in})}$ $M_o = 1.1642 \text{ kipft/ft}$ Required depth of embedment in earth: $L_x^3 - \left(14.14 \times \frac{H_o \times L_x}{R}\right) - \left(18.85 \times \frac{M_o}{R}\right) = 0$ Solving the cubic equation: $L_{e,x} = 4.3748 \text{ ft}$ - Required depth in x-direction, Considering z-direction: H_o - Lateral force per length of pile, $H_o = \frac{V_z}{1.57 b}$ $H_o = \frac{(0.093 \text{ kip})}{1.57 \times (48 \text{ in})}$ $H_o = 0.014809 \text{ kip/ft}$ M_o - Moment per length of pile, $M_o = \frac{M_x + (V_z H)}{1.57 b}$ $M_o = \frac{(0.306 \text{ kipft}) + ((0.093 \text{ kip}) \times (0 \text{ ft}))}{1.57 \times (48 \text{ in})}$ $M_o = 0.048726 \text{ kipft/ft}$ Required depth of embedment in earth: $L_z^3 - \left(14.14 \times \frac{H_o \times L_z}{R}\right) - \left(18.85 \times \frac{M_o}{R}\right) = 0$ Solving the cubic equation: $L_{e,z} = 1.7613 \text{ ft}$ - Required depth in z-direction, Minimum embedded depth required: $L_{e,req}$ - Depth of pile required, $L_{e,req} = MAX[L_{e,x}, L_{e,z}]$ $L_{e,req} = MAX[(4.3748 \text{ ft}), (1.7613 \text{ ft})]$ $L_{e,req} = 4.375 \text{ ft}$ L_e - Actual embedded length of pile, $L_e = L - h_e - h_2$ $L_e = (4.5 \text{ ft}) - (0 \text{ ft}) - (0 \text{ ft})$ $L_e = 4.5 \text{ ft}$ Ratio - Embedded depth $Ratio = \frac{L_{e,req}}{L_e}$ $Ratio = \frac{(4.375 \text{ ft})}{(4.5 \text{ ft})}$ $Ratio = 0.97222$	Status: PASS Ratio: 0.970
	End-bearing Capacity (ASD) A - Pile cross-section area $A = b D$ $A = (48 \text{ in}) \times (48 \text{ in})$ $A = 16 \text{ ft}^2$ q - End-bearing pressure $q = \frac{P_o}{A}$ $q = \frac{(6.382 \text{ kip})}{(16 \text{ ft}^2)}$	

$$q = 0.398875 \text{ kip/ft}^2$$

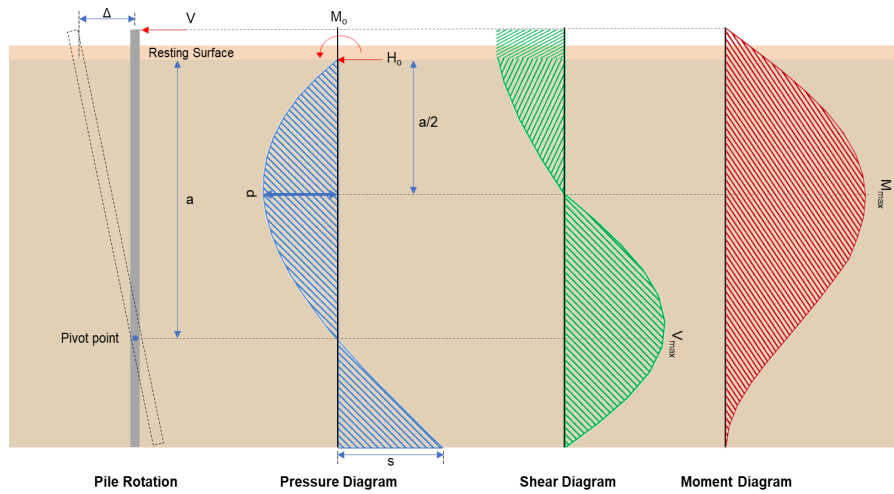
	$q = 0.00000 \text{ kip/ft}$	
	Check bearing capacity ratio: Ratio - Capacity $\text{Ratio} = \frac{q}{q_a}$ $\text{Ratio} = \frac{(0.39888 \text{ kip/ft}^2)}{(2000 \text{ psf})}$ $\text{Ratio} = 0.19944$	Status: PASS Ratio: 0.200
Czerniak	Lateral Soil Pressure (ASD): L/D - Length to least lateral dimension ratio, $L/D = \frac{L}{D}$ $L/D = \frac{(4.5 \text{ ft})}{(48 \text{ in})}$ $L/D = 1.125$ Since $L/D \leq 10$, Pile is short. Considering x-direction: $H_o = -0.035828 \text{ kip/ft}$ - Lateral force per length of pile, $M_o = 1.1642 \text{ kipft/ft}$ - Overturning moment per length of pile, a - Distance from resting surface to pivot point, $a = \frac{(4 M_o L_e) + (3 H_o L_e^2)}{(6 M_o) + (4 H_o L_e)}$ $a = \frac{(4 \times (1.1642 \text{ kipft/ft}) \times (4.5 \text{ ft})) + (3 \times (-0.035828 \text{ kip/ft}) \times (4.5 \text{ ft})^2)}{(6 \times (1.1642 \text{ kipft/ft})) + (4 \times (-0.035828 \text{ kip/ft}) \times (4.5 \text{ ft}))}$ $a = 3.0317 \text{ ft}$ p - Earth pressure against the pile at distance $a/2$ from resting surface, $p = \frac{0.75 [(4 M_o) + (3 H_o L_e)]^2}{L_e^3 [(3 M_o) + (2 H_o L_e)]}$ $p = \frac{0.75 \times [(4 \times (1.1642 \text{ kipft/ft})) + (3 \times (-0.035828 \text{ kip/ft}) \times (4.5 \text{ ft}))]^2}{(4.5 \text{ ft})^3 \times [(3 \times (1.1642 \text{ kipft/ft})) + (2 \times (-0.035828 \text{ kip/ft}) \times (4.5 \text{ ft}))]}$ $p = 0.20345 \text{ kip/ft}^2$ s - Earth pressure against the pile at distance L_e, $s = \frac{6 [(2 M_o) + (H_o L_e)]}{L_e^2}$ $s = \frac{6 \times [(2 \times (1.1642 \text{ kipft/ft})) + ((-0.035828 \text{ kip/ft}) \times (4.5 \text{ ft}))]}{(4.5 \text{ ft})^2}$ $s = 0.64211 \text{ kip/ft}^2$ Check lateral soil pressure capacity: p_a - Allowable lateral soil pressure at depth $a/2$, $p_a = R \frac{a}{2}$ $p_a = (150 \text{ psf/ft}) \times \frac{(3.0317 \text{ ft})}{2}$ $p_a = 0.22738 \text{ kip/ft}^2$ Ratio - Lateral soil capacity $\text{Ratio} = \frac{p}{p_a}$ $\text{Ratio} = \frac{(0.20345 \text{ kip/ft}^2)}{(0.22738 \text{ kip/ft}^2)}$ $\text{Ratio} = 0.89479$ p_s - Allowable lateral soil pressure at depth L_e,	Status: PASS Ratio: 0.890

	$p_s = R L_e$ $p_s = (150 \text{ psf/ft}) \times (4.5 \text{ ft})$ $p_s = 0.675 \text{ kip/ft}^2$ Ratio - Lateral soil capacity $\text{Ratio} = \frac{s}{p_s}$ $\text{Ratio} = \frac{(0.64211 \text{ kip/ft}^2)}{(0.675 \text{ kip/ft}^2)}$ $\text{Ratio} = 0.95127$	Status: PASS Ratio: 0.950
	Considering z-direction: $H_o = 0.014809 \text{ kip/ft}$ - Lateral force per length of pile, $M_o = 0.048726 \text{ kipft/ft}$ - Overturning moment per length of pile, a - Distance from resting surface to pivot point, $a = \frac{(4 M_o L_e) + (3 H_o L_e^2)}{(6 M_o) + (4 H_o L_e)}$ $a = \frac{(4 \times (0.048726 \text{ kipft/ft}) \times (4.5 \text{ ft})) + (3 \times (0.014809 \text{ kip/ft}) \times (4.5 \text{ ft})^2)}{(6 \times (0.048726 \text{ kipft/ft})) + (4 \times (0.014809 \text{ kip/ft}) \times (4.5 \text{ ft}))}$ $a = 3.1788 \text{ ft}$ p - Earth pressure against the pile at distance $a/2$ from resting surface, $p = \frac{0.75 [(4 M_o) + (3 H_o L_e)]^2}{L_e^3 [(3 M_o) + (2 H_o L_e)]}$ $p = \frac{0.75 \times [(4 \times (0.048726 \text{ kipft/ft})) + (3 \times (0.014809 \text{ kip/ft}) \times (4.5 \text{ ft}))]^2}{(4.5 \text{ ft})^3 \times [(3 \times (0.048726 \text{ kipft/ft})) + (2 \times (0.014809 \text{ kip/ft}) \times (4.5 \text{ ft}))]}$ $p = 0.02066 \text{ kip/ft}^2$ s - Earth pressure against the pile at distance L_e, $s = \frac{6 [(2 M_o) + (H_o L_e)]}{L_e^2}$ $s = \frac{6 \times [(2 \times (0.048726 \text{ kipft/ft})) + ((0.014809 \text{ kip/ft}) \times (4.5 \text{ ft}))]}{(4.5 \text{ ft})^2}$ $s = 0.04862 \text{ kip/ft}^2$ Check lateral soil pressure capacity: p_a - Allowable lateral soil pressure at depth $a/2$, $p_a = R \frac{a}{2}$ $p_a = (150 \text{ psf/ft}) \times \frac{(3.1788 \text{ ft})}{2}$ $p_a = 0.23841 \text{ kip/ft}^2$ Ratio - Lateral soil capacity $\text{Ratio} = \frac{p}{p_a}$ $\text{Ratio} = \frac{(0.02066 \text{ kip/ft}^2)}{(0.23841 \text{ kip/ft}^2)}$ $\text{Ratio} = 0.086656$ p_s - Allowable lateral soil pressure at depth L_e, $p_s = R L_e$ $p_s = (150 \text{ psf/ft}) \times (4.5 \text{ ft})$ $p_s = 0.675 \text{ kip/ft}^2$ Ratio - Lateral soil capacity $\text{Ratio} = \frac{s}{p_s}$	Status: PASS Ratio: 0.090

$$Ratio = \frac{(0.04862 \text{ kip/ft}^2)}{(0.675 \text{ kip/ft}^2)}$$

$$Ratio = 0.07203$$

Status: **PASS**
Ratio: **0.070**



Shear force and Bending moment (x-direction, LRFD)

H_o - Lateral force per length of pile,

$$H_o = \frac{V_x}{1.57 D}$$

$$H_o = \frac{(-0.376 \text{ kip})}{1.57 \times (48 \text{ in})}$$

$$H_o = -0.059873 \text{ kip/ft}$$

M_o - Moment per length of pile,

$$M_o = \frac{M_x + (V_x H)}{1.57 D}$$

$$M_o = \frac{(12.67 \text{ kipft}) + ((-0.376 \text{ kip}) \times (0 \text{ ft}))}{1.57 \times (48 \text{ in})}$$

$$M_o = 2.0175 \text{ kipft/ft}$$

E - Distance from lateral load to resisting surface,

$$E = \frac{M_o}{H_o}$$

$$E = \frac{(2.0175 \text{ kipft/ft})}{(-0.059873 \text{ kip/ft})}$$

$$E = 33.697 \text{ ft}$$

a - Distance from resting surface to pivot point,

$$a = \frac{(4 M_o L_e) + (3 H_o L_e^2)}{(6 M_o) + (4 H_o L_e)}$$

$$a = \frac{(4 \times (2.0175 \text{ kipft/ft}) \times (4.5 \text{ ft})) + (3 \times (-0.059873 \text{ kip/ft}) \times (4.5 \text{ ft})^2)}{(6 \times (2.0175 \text{ kipft/ft})) + (4 \times (-0.059873 \text{ kip/ft}) \times (4.5 \text{ ft}))}$$

$$a = 3.0307 \text{ ft}$$

V_{max} - Max shear force located at depth a ,

$$V_{max} = (H_o D) \left[1 - \left[3 \left(\frac{4 E}{L_e} + 3 \right) \left(\frac{a}{L_e} \right)^2 \right] + \left[4 \left(\frac{3 E}{L_e} + 2 \right) \left(\frac{a}{L_e} \right)^3 \right] \right]$$

$$V_{max} = ((-0.059873 \text{ kip/ft}) \times (48 \text{ in})) \times \left[1 - \left[3 \times \left(\frac{4 \times (33.697 \text{ ft})}{(4.5 \text{ ft})} + 3 \right) \times \left(\frac{(3.0307 \text{ ft})}{(4.5 \text{ ft})} \right)^2 \right] + \left[4 \times \left(\frac{3 \times (33.697 \text{ ft})}{(4.5 \text{ ft})} + 2 \right) \times \left(\frac{(3.0307 \text{ ft})}{(4.5 \text{ ft})} \right)^3 \right] \right]$$

$$V_{max} = 3.3401 \text{ kip}$$

M_{max} - Max bending moment located at depth $a/2$,

$$M_{max} = (H_o D L_e) \left[\left(\frac{E}{L_e} + \frac{a}{2 L_e} \right) - \left[\left(\frac{4 E}{L_e} + 3 \right) \left(\frac{a}{2 L_e} \right)^3 \right] + \left[\left(\frac{3 E}{L_e} + 2 \right) \left(\frac{a}{2 L_e} \right)^4 \right] \right]$$

$$M_{max} = ((-0.059873 \text{ kip/ft}) \times (48 \text{ in}) \times (4.5 \text{ ft})) \times \left[\left(\frac{(33.697 \text{ ft})}{(4.5 \text{ ft})} + \frac{(3.0307 \text{ ft})}{2 \times (4.5 \text{ ft})} \right) - \left[\left(\frac{4 \times (33.697 \text{ ft})}{(4.5 \text{ ft})} + 3 \right) \times \left(\frac{(3.0307 \text{ ft})}{2 \times (4.5 \text{ ft})} \right)^3 \right] + \left[\left(\frac{3 \times (33.697 \text{ ft})}{(4.5 \text{ ft})} + 2 \right) \times \left(\frac{(3.0307 \text{ ft})}{2 \times (4.5 \text{ ft})} \right)^4 \right] \right]$$

$$M_{max} = 7.4159 \text{ kipft}$$

Shear force and Bending moment (z-direction, LRFD)

H_o - Lateral force per length of pile,

$$H_o = \frac{V_z}{1.57 b}$$

$$H_o = \frac{(0.146 \text{ kip})}{1.57 \times (48 \text{ in})}$$

$$H_o = 0.023248 \text{ kip/ft}$$

M_o - Moment per length of pile,

$$M_o = \frac{M_x + (V_z H)}{1.57 b}$$

$$M_o = \frac{(0.486 \text{ kipft}) + ((0.146 \text{ kip}) \times (0 \text{ ft}))}{1.57 \times (48 \text{ in})}$$

$$M_o = 0.077389 \text{ kipft/ft}$$

E - Distance from lateral load to resisting surface,

$$E = \frac{M_o}{H_o}$$

$$E = \frac{(0.077389 \text{ kipft/ft})}{(0.023248 \text{ kip/ft})}$$

$$E = 3.3288 \text{ ft}$$

a - Distance from resting surface to pivot point,

$$a = \frac{(4 M_o L_e) + (3 H_o L_e^2)}{(6 M_o) + (4 H_o L_e)}$$

$$a = \frac{(4 \times (0.077389 \text{ kipft/ft}) \times (4.5 \text{ ft})) + (3 \times (0.023248 \text{ kip/ft}) \times (4.5 \text{ ft})^2)}{(6 \times (0.077389 \text{ kipft/ft})) + (4 \times (0.023248 \text{ kip/ft}) \times (4.5 \text{ ft}))}$$

$$a = 3.1778 \text{ ft}$$

V_{max} - Max shear force located at depth a ,

$$V_{max} = (H_o b) \left[1 - \left[3 \left(\frac{4 E}{L_e} + 3 \right) \left(\frac{a}{L_e} \right)^2 \right] + \left[4 \left(\frac{3 E}{L_e} + 2 \right) \left(\frac{a}{L_e} \right)^3 \right] \right]$$

$$V_{max} = ((0.023248 \text{ kip/ft}) \times (48 \text{ in})) \times \left[1 - \left[3 \times \left(\frac{4 \times (3.3288 \text{ ft})}{(4.5 \text{ ft})} + 3 \right) \times \left(\frac{(3.1778 \text{ ft})}{(4.5 \text{ ft})} \right)^2 \right] + \left[4 \times \left(\frac{3 \times (3.3288 \text{ ft})}{(4.5 \text{ ft})} + 2 \right) \times \left(\frac{(3.1778 \text{ ft})}{(4.5 \text{ ft})} \right)^3 \right] \right]$$

$$V_{max} = 0.18334 \text{ kip}$$

M_{max} - Max bending moment located at depth $a/2$,

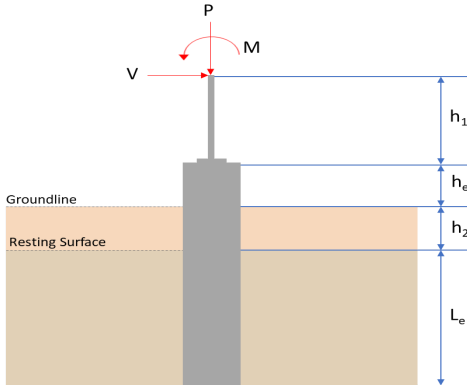
$$M_{max} = (H_o b L_e) \left[\left(\frac{E}{L_e} + \frac{a}{2 L_e} \right) - \left[\left(\frac{4 E}{L_e} + 3 \right) \left(\frac{a}{2 L_e} \right)^3 \right] + \left[\left(\frac{3 E}{L_e} + 2 \right) \left(\frac{a}{2 L_e} \right)^4 \right] \right]$$

$$M_{max} = ((0.023248 \text{ kip/ft}) \times (48 \text{ in}) \times (4.5 \text{ ft})) \times \left[\left(\frac{(3.3288 \text{ ft})}{(4.5 \text{ ft})} + \frac{(3.1778 \text{ ft})}{2 \times (4.5 \text{ ft})} \right) - \left[\left(\frac{4 \times (3.3288 \text{ ft})}{(4.5 \text{ ft})} + 3 \right) \times \left(\frac{(3.1778 \text{ ft})}{2 \times (4.5 \text{ ft})} \right)^3 \right] + \left[\left(\frac{3 \times (3.3288 \text{ ft})}{(4.5 \text{ ft})} + 2 \right) \times \left(\frac{(3.1778 \text{ ft})}{2 \times (4.5 \text{ ft})} \right)^4 \right] \right]$$

		$M_{max} = 0.37499 \text{ kipft}$	
		Minimum Reinforcement Check (LRFD) Parameters: $f'_{ck} = 2.5 \text{ ksi}$ - Concrete strength, $f_{yk} = 60 \text{ ksi}$ - Longitudinal reinforcement strength, $\phi = 0.65$ - Reduction factor for axial strength, $\alpha = 0.8$ - Alpha factor for axial strength, $A_g = 2304 \text{ in}^2$ - Gross area of concrete, Longitudinal reinforcement: Required reinforcement due to axial load, $A_{st,required}$ $A_{st,required}$ $A_{st,required} = \text{Min} \left[\frac{\frac{P}{\phi \alpha} - (0.85 f'_{ck} A_g)}{f_{yk} - (0.85 f'_{ck})}, (0.08 A_g) \right]$ $A_{st,required} = \text{Min} \left[\frac{\frac{(0.926 \text{ kip})}{(0.65) \times (0.8)} - (0.85 \times (2.5 \text{ ksi}) \times (2304 \text{ in}^2))}{(60 \text{ ksi}) - (0.85 \times (2.5 \text{ ksi}))}, (0.08 \times (2304 \text{ in}^2)) \right]$ $A_{st,required} = -84.266 \text{ in}^2$ A_{min} - Governing minimum reinforcement area, $A_{min} = \text{Max} [A_{st,required}, (0.0018 A_g)]$ $A_{min} = \text{Max} [(-84.266 \text{ in}^2), (0.0018 \times (2304 \text{ in}^2))]$ $A_{min} = 4.1472 \text{ in}^2$ n_{rebar} - Required number of reinforcement, $n_{rebar} = \frac{A_{min}}{A_{rebar}}$ $n_{rebar} = \frac{(4.1472 \text{ in}^2)}{(0.3068 \text{ in}^2)}$ $n_{rebar} = 14$ A_{st} - Actual total reinforcement area, $A_{st} = n_{rebar} \frac{\pi d_{bar}^2}{4}$ $A_{st} = (14) \times \frac{\pi \times (0.625 \text{ in})^2}{4}$ $A_{st} = 4.2951 \text{ in}^2$ Ratio - Capacity $\text{Ratio} = \frac{A_{min}}{A_{st}}$ $\text{Ratio} = \frac{(4.1472 \text{ in}^2)}{(4.2951 \text{ in}^2)}$ $\text{Ratio} = 0.96556$ 25.2.3 s_{rebar} - Minimum spacing of reinforcement, $s_{rebar} = \text{Max} [1.5, (1.5 d_{bar})]$ $s_{rebar} = \text{Max} [1.5, (1.5 \times (0.625 \text{ in}))]$ $s_{rebar} = 1.5 \text{ in}$ Ties: 25.7.2.2 Since longitudinal reinforcement is $\leq \text{No. } 10\phi$: Use #3(0.375 in) 25.7.2.1 s_{ties} - Maximum spacing of ties, $s_{ties} = \text{Min} [(16 d_{bar}), (48 d_{ties}), \text{Min}(D, b)]$ $s_{ties} = \text{Min} [(16 \times (0.625 \text{ in})), (48 \times (0.375 \text{ in})), \text{Min}((48 \text{ in}), (48 \text{ in}))]$ $s_{ties} = 10 \text{ in}$ Summary: Main reinforcement: 14 - #5 (0.625 in)	Status: PASS Ratio: 0.970

	Ties: #3(0.375 in) - 10 in	
22.4.2.2	Axial Compression Strength (ACI 318-19, LRFD) ϕP_N - Allowable axial compressive strength $\phi P_N = \phi 0.80 \left[(0.85 f'_{ck} [A_g - A_{st}]) + (f_{yk} A_{st}) \right]$ $\phi P_N = (0.65) \times 0.80 \times \left[(0.85 \times (2.5 \text{ ksi}) \times [(2304 \text{ in}^2) - (4.2951 \text{ in}^2)]) + ((60 \text{ ksi}) \times (4.2951 \text{ in}^2)) \right]$ $\phi P_N = 2675.2 \text{ kip}$ Ratio - Capacity $\text{Ratio} = \frac{P}{\phi P_N}$ $\text{Ratio} = \frac{(9.926 \text{ kip})}{(2675.2 \text{ kip})}$ $\text{Ratio} = 0.0037104$	Status: PASS Ratio: 0.000
22.5.2.2	Shear Strength (ACI 318-19, LRFD) Parameters: $b_w = 48 \text{ in}$ - Effective width, d - Effective depth $d = 0.80 D$ $d = 0.80 \times (48 \text{ in})$ $d = 38.4 \text{ in}$	
22.5.5.1.3	λ_s - size effect modification factor $\lambda_s = MIN \left[\sqrt{\frac{2}{1 + \frac{d}{10}}}, 1 \right]$ $\lambda_s = MIN \left[\sqrt{\frac{2}{1 + \frac{(38.4 \text{ in})}{10}}}, 1 \right]$ $\lambda_s = 0.64282$	
22.5.5.1.1	The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5 \text{ ksi} \rightarrow 2500 \text{ psi}$, $V_{c,max}$ - Max shear strength of concrete $V_{c,max} = 5 \lambda_s \sqrt{f'_{ck}} b_w d$ $V_{c,max} = 5 \times (0.64282) \times \sqrt{(2500 \text{ psi})} \times (48 \text{ in}) \times (38.4 \text{ in})$ $V_{c,max} = 296.21 \text{ kip}$	
22.5.5.1.1(a)	The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5 \text{ ksi} \rightarrow 2500 \text{ psi}$, $P = 9.926 \text{ kip} \rightarrow 9926 \text{ lbf}$, $V_{c,a}$ - Shear strength of concrete (a) $V_{c,a} = \left[2 \lambda_s \sqrt{f'_{ck}} + \frac{P}{6 A_g} \right] b_w d$ $V_{c,a} = \left[2 \times (0.64282) \times \sqrt{(2500 \text{ psi})} + \frac{(9926 \text{ lbf})}{6 \times (2304 \text{ in}^2)} \right] \times (48 \text{ in}) \times (38.4 \text{ in})$ $V_{c,a} = 119.81 \text{ kip}$	
22.5.5.1.2	The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5 \text{ ksi} \rightarrow 2500 \text{ psi}$, $V_{c,b}$ - Shear strength of concrete (b) $V_{c,b} = \left[2 \lambda_s \sqrt{f'_{ck}} + (0.05 f'_{ck}) \right] b_w d$ $V_{c,b} = \left[2 \times (0.64282) \times \sqrt{(2500 \text{ psi})} + (0.05 \times (2500 \text{ psi})) \right] \times (48 \text{ in}) \times (38.4 \text{ in})$ $V_{c,b} = 348.89 \text{ kip}$ V_c - Governing shear strength of concrete $V_c = MIN [V_{c,max}, V_{c,a}, V_{c,b}]$ $V_c = MIN [(296.21 \text{ kip}), (119.81 \text{ kip}), (348.89 \text{ kip})]$ $V_c = 119.81 \text{ kip}$	

14.5.2.1b	$\lambda = 1$ - Concrete modification factor (Normal concrete), Allowable flexural strength: M_n shall be the lesser of: $\phi M_{n,1}$ $\phi M_{n,1} = \phi \times 5 \times \lambda \times \sqrt{f'_c} \times S_m$ $\phi M_{n,1} = 0.65 \times 5 \times 1 \times \sqrt{2.5 \text{ ksi}} \times 18432.001 \text{ in}^3$ $\phi M_{n,1} = 249.600 \text{ kipft}$ $\phi M_{n,2}$ $\phi M_{n,2} = \phi \times 0.85 \times f'_{ck} \times S_m$ $\phi M_{n,2} = (0.65) \times 0.85 \times (2.5 \text{ ksi}) \times (18432 \text{ in}^3)$ $\phi M_{n,2} = 2121.6 \text{ kipft}$ Therefore, ϕM_n - Allowable flexural strength, $\phi M_n = \text{MIN}[\phi M_{n,1}, \phi M_{n,2}]$ $\phi M_n = \text{MIN}[(249.6 \text{ kipft}), (2121.6 \text{ kipft})]$ $\phi M_n = 249.6 \text{ kipft}$ Considering x-direction: $M_{max} = 7.4159 \text{ kipft}$ - Maximum moment in the x-direction, Ratio - Capacity $\text{Ratio} = \frac{M_{max}}{\phi M_n}$ $\text{Ratio} = \frac{(7.4159 \text{ kipft})}{(249.6 \text{ kipft})}$ $\text{Ratio} = 0.029711$	Status: PASS Ratio: 0.030
	Considering z-direction: $M_{max} = 0.37499 \text{ kipft}$ - Maximum moment in the z-direction, Ratio - Capacity $\text{Ratio} = \frac{M_{max}}{\phi M_n}$ $\text{Ratio} = \frac{(0.37499 \text{ kipft})}{(249.6 \text{ kipft})}$ $\text{Ratio} = 0.0015023$	Status: PASS Ratio: 0.000

REFERENCES	CALCULATIONS	RESULTS																										
	SkyCiv Foundation Design Pile Foundation Design Information : Design code : IBC 2021 (International Building Code) Unit System : Imperial																											
	Pile Input  Geometry Pile shape: rectangular b = 48 in - Pile width D = 48 in - Pile depth L = 4.5 ft - Total pile length h1 = 0 ft - Lateral load height from the top of the pile, h2 = 0 ft - Depth to resisting surface he = 0 ft - Length of pile above the ground Tabulation of Soil Parameters <table><tr><th>Layer</th><th>Label</th><th>Allowable Bearing Pressure (qa) (psf)</th><th>Allowable Lateral Pressure (R) (psf/ft)</th></tr><tr><td>1</td><td>Sand, silty sand, clayey sand, silty gravel & clayey gravel</td><td>2000.000</td><td>150.000</td></tr></table> Tabulation of Loads <table><tr><th>Load Component</th><th>ASD</th><th>LRFD</th></tr><tr><td>P (kip)</td><td>6.382</td><td>9.926</td></tr><tr><td>Vx (kip)</td><td>-0.225</td><td>-0.376</td></tr><tr><td>Vz (kip)</td><td>-0.093</td><td>-0.146</td></tr><tr><td>Mx (kipft)</td><td>-0.306</td><td>-0.486</td></tr><tr><td>Mz (kipft)</td><td>7.311</td><td>12.670</td></tr></table> Material Properties f'ck = 2.5 ksi - Concrete strength,	Layer	Label	Allowable Bearing Pressure (qa) (psf)	Allowable Lateral Pressure (R) (psf/ft)	1	Sand, silty sand, clayey sand, silty gravel & clayey gravel	2000.000	150.000	Load Component	ASD	LRFD	P (kip)	6.382	9.926	Vx (kip)	-0.225	-0.376	Vz (kip)	-0.093	-0.146	Mx (kipft)	-0.306	-0.486	Mz (kipft)	7.311	12.670	
Layer	Label	Allowable Bearing Pressure (qa) (psf)	Allowable Lateral Pressure (R) (psf/ft)																									
1	Sand, silty sand, clayey sand, silty gravel & clayey gravel	2000.000	150.000																									
Load Component	ASD	LRFD																										
P (kip)	6.382	9.926																										
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Vz (kip)	-0.093	-0.146																										
Mx (kipft)	-0.306	-0.486																										
Mz (kipft)	7.311	12.670																										
	Required depth to resist lateral loads (ASD) H - Point of application of the lateral load $H = h_1 + h_2 + h_e$ $H = (0 \text{ ft}) + (0 \text{ ft}) + (0 \text{ ft})$ $H = 0 \text{ ft}$ Considering x-direction: Ho - Lateral force per length of pile, $H_o = \frac{V_x}{1.57 D}$ $H_o = \frac{(-0.225 \text{ kip})}{1.57 \times (48 \text{ in})}$ $H_o = -0.035828 \text{ kip/ft}$ Mo - Moment per length of pile, $M_o = \frac{M_z + (V_x H)}{1.57 D}$																											

	$M_o = \frac{(7.311 \text{ kipft}) + ((-0.225 \text{ kip}) \times (0 \text{ ft}))}{1.57 \times (48 \text{ in})}$ $M_o = 1.1642 \text{ kipft/ft}$ Required depth of embedment in earth: $L_x^3 - \left(14.14 \times \frac{H_o \times L_x}{R}\right) - \left(18.85 \times \frac{M_o}{R}\right) = 0$ Solving the cubic equation: $L_{e,x} = 4.3748 \text{ ft}$ - Required depth in x-direction, Considering z-direction: H_o - Lateral force per length of pile, $H_o = \frac{V_z}{1.57 b}$ $H_o = \frac{(-0.093 \text{ kip})}{1.57 \times (48 \text{ in})}$ $H_o = -0.014809 \text{ kip/ft}$ M_o - Moment per length of pile, $M_o = \frac{M_x + (V_z H)}{1.57 b}$ $M_o = \frac{(0.306 \text{ kipft}) + ((-0.093 \text{ kip}) \times (0 \text{ ft}))}{1.57 \times (48 \text{ in})}$ $M_o = 0.048726 \text{ kipft/ft}$ Required depth of embedment in earth: $L_z^3 - \left(14.14 \times \frac{H_o \times L_z}{R}\right) - \left(18.85 \times \frac{M_o}{R}\right) = 0$ Solving the cubic equation: $L_{e,z} = 1.3866 \text{ ft}$ - Required depth in z-direction, Minimum embedded depth required: $L_{e,req}$ - Depth of pile required, $L_{e,req} = \text{MAX}[L_{e,x}, L_{e,z}]$ $L_{e,req} = \text{MAX}[(4.3748 \text{ ft}), (1.3866 \text{ ft})]$ $L_{e,req} = 4.375 \text{ ft}$ L_e - Actual embedded length of pile, $L_e = L - h_c - h_2$ $L_e = (4.5 \text{ ft}) - (0 \text{ ft}) - (0 \text{ ft})$ $L_e = 4.5 \text{ ft}$ Ratio - Embedded depth $\text{Ratio} = \frac{L_{e,req}}{L_e}$ $\text{Ratio} = \frac{(4.375 \text{ ft})}{(4.5 \text{ ft})}$ $\text{Ratio} = 0.97222$	Status: PASS Ratio: 0.970
	End-bearing Capacity (ASD) A - Pile cross-section area $A = b D$ $A = (48 \text{ in}) \times (48 \text{ in})$ $A = 16 \text{ ft}^2$ q - End-bearing pressure $q = \frac{P_o}{A}$ $q = \frac{(6.382 \text{ kip})}{(16 \text{ ft}^2)}$	

$$q = 0.398875 \text{ kip/ft}^2$$

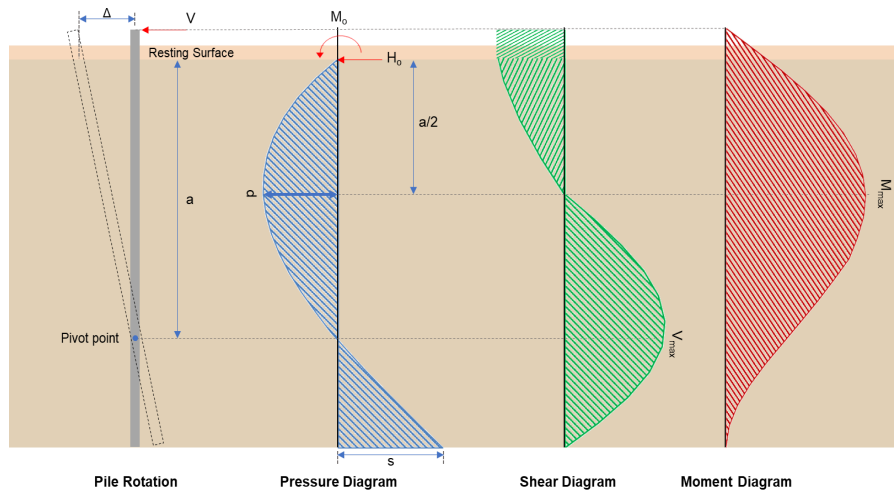
	$q = 0.00000 \text{ kip/ft}$	
	Check bearing capacity ratio: Ratio - Capacity $\text{Ratio} = \frac{q}{q_a}$ $\text{Ratio} = \frac{(0.39888 \text{ kip/ft}^2)}{(2000 \text{ psf})}$ $\text{Ratio} = 0.19944$	Status: PASS Ratio: 0.200
Czerniak	Lateral Soil Pressure (ASD): L/D - Length to least lateral dimension ratio, $L/D = \frac{L}{D}$ $L/D = \frac{(4.5 \text{ ft})}{(48 \text{ in})}$ $L/D = 1.125$ Since $L/D \leq 10$, Pile is short. Considering x-direction: $H_o = -0.035828 \text{ kip/ft}$ - Lateral force per length of pile, $M_o = 1.1642 \text{ kipft/ft}$ - Overturning moment per length of pile, a - Distance from resting surface to pivot point, $a = \frac{(4 M_o L_e) + (3 H_o L_e^2)}{(6 M_o) + (4 H_o L_e)}$ $a = \frac{(4 \times (1.1642 \text{ kipft/ft}) \times (4.5 \text{ ft})) + (3 \times (-0.035828 \text{ kip/ft}) \times (4.5 \text{ ft})^2)}{(6 \times (1.1642 \text{ kipft/ft})) + (4 \times (-0.035828 \text{ kip/ft}) \times (4.5 \text{ ft}))}$ $a = 3.0317 \text{ ft}$ p - Earth pressure against the pile at distance $a/2$ from resting surface, $p = \frac{0.75 [(4 M_o) + (3 H_o L_e)]^2}{L_e^3 [(3 M_o) + (2 H_o L_e)]}$ $p = \frac{0.75 \times [(4 \times (1.1642 \text{ kipft/ft})) + (3 \times (-0.035828 \text{ kip/ft}) \times (4.5 \text{ ft}))]^2}{(4.5 \text{ ft})^3 \times [(3 \times (1.1642 \text{ kipft/ft})) + (2 \times (-0.035828 \text{ kip/ft}) \times (4.5 \text{ ft}))]}$ $p = 0.20345 \text{ kip/ft}^2$ s - Earth pressure against the pile at distance L_e, $s = \frac{6 [(2 M_o) + (H_o L_e)]}{L_e^2}$ $s = \frac{6 \times [(2 \times (1.1642 \text{ kipft/ft})) + ((-0.035828 \text{ kip/ft}) \times (4.5 \text{ ft}))]}{(4.5 \text{ ft})^2}$ $s = 0.64211 \text{ kip/ft}^2$ Check lateral soil pressure capacity: p_a - Allowable lateral soil pressure at depth $a/2$, $p_a = R \frac{a}{2}$ $p_a = (150 \text{ psf/ft}) \times \frac{(3.0317 \text{ ft})}{2}$ $p_a = 0.22738 \text{ kip/ft}^2$ Ratio - Lateral soil capacity $\text{Ratio} = \frac{p}{p_a}$ $\text{Ratio} = \frac{(0.20345 \text{ kip/ft}^2)}{(0.22738 \text{ kip/ft}^2)}$ $\text{Ratio} = 0.89479$ p_s - Allowable lateral soil pressure at depth L_e,	Status: PASS Ratio: 0.890

	$p_s = R L_e$ $p_s = (150 \text{ psf/ft}) \times (4.5 \text{ ft})$ $p_s = 0.675 \text{ kip/ft}^2$ Ratio - Lateral soil capacity $\text{Ratio} = \frac{s}{p_s}$ $\text{Ratio} = \frac{(0.64211 \text{ kip/ft}^2)}{(0.675 \text{ kip/ft}^2)}$ $\text{Ratio} = 0.95127$	Status: PASS Ratio: 0.950
	Considering z-direction: $H_o = -0.014809 \text{ kip/ft}$ - Lateral force per length of pile, $M_o = 0.048726 \text{ kipft/ft}$ - Overturning moment per length of pile, a - Distance from resting surface to pivot point, $a = \frac{(4 M_o L_e) + (3 H_o L_e^2)}{(6 M_o) + (4 H_o L_e)}$ $a = \frac{(4 \times (0.048726 \text{ kipft/ft}) \times (4.5 \text{ ft})) + (3 \times (-0.014809 \text{ kip/ft}) \times (4.5 \text{ ft})^2)}{(6 \times (0.048726 \text{ kipft/ft})) + (4 \times (-0.014809 \text{ kip/ft}) \times (4.5 \text{ ft}))}$ $a = 3.1788 \text{ ft}$ p - Earth pressure against the pile at distance $a/2$ from resting surface, $p = \frac{0.75 [(4 M_o) + (3 H_o L_e)]^2}{L_e^3 [(3 M_o) + (2 H_o L_e)]}$ $p = \frac{0.75 \times [(4 \times (0.048726 \text{ kipft/ft})) + (3 \times (-0.014809 \text{ kip/ft}) \times (4.5 \text{ ft}))]^2}{(4.5 \text{ ft})^3 \times [(3 \times (0.048726 \text{ kipft/ft})) + (2 \times (-0.014809 \text{ kip/ft}) \times (4.5 \text{ ft}))]}$ $p = 0.000072246 \text{ kip/ft}^2$ s - Earth pressure against the pile at distance L_e, $s = \frac{6 [(2 M_o) + (H_o L_e)]}{L_e^2}$ $s = \frac{6 \times [(2 \times (0.048726 \text{ kipft/ft})) + ((-0.014809 \text{ kip/ft}) \times (4.5 \text{ ft}))]}{(4.5 \text{ ft})^2}$ $s = 0.0091295 \text{ kip/ft}^2$ Check lateral soil pressure capacity: p_a - Allowable lateral soil pressure at depth $a/2$, $p_a = R \frac{a}{2}$ $p_a = (150 \text{ psf/ft}) \times \frac{(3.1788 \text{ ft})}{2}$ $p_a = 0.23841 \text{ kip/ft}^2$ Ratio - Lateral soil capacity $\text{Ratio} = \frac{p}{p_a}$ $\text{Ratio} = \frac{(0.000072246 \text{ kip/ft}^2)}{(0.23841 \text{ kip/ft}^2)}$ $\text{Ratio} = 0.00030303$ p_s - Allowable lateral soil pressure at depth L_e, $p_s = R L_e$ $p_s = (150 \text{ psf/ft}) \times (4.5 \text{ ft})$ $p_s = 0.675 \text{ kip/ft}^2$ Ratio - Lateral soil capacity $\text{Ratio} = \frac{s}{p_s}$	Status: PASS Ratio: 0.000

$$Ratio = \frac{(0.0091295 \text{ kip/ft}^2)}{(0.675 \text{ kip/ft}^2)}$$

$$Ratio = 0.013525$$

Status: **PASS**
Ratio: **0.010**



Shear force and Bending moment (x-direction, LRFD)

H_o - Lateral force per length of pile,

$$H_o = \frac{V_x}{1.57 D}$$

$$H_o = \frac{(-0.376 \text{ kip})}{1.57 \times (48 \text{ in})}$$

$$H_o = -0.059873 \text{ kip/ft}$$

M_o - Moment per length of pile,

$$M_o = \frac{M_x + (V_x H)}{1.57 D}$$

$$M_o = \frac{(12.67 \text{ kipft}) + ((-0.376 \text{ kip}) \times (0 \text{ ft}))}{1.57 \times (48 \text{ in})}$$

$$M_o = 2.0175 \text{ kipft/ft}$$

E - Distance from lateral load to resisting surface,

$$E = \frac{M_o}{H_o}$$

$$E = \frac{(2.0175 \text{ kipft/ft})}{(-0.059873 \text{ kip/ft})}$$

$$E = 33.697 \text{ ft}$$

a - Distance from resting surface to pivot point,

$$a = \frac{(4 M_o L_e) + (3 H_o L_e^2)}{(6 M_o) + (4 H_o L_e)}$$

$$a = \frac{(4 \times (2.0175 \text{ kipft/ft}) \times (4.5 \text{ ft})) + (3 \times (-0.059873 \text{ kip/ft}) \times (4.5 \text{ ft})^2)}{(6 \times (2.0175 \text{ kipft/ft})) + (4 \times (-0.059873 \text{ kip/ft}) \times (4.5 \text{ ft}))}$$

$$a = 3.0307 \text{ ft}$$

V_{max} - Max shear force located at depth a ,

$$V_{max} = (H_o D) \left[1 - \left[3 \left(\frac{4 E}{L_e} + 3 \right) \left(\frac{a}{L_e} \right)^2 \right] + \left[4 \left(\frac{3 E}{L_e} + 2 \right) \left(\frac{a}{L_e} \right)^3 \right] \right]$$

$$V_{max} = ((-0.059873 \text{ kip/ft}) \times (48 \text{ in})) \times \left[1 - \left[3 \times \left(\frac{4 \times (33.697 \text{ ft})}{(4.5 \text{ ft})} + 3 \right) \times \left(\frac{(3.0307 \text{ ft})}{(4.5 \text{ ft})} \right)^2 \right] + \left[4 \times \left(\frac{3 \times (33.697 \text{ ft})}{(4.5 \text{ ft})} + 2 \right) \times \left(\frac{(3.0307 \text{ ft})}{(4.5 \text{ ft})} \right)^3 \right] \right]$$

$$V_{max} = 3.3401 \text{ kip}$$

M_{max} - Max bending moment located at depth $a/2$,

$$M_{max} = (H_o D L_e) \left[\left(\frac{E}{L_e} + \frac{a}{2 L_e} \right) - \left[\left(\frac{4 E}{L_e} + 3 \right) \left(\frac{a}{2 L_e} \right)^3 \right] + \left[\left(\frac{3 E}{L_e} + 2 \right) \left(\frac{a}{2 L_e} \right)^4 \right] \right]$$

$$M_{max} = ((-0.059873 \text{ kip/ft}) \times (48 \text{ in}) \times (4.5 \text{ ft})) \times \left[\left(\frac{(33.697 \text{ ft})}{(4.5 \text{ ft})} + \frac{(3.0307 \text{ ft})}{2 \times (4.5 \text{ ft})} \right) - \left[\left(\frac{4 \times (33.697 \text{ ft})}{(4.5 \text{ ft})} + 3 \right) \times \left(\frac{(3.0307 \text{ ft})}{2 \times (4.5 \text{ ft})} \right)^3 \right] + \left[\left(\frac{3 \times (33.697 \text{ ft})}{(4.5 \text{ ft})} + 2 \right) \times \left(\frac{(3.0307 \text{ ft})}{2 \times (4.5 \text{ ft})} \right)^4 \right] \right]$$

$$M_{max} = 7.4159 \text{ kipft}$$

Shear force and Bending moment (z-direction, LRFD)

H_o - Lateral force per length of pile,

$$H_o = \frac{V_z}{1.57 b}$$

$$H_o = \frac{(-0.146 \text{ kip})}{1.57 \times (48 \text{ in})}$$

$$H_o = -0.023248 \text{ kip/ft}$$

M_o - Moment per length of pile,

$$M_o = \frac{M_x + (V_z H)}{1.57 b}$$

$$M_o = \frac{(0.486 \text{ kipft}) + ((-0.146 \text{ kip}) \times (0 \text{ ft}))}{1.57 \times (48 \text{ in})}$$

$$M_o = 0.077389 \text{ kipft/ft}$$

E - Distance from lateral load to resisting surface,

$$E = \frac{M_o}{H_o}$$

$$E = \frac{(0.077389 \text{ kipft/ft})}{(-0.023248 \text{ kip/ft})}$$

$$E = 3.3288 \text{ ft}$$

a - Distance from resting surface to pivot point,

$$a = \frac{(4 M_o L_e) + (3 H_o L_e^2)}{(6 M_o) + (4 H_o L_e)}$$

$$a = \frac{(4 \times (0.077389 \text{ kipft/ft}) \times (4.5 \text{ ft})) + (3 \times (-0.023248 \text{ kip/ft}) \times (4.5 \text{ ft})^2)}{(6 \times (0.077389 \text{ kipft/ft})) + (4 \times (-0.023248 \text{ kip/ft}) \times (4.5 \text{ ft}))}$$

$$a = 3.1778 \text{ ft}$$

V_{max} - Max shear force located at depth a ,

$$V_{max} = (H_o b) \left[1 - \left[3 \left(\frac{4 E}{L_e} + 3 \right) \left(\frac{a}{L_e} \right)^2 \right] + \left[4 \left(\frac{3 E}{L_e} + 2 \right) \left(\frac{a}{L_e} \right)^3 \right] \right]$$

$$V_{max} = ((-0.023248 \text{ kip/ft}) \times (48 \text{ in})) \times \left[1 - \left[3 \times \left(\frac{4 \times (3.3288 \text{ ft})}{(4.5 \text{ ft})} + 3 \right) \times \left(\frac{(3.1778 \text{ ft})}{(4.5 \text{ ft})} \right)^2 \right] + \left[4 \times \left(\frac{3 \times (3.3288 \text{ ft})}{(4.5 \text{ ft})} + 2 \right) \times \left(\frac{(3.1778 \text{ ft})}{(4.5 \text{ ft})} \right)^3 \right] \right]$$

$$V_{max} = 0.18334 \text{ kip}$$

M_{max} - Max bending moment located at depth $a/2$,

$$M_{max} = (H_o b L_e) \left[\left(\frac{E}{L_e} + \frac{a}{2 L_e} \right) - \left[\left(\frac{4 E}{L_e} + 3 \right) \left(\frac{a}{2 L_e} \right)^3 \right] + \left[\left(\frac{3 E}{L_e} + 2 \right) \left(\frac{a}{2 L_e} \right)^4 \right] \right]$$

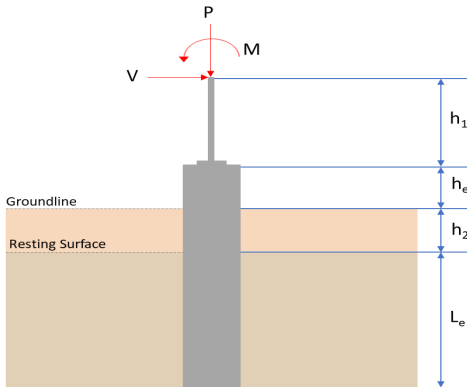
$$M_{max} = ((-0.023248 \text{ kip/ft}) \times (48 \text{ in}) \times (4.5 \text{ ft})) \times \left[\left(\frac{(3.3288 \text{ ft})}{(4.5 \text{ ft})} + \frac{(3.1778 \text{ ft})}{2 \times (4.5 \text{ ft})} \right) - \left[\left(\frac{4 \times (3.3288 \text{ ft})}{(4.5 \text{ ft})} + 3 \right) \times \left(\frac{(3.1778 \text{ ft})}{2 \times (4.5 \text{ ft})} \right)^3 \right] + \left[\left(\frac{3 \times (3.3288 \text{ ft})}{(4.5 \text{ ft})} + 2 \right) \times \left(\frac{(3.1778 \text{ ft})}{2 \times (4.5 \text{ ft})} \right)^4 \right] \right]$$

		$M_{max} = 0.37499 \text{ kipft}$	
		Minimum Reinforcement Check (LRFD) Parameters: $f'_{ck} = 2.5 \text{ ksi}$ - Concrete strength, $f_{yk} = 60 \text{ ksi}$ - Longitudinal reinforcement strength, $\phi = 0.65$ - Reduction factor for axial strength, $\alpha = 0.8$ - Alpha factor for axial strength, $A_g = 2304 \text{ in}^2$ - Gross area of concrete, Longitudinal reinforcement: Required reinforcement due to axial load, $A_{st,required}$ $A_{st,required}$ $A_{st,required} = \text{Min} \left[\frac{\frac{P}{\phi \alpha} - (0.85 f'_{ck} A_g)}{f_{yk} - (0.85 f'_{ck})}, (0.08 A_g) \right]$ $A_{st,required} = \text{Min} \left[\frac{\frac{(0.926 \text{ kip})}{(0.65) \times (0.8)} - (0.85 \times (2.5 \text{ ksi}) \times (2304 \text{ in}^2))}{(60 \text{ ksi}) - (0.85 \times (2.5 \text{ ksi}))}, (0.08 \times (2304 \text{ in}^2)) \right]$ $A_{st,required} = -84.266 \text{ in}^2$ A_{min} - Governing minimum reinforcement area, $A_{min} = \text{Max} [A_{st,required}, (0.0018 A_g)]$ $A_{min} = \text{Max} [(-84.266 \text{ in}^2), (0.0018 \times (2304 \text{ in}^2))]$ $A_{min} = 4.1472 \text{ in}^2$ n_{rebar} - Required number of reinforcement, $n_{rebar} = \frac{A_{min}}{A_{rebar}}$ $n_{rebar} = \frac{(4.1472 \text{ in}^2)}{(0.3068 \text{ in}^2)}$ $n_{rebar} = 14$ A_{st} - Actual total reinforcement area, $A_{st} = n_{rebar} \frac{\pi d_{bar}^2}{4}$ $A_{st} = (14) \times \frac{\pi \times (0.625 \text{ in})^2}{4}$ $A_{st} = 4.2951 \text{ in}^2$ Ratio - Capacity $\text{Ratio} = \frac{A_{min}}{A_{st}}$ $\text{Ratio} = \frac{(4.1472 \text{ in}^2)}{(4.2951 \text{ in}^2)}$ $\text{Ratio} = 0.96556$ 25.2.3 s_{rebar} - Minimum spacing of reinforcement, $s_{rebar} = \text{Max} [1.5, (1.5 d_{bar})]$ $s_{rebar} = \text{Max} [1.5, (1.5 \times (0.625 \text{ in}))]$ $s_{rebar} = 1.5 \text{ in}$ Ties: 25.7.2.2 Since longitudinal reinforcement is $\leq \text{No. } 10\phi$: Use #3(0.375 in) 25.7.2.1 s_{ties} - Maximum spacing of ties, $s_{ties} = \text{Min} [(16 d_{bar}), (48 d_{ties}), \text{Min}(D, b)]$ $s_{ties} = \text{Min} [(16 \times (0.625 \text{ in})), (48 \times (0.375 \text{ in})), \text{Min}((48 \text{ in}), (48 \text{ in}))]$ $s_{ties} = 10 \text{ in}$ Summary: Main reinforcement: 14 - #5 (0.625 in)	Status: PASS Ratio: 0.970

	Ties: #3(0.375 in) - 10 in	
22.4.2.2	Axial Compression Strength (ACI 318-19, LRFD) ϕP_N - Allowable axial compressive strength $\phi P_N = \phi 0.80 \left[(0.85 f'_{ck} [A_g - A_{st}]) + (f_{yk} A_{st}) \right]$ $\phi P_N = (0.65) \times 0.80 \times \left[(0.85 \times (2.5 \text{ ksi}) \times [(2304 \text{ in}^2) - (4.2951 \text{ in}^2)]) + ((60 \text{ ksi}) \times (4.2951 \text{ in}^2)) \right]$ $\phi P_N = 2675.2 \text{ kip}$ Ratio - Capacity $\text{Ratio} = \frac{P}{\phi P_N}$ $\text{Ratio} = \frac{(9.926 \text{ kip})}{(2675.2 \text{ kip})}$ $\text{Ratio} = 0.0037104$	Status: PASS Ratio: 0.000
22.5.2.2	Shear Strength (ACI 318-19, LRFD) Parameters: $b_w = 48 \text{ in}$ - Effective width, d - Effective depth $d = 0.80 D$ $d = 0.80 \times (48 \text{ in})$ $d = 38.4 \text{ in}$	
22.5.5.1.3	λ_s - size effect modification factor $\lambda_s = \text{MIN} \left[\sqrt{\frac{2}{1 + \frac{d}{10}}}, 1 \right]$ $\lambda_s = \text{MIN} \left[\sqrt{\frac{2}{1 + \frac{(38.4 \text{ in})}{10}}}, 1 \right]$ $\lambda_s = 0.64282$	
22.5.5.1.1	The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5 \text{ ksi} \rightarrow 2500 \text{ psi}$, $V_{c,max}$ - Max shear strength of concrete $V_{c,max} = 5 \lambda_s \sqrt{f'_{ck}} b_w d$ $V_{c,max} = 5 \times (0.64282) \times \sqrt{(2500 \text{ psi})} \times (48 \text{ in}) \times (38.4 \text{ in})$ $V_{c,max} = 296.21 \text{ kip}$	
22.5.5.1.1(a)	The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5 \text{ ksi} \rightarrow 2500 \text{ psi}$, $P = 9.926 \text{ kip} \rightarrow 9926 \text{ lbf}$, $V_{c,a}$ - Shear strength of concrete (a) $V_{c,a} = \left[2 \lambda_s \sqrt{f'_{ck}} + \frac{P}{6 A_g} \right] b_w d$ $V_{c,a} = \left[2 \times (0.64282) \times \sqrt{(2500 \text{ psi})} + \frac{(9926 \text{ lbf})}{6 \times (2304 \text{ in}^2)} \right] \times (48 \text{ in}) \times (38.4 \text{ in})$ $V_{c,a} = 119.81 \text{ kip}$	
22.5.5.1.2	The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5 \text{ ksi} \rightarrow 2500 \text{ psi}$, $V_{c,b}$ - Shear strength of concrete (b) $V_{c,b} = \left[2 \lambda_s \sqrt{f'_{ck}} + (0.05 f'_{ck}) \right] b_w d$ $V_{c,b} = \left[2 \times (0.64282) \times \sqrt{(2500 \text{ psi})} + (0.05 \times (2500 \text{ psi})) \right] \times (48 \text{ in}) \times (38.4 \text{ in})$ $V_{c,b} = 348.89 \text{ kip}$ V_c - Governing shear strength of concrete $V_c = \text{Min} [V_{c,max}, V_{c,a}, V_{c,b}]$ $V_c = \text{Min} [(296.21 \text{ kip}), (119.81 \text{ kip}), (348.89 \text{ kip})]$ $V_c = 119.81 \text{ kip}$	

22.5.1.2 22.5.8.5.3 22.5.1.1	The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5 \text{ ksi} \rightarrow 2500 \text{ psi}$, $V_{s,a}$ - Shear strength of steel (a) $V_{s,a} = 8 \sqrt{f'_{ck}} b_w d$ $V_{s,a} = 8 \times \sqrt{(2500 \text{ psi})} \times (48 \text{ in}) \times (38.4 \text{ in})$ $V_{s,a} = 737.28 \text{ kip}$ A_v - Ties rebar area, $A_v = \frac{\pi d_{tes}^2}{4}$ $A_v = \frac{\pi \times (0.375 \text{ in})^2}{4}$ $A_v = 0.11045 \text{ in}^2$ $V_{s,b}$ - Shear strength of steel (b) $V_{s,b} = \frac{2 A_v f_{ysk} d}{s_{ties}}$ $V_{s,b} = \frac{2 \times (0.11045 \text{ in}^2) \times (60 \text{ ksi}) \times (38.4 \text{ in})}{(10 \text{ in})}$ $V_{s,b} = 50.894 \text{ kip}$ V_s - Governing shear strength of steel $V_s = MIN[V_{s,a}, V_{s,b}]$ $V_s = MIN[(737.28 \text{ kip}), (50.894 \text{ kip})]$ $V_s = 50.894 \text{ kip}$ ϕV_n - Allowable shear strength $\phi V_n = \phi (V_c + V_s)$ $\phi V_n = (0.65) \times ((119.81 \text{ kip}) + (50.894 \text{ kip}))$ $\phi V_n = 110.96 \text{ kip}$ Considering x-direction: $V_{max} = 3.3401 \text{ kip}$ - Maximum shear force in the x-direction, $Ratio$ - Capacity $Ratio = \frac{V_{max}}{\phi V_n}$ $Ratio = \frac{(3.3401 \text{ kip})}{(110.96 \text{ kip})}$ $Ratio = 0.030102$ Considering z-direction: $V_{max} = 0.18334 \text{ kip}$ - Maximum shear force in the z-direction, $Ratio$ - Capacity $Ratio = \frac{V_{max}}{\phi V_n}$ $Ratio = \frac{(0.18334 \text{ kip})}{(110.96 \text{ kip})}$ $Ratio = 0.0016524$	Status: PASS Ratio: 0.030 Status: PASS Ratio: 0.000
	Flexural Strength (ACI 318-19, LRFD) S_m - Section modulus $S_m = \frac{b D^3}{6}$ $S_m = \frac{(48 \text{ in}) \times (48 \text{ in})^2}{6}$ $S_m = 18432 \text{ in}^3$	

14.5.2.1b	$\lambda = 1$ - Concrete modification factor (Normal concrete), Allowable flexural strength: M_n shall be the lesser of: $\phi M_{n,1}$ $\phi M_{n,1} = \phi \times 5 \times \lambda \times \sqrt{f'_c} \times S_m$ $\phi M_{n,1} = 0.65 \times 5 \times 1 \times \sqrt{2.5 \text{ ksi}} \times 18432.001 \text{ in}^3$ $\phi M_{n,1} = 249.600 \text{ kipft}$ $\phi M_{n,2}$ $\phi M_{n,2} = \phi \times 0.85 \times f'_c \times S_m$ $\phi M_{n,2} = (0.65) \times 0.85 \times (2.5 \text{ ksi}) \times (18432 \text{ in}^3)$ $\phi M_{n,2} = 2121.6 \text{ kipft}$ Therefore, ϕM_n - Allowable flexural strength, $\phi M_n = \text{MIN}[\phi M_{n,1}, \phi M_{n,2}]$ $\phi M_n = \text{MIN}[(249.6 \text{ kipft}), (2121.6 \text{ kipft})]$ $\phi M_n = 249.6 \text{ kipft}$ Considering x-direction: $M_{max} = 7.4159 \text{ kipft}$ - Maximum moment in the x-direction, Ratio - Capacity $\text{Ratio} = \frac{M_{max}}{\phi M_n}$ $\text{Ratio} = \frac{(7.4159 \text{ kipft})}{(249.6 \text{ kipft})}$ $\text{Ratio} = 0.029711$	Status: PASS Ratio: 0.030
	Considering z-direction: $M_{max} = 0.37499 \text{ kipft}$ - Maximum moment in the z-direction, Ratio - Capacity $\text{Ratio} = \frac{M_{max}}{\phi M_n}$ $\text{Ratio} = \frac{(0.37499 \text{ kipft})}{(249.6 \text{ kipft})}$ $\text{Ratio} = 0.0015023$	Status: PASS Ratio: 0.000

REFERENCES	CALCULATIONS	RESULTS																										
	SkyCiv Foundation Design Pile Foundation Design Information : Design code : IBC 2021 (International Building Code) Unit System : Imperial																											
	Pile Input  Geometry Pile shape: rectangular b = 48 in - Pile width D = 48 in - Pile depth L = 4.75 ft - Total pile length h1 = 0 ft - Lateral load height from the top of the pile, h2 = 0 ft - Depth to resisting surface he = 0 ft - Length of pile above the ground Tabulation of Soil Parameters <table><tr><th>Layer</th><th>Label</th><th>Allowable Bearing Pressure (qa) (psf)</th><th>Allowable Lateral Pressure (R) (psf/ft)</th></tr><tr><td>1</td><td>Sand, silty sand, clayey sand, silty gravel & clayey gravel</td><td>2000.000</td><td>150.000</td></tr></table> Tabulation of Loads <table><tr><th>Load Component</th><th>ASD</th><th>LRFD</th></tr><tr><td>P (kip)</td><td>7.488</td><td>11.674</td></tr><tr><td>Vx (kip)</td><td>-0.256</td><td>-0.428</td></tr><tr><td>Vz (kip)</td><td>0.000</td><td>0.000</td></tr><tr><td>Mx (kipft)</td><td>0.000</td><td>0.000</td></tr><tr><td>Mz (kipft)</td><td>7.739</td><td>13.384</td></tr></table> Material Properties f'ck = 2.5 ksi - Concrete strength,	Layer	Label	Allowable Bearing Pressure (qa) (psf)	Allowable Lateral Pressure (R) (psf/ft)	1	Sand, silty sand, clayey sand, silty gravel & clayey gravel	2000.000	150.000	Load Component	ASD	LRFD	P (kip)	7.488	11.674	Vx (kip)	-0.256	-0.428	Vz (kip)	0.000	0.000	Mx (kipft)	0.000	0.000	Mz (kipft)	7.739	13.384	
Layer	Label	Allowable Bearing Pressure (qa) (psf)	Allowable Lateral Pressure (R) (psf/ft)																									
1	Sand, silty sand, clayey sand, silty gravel & clayey gravel	2000.000	150.000																									
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P (kip)	7.488	11.674																										
Vx (kip)	-0.256	-0.428																										
Vz (kip)	0.000	0.000																										
Mx (kipft)	0.000	0.000																										
Mz (kipft)	7.739	13.384																										
	Required depth to resist lateral loads (ASD) H - Point of application of the lateral load $H = h_1 + h_2 + h_e$ $H = (0 \text{ ft}) + (0 \text{ ft}) + (0 \text{ ft})$ $H = 0 \text{ ft}$ Considering x-direction: H_o - Lateral force per length of pile, $H_o = \frac{V_x}{1.57 D}$ $H_o = \frac{(-0.256 \text{ kip})}{1.57 \times (48 \text{ in})}$ $H_o = -0.040764 \text{ kip/ft}$ M_o - Moment per length of pile, $M_o = \frac{M_z + (V_x H)}{1.57 D}$																											

	$M_o = \frac{(7.739 \text{ kipft}) + ((-0.256 \text{ kip}) \times (0 \text{ ft}))}{1.57 \times (48 \text{ in})}$ $M_o = 1.2323 \text{ kipft/ft}$ Required depth of embedment in earth: $L_x^3 - \left(14.14 \times \frac{H_o \times L_x}{R}\right) - \left(18.85 \times \frac{M_o}{R}\right) = 0$ Solving the cubic equation: $L_{e,x} = 4.4432 \text{ ft}$ - Required depth in x-direction, Considering z-direction: $L_{e,z} = 0 \text{ ft}$ - Required depth in z-direction, Minimum embedded depth required: $L_{e,req}$ - Depth of pile required, $L_{e,req} = \text{MAX}[L_{e,x}, L_{e,z}]$ $L_{e,req} = \text{MAX}[(4.4432 \text{ ft}), (0 \text{ ft})]$ $L_{e,req} = 4.443 \text{ ft}$ L_e - Actual embedded length of pile, $L_e = L - h_e - h_2$ $L_e = (4.75 \text{ ft}) - (0 \text{ ft}) - (0 \text{ ft})$ $L_e = 4.75 \text{ ft}$ <i>Ratio</i> - Embedded depth $\text{Ratio} = \frac{L_{e,req}}{L_e}$ $\text{Ratio} = \frac{(4.443 \text{ ft})}{(4.75 \text{ ft})}$ $\text{Ratio} = 0.93537$	Status: PASS Ratio: 0.940
	End-bearing Capacity (ASD) A - Pile cross-section area $A = b \ D$ $A = (48 \text{ in}) \times (48 \text{ in})$ $A = 16 \text{ ft}^2$ q - End-bearing pressure $q = \frac{P_v}{A}$ $q = \frac{(7.488 \text{ kip})}{(16 \text{ ft}^2)}$ $q = 0.468 \text{ kip/ft}^2$ Check bearing capacity ratio: <i>Ratio</i> - Capacity $\text{Ratio} = \frac{q}{q_a}$ $\text{Ratio} = \frac{(0.468 \text{ kip/ft}^2)}{(2000 \text{ psf})}$ $\text{Ratio} = 0.234$	Status: PASS Ratio: 0.230
Czerniak	Lateral Soil Pressure (ASD): L/D - Length to least lateral dimension ratio, $L/D = \frac{L}{D}$ $L/D = \frac{(4.75 \text{ ft})}{(48 \text{ in})}$	

$$L/D = 1.1875$$

Since $L/D \leq 10$,

Pile is short.

Considering x-direction:

$H_o = -0.040764$ kip/ft - Lateral force per length of pile,

$M_o = 1.2323$ kipft/ft - Overturning moment per length of pile,

a - Distance from resting surface to pivot point,

$$a = \frac{(4 M_o L_e) + (3 H_o L_e^2)}{(6 M_o) + (4 H_o L_e)}$$

$$a = \frac{(4 \times (1.2323 \text{ kipft/ft}) \times (4.75 \text{ ft})) + (3 \times (-0.040764 \text{ kip/ft}) \times (4.75 \text{ ft})^2)}{(6 \times (1.2323 \text{ kipft/ft})) + (4 \times (-0.040764 \text{ kip/ft}) \times (4.75 \text{ ft}))}$$

$$a = 3.2042 \text{ ft}$$

p - Earth pressure against the pile at distance $a/2$ from resting surface,

$$p = \frac{0.75 [(4 M_o) + (3 H_o L_e)]^2}{L_e^3 [(3 M_o) + (2 H_o L_e)]}$$

$$p = \frac{0.75 \times [(4 \times (1.2323 \text{ kipft/ft})) + (3 \times (-0.040764 \text{ kip/ft}) \times (4.75 \text{ ft}))]^2}{(4.75 \text{ ft})^3 \times [(3 \times (1.2323 \text{ kipft/ft})) + (2 \times (-0.040764 \text{ kip/ft}) \times (4.75 \text{ ft}))]}$$

$$p = 0.18991 \text{ kip/ft}^2$$

s - Earth pressure against the pile at distance L_e ,

$$s = \frac{6 [(2 M_o) + (H_o L_e)]}{L_e^2}$$

$$s = \frac{6 \times [(2 \times (1.2323 \text{ kipft/ft})) + ((-0.040764 \text{ kip/ft}) \times (4.75 \text{ ft}))]}{(4.75 \text{ ft})^2}$$

$$s = 0.60393 \text{ kip/ft}^2$$

Check lateral soil pressure capacity:

p_a - Allowable lateral soil pressure at depth $a/2$,

$$p_a = R \frac{a}{2}$$

$$p_a = (150 \text{ psf/ft}) \times \frac{(3.2042 \text{ ft})}{2}$$

$$p_a = 0.24031 \text{ kip/ft}^2$$

Ratio - Lateral soil capacity

$$\text{Ratio} = \frac{p}{p_a}$$

$$\text{Ratio} = \frac{(0.18991 \text{ kip/ft}^2)}{(0.24031 \text{ kip/ft}^2)}$$

$$\text{Ratio} = 0.79025$$

p_s - Allowable lateral soil pressure at depth L_e ,

$$p_s = R L_e$$

$$p_s = (150 \text{ psf/ft}) \times (4.75 \text{ ft})$$

$$p_s = 0.7125 \text{ kip/ft}^2$$

Ratio - Lateral soil capacity

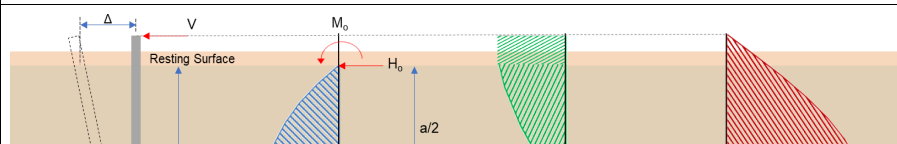
$$\text{Ratio} = \frac{s}{p_s}$$

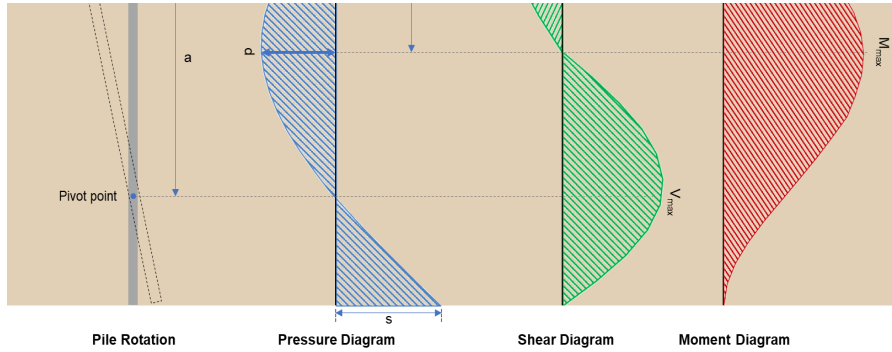
$$\text{Ratio} = \frac{(0.60393 \text{ kip/ft}^2)}{(0.7125 \text{ kip/ft}^2)}$$

$$\text{Ratio} = 0.84762$$

Status: **PASS**
Ratio: **0.790**

Status: **PASS**
Ratio: **0.850**





Shear force and Bending moment (x-direction, LRFD)

H_o - Lateral force per length of pile,

$$H_o = \frac{V_x}{1.57 D}$$

$$H_o = \frac{(-0.428 \text{ kip})}{1.57 \times (48 \text{ in})}$$

$$H_o = -0.068153 \text{ kip/ft}$$

M_o - Moment per length of pile,

$$M_o = \frac{M_x + (V_x H)}{1.57 D}$$

$$M_o = \frac{(13.384 \text{ kipft}) + ((-0.428 \text{ kip}) \times (0 \text{ ft}))}{1.57 \times (48 \text{ in})}$$

$$M_o = 2.1312 \text{ kipft/ft}$$

E - Distance from lateral load to resisting surface,

$$E = \frac{M_o}{H_o}$$

$$E = \frac{(2.1312 \text{ kipft/ft})}{(-0.068153 \text{ kip/ft})}$$

$$E = 31.271 \text{ ft}$$

a - Distance from resting surface to pivot point,

$$a = \frac{(4 M_o L_e) + (3 H_o L_e^2)}{(6 M_o) + (4 H_o L_e)}$$

$$a = \frac{(4 \times (2.1312 \text{ kipft/ft}) \times (4.75 \text{ ft})) + (3 \times (-0.068153 \text{ kip/ft}) \times (4.75 \text{ ft})^2)}{(6 \times (2.1312 \text{ kipft/ft})) + (4 \times (-0.068153 \text{ kip/ft}) \times (4.75 \text{ ft}))}$$

$$a = 3.2031 \text{ ft}$$

V_{max} - Max shear force located at depth a ,

$$V_{max} = (H_o D) \left[1 - \left[3 \left(\frac{4E}{L_e} + 3 \right) \left(\frac{a}{L_e} \right)^2 \right] + \left[4 \left(\frac{3E}{L_e} + 2 \right) \left(\frac{a}{L_e} \right)^3 \right] \right]$$

$$V_{max} = ((-0.068153 \text{ kip/ft}) \times (48 \text{ in})) \times \left[1 - \left[3 \times \left(\frac{4 \times (31.271 \text{ ft})}{(4.75 \text{ ft})} + 3 \right) \times \left(\frac{(3.2031 \text{ ft})}{(4.75 \text{ ft})} \right)^2 \right] + \left[4 \times \left(\frac{3 \times (31.271 \text{ ft})}{(4.75 \text{ ft})} + 2 \right) \times \left(\frac{(3.2031 \text{ ft})}{(4.75 \text{ ft})} \right)^3 \right] \right]$$

$$V_{max} = 3.3636 \text{ kip}$$

M_{max} - Max bending moment located at depth $a/2$,

$$M_{max} = (H_o D L_e) \left[\left(\frac{E}{L_e} + \frac{a}{2 L_e} \right) - \left[\left(\frac{4E}{L_e} + 3 \right) \left(\frac{a}{2 L_e} \right)^3 \right] + \left[\left(\frac{3E}{L_e} + 2 \right) \left(\frac{a}{2 L_e} \right)^4 \right] \right]$$

$$M_{max} = ((-0.068153 \text{ kip/ft}) \times (48 \text{ in}) \times (4.75 \text{ ft})) \times \left[\left(\frac{(31.271 \text{ ft})}{(4.75 \text{ ft})} + \frac{(3.2031 \text{ ft})}{2 \times (4.75 \text{ ft})} \right) - \left[\left(\frac{4 \times (31.271 \text{ ft})}{(4.75 \text{ ft})} + 3 \right) \times \left(\frac{(3.2031 \text{ ft})}{2 \times (4.75 \text{ ft})} \right)^3 \right] + \left[\left(\frac{3 \times (31.271 \text{ ft})}{(4.75 \text{ ft})} + 2 \right) \times \left(\frac{(3.2031 \text{ ft})}{2 \times (4.75 \text{ ft})} \right)^4 \right] \right]$$

		$M_{max} = 7.8695 \text{ kipft}$	
		Minimum Reinforcement Check (LRFD) Parameters: $f'_{ck} = 2.5 \text{ ksi}$ - Concrete strength, $f_{yk} = 60 \text{ ksi}$ - Longitudinal reinforcement strength, $\phi = 0.65$ - Reduction factor for axial strength, $\alpha = 0.8$ - Alpha factor for axial strength, $A_g = 2304 \text{ in}^2$ - Gross area of concrete, Longitudinal reinforcement: Required reinforcement due to axial load, $A_{st,required}$ $A_{st,required}$ $A_{st,required} = \text{Min} \left[\frac{\frac{P}{\phi \alpha} - (0.85 f'_{ck} A_g)}{f_{yk} - (0.85 f'_{ck})}, (0.08 A_g) \right]$ $A_{st,required} = \text{Min} \left[\frac{\frac{(11.674 \text{ kip})}{(0.65) \times (0.8)} - (0.85 \times (2.5 \text{ ksi}) \times (2304 \text{ in}^2))}{(60 \text{ ksi}) - (0.85 \times (2.5 \text{ ksi}))}, (0.08 \times (2304 \text{ in}^2)) \right]$ $A_{st,required} = -84.208 \text{ in}^2$ A_{min} - Governing minimum reinforcement area, $A_{min} = \text{Max} [A_{st,required}, (0.0018 A_g)]$ $A_{min} = \text{Max} [(-84.208 \text{ in}^2), (0.0018 \times (2304 \text{ in}^2))]$ $A_{min} = 4.1472 \text{ in}^2$ n_{rebar} - Required number of reinforcement, $n_{rebar} = \frac{A_{min}}{A_{rebar}}$ $n_{rebar} = \frac{(4.1472 \text{ in}^2)}{(0.3068 \text{ in}^2)}$ $n_{rebar} = 14$ A_{st} - Actual total reinforcement area, $A_{st} = n_{rebar} \frac{\pi d_{bar}^2}{4}$ $A_{st} = (14) \times \frac{\pi \times (0.625 \text{ in})^2}{4}$ $A_{st} = 4.2951 \text{ in}^2$ Ratio - Capacity $\text{Ratio} = \frac{A_{min}}{A_{st}}$ $\text{Ratio} = \frac{(4.1472 \text{ in}^2)}{(4.2951 \text{ in}^2)}$ $\text{Ratio} = 0.96556$ 25.2.3 s_{rebar} - Minimum spacing of reinforcement, $s_{rebar} = \text{Max} [1.5, (1.5 d_{bar})]$ $s_{rebar} = \text{Max} [1.5, (1.5 \times (0.625 \text{ in}))]$ $s_{rebar} = 1.5 \text{ in}$ Ties: 25.7.2.2 Since longitudinal reinforcement is $\leq \text{No. } 10\phi$: Use #3(0.375 in) 25.7.2.1 s_{ties} - Maximum spacing of ties, $s_{ties} = \text{Min} [(16 d_{bar}), (48 d_{ties}), \text{Min}(D, b)]$ $s_{ties} = \text{Min} [(16 \times (0.625 \text{ in})), (48 \times (0.375 \text{ in})), \text{Min}((48 \text{ in}), (48 \text{ in}))]$ $s_{ties} = 10 \text{ in}$ Summary: Main reinforcement: 14 - #5 (0.625 in)	
			Status: PASS Ratio: 0.970

	Ties: #3(0.375 in) - 10 in	
22.4.2.2	Axial Compression Strength (ACI 318-19, LRFD) ϕP_N - Allowable axial compressive strength $\phi P_N = \phi 0.80 [(0.85 f'_{ck} [A_g - A_{st}]) + (f_{yk} A_{st})]$ $\phi P_N = (0.65) \times 0.80 \times [(0.85 \times (2.5 \text{ ksi}) \times [(2304 \text{ in}^2) - (4.2951 \text{ in}^2)]) + ((60 \text{ ksi}) \times (4.2951 \text{ in}^2))]$ $\phi P_N = 2675.2 \text{ kip}$ Ratio - Capacity $\text{Ratio} = \frac{P}{\phi P_N}$ $\text{Ratio} = \frac{(11.674 \text{ kip})}{(2675.2 \text{ kip})}$ $\text{Ratio} = 0.0043638$	Status: PASS Ratio: 0.000
22.5.2.2	Shear Strength (ACI 318-19, LRFD) Parameters: $b_w = 48 \text{ in}$ - Effective width, d - Effective depth $d = 0.80 D$ $d = 0.80 \times (48 \text{ in})$ $d = 38.4 \text{ in}$	
22.5.5.1.3	λ_s - size effect modification factor $\lambda_s = \text{MIN} \left[\sqrt{\frac{2}{1 + \frac{d}{10}}}, 1 \right]$ $\lambda_s = \text{MIN} \left[\sqrt{\frac{2}{1 + \frac{(38.4 \text{ in})}{10}}}, 1 \right]$ $\lambda_s = 0.64282$	
22.5.5.1.1	The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5 \text{ ksi} \rightarrow 2500 \text{ psi}$, $V_{c,max}$ - Max shear strength of concrete $V_{c,max} = 5 \lambda_s \sqrt{f'_{ck}} b_w d$ $V_{c,max} = 5 \times (0.64282) \times \sqrt{(2500 \text{ psi})} \times (48 \text{ in}) \times (38.4 \text{ in})$ $V_{c,max} = 296.21 \text{ kip}$	
22.5.5.1.1(a)	The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5 \text{ ksi} \rightarrow 2500 \text{ psi}$, $P = 11.674 \text{ kip} \rightarrow 11674 \text{ lbf}$, $V_{c,a}$ - Shear strength of concrete (a) $V_{c,a} = \left[2 \lambda_s \sqrt{f'_{ck}} + \frac{P}{6 A_g} \right] b_w d$ $V_{c,a} = \left[2 \times (0.64282) \times \sqrt{(2500 \text{ psi})} + \frac{(11674 \text{ lbf})}{6 \times (2304 \text{ in}^2)} \right] \times (48 \text{ in}) \times (38.4 \text{ in})$ $V_{c,a} = 120.04 \text{ kip}$	
22.5.5.1.2	The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5 \text{ ksi} \rightarrow 2500 \text{ psi}$, $V_{c,b}$ - Shear strength of concrete (b) $V_{c,b} = \left[2 \lambda_s \sqrt{f'_{ck}} + (0.05 f'_{ck}) \right] b_w d$ $V_{c,b} = \left[2 \times (0.64282) \times \sqrt{(2500 \text{ psi})} + (0.05 \times (2500 \text{ psi})) \right] \times (48 \text{ in}) \times (38.4 \text{ in})$ $V_{c,b} = 348.89 \text{ kip}$ V_c - Governing shear strength of concrete $V_c = \text{Min} [V_{c,max}, V_{c,a}, V_{c,b}]$ $V_c = \text{Min} [(296.21 \text{ kip}), (120.04 \text{ kip}), (348.89 \text{ kip})]$ $V_c = 120.04 \text{ kip}$	

22.5.1.2	The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5 \text{ ksi} \rightarrow 2500 \text{ psi}$, $V_{s,a}$ - Shear strength of steel (a) $V_{s,a} = 8 \sqrt{f'_{ck}} b_w d$ $V_{s,a} = 8 \times \sqrt{(2500 \text{ psi})} \times (48 \text{ in}) \times (38.4 \text{ in})$ $V_{s,a} = 737.28 \text{ kip}$ A_v - Ties rebar area, $A_v = \frac{\pi d_{ties}^2}{4}$ $A_v = \frac{\pi \times (0.375 \text{ in})^2}{4}$ $A_v = 0.11045 \text{ in}^2$ 22.5.8.5.3 $V_{s,b}$ - Shear strength of steel (b) $V_{s,b} = \frac{2 A_v f_{ywk} d}{s_{ties}}$ $V_{s,b} = \frac{2 \times (0.11045 \text{ in}^2) \times (60 \text{ ksi}) \times (38.4 \text{ in})}{(10 \text{ in})}$ $V_{s,b} = 50.894 \text{ kip}$ V_s - Governing shear strength of steel $V_s = MIN[V_{s,a}, V_{s,b}]$ $V_s = MIN[(737.28 \text{ kip}), (50.894 \text{ kip})]$ $V_s = 50.894 \text{ kip}$ 22.5.1.1 ϕV_n - Allowable shear strength $\phi V_n = \phi (V_c + V_s)$ $\phi V_n = (0.65) \times ((120.04 \text{ kip}) + (50.894 \text{ kip}))$ $\phi V_n = 111.11 \text{ kip}$ Considering x-direction: $V_{max} = 3.3636 \text{ kip}$ - Maximum shear force in the x-direction, $Ratio$ - Capacity $Ratio = \frac{V_{max}}{\phi V_n}$ $Ratio = \frac{(3.3636 \text{ kip})}{(111.11 \text{ kip})}$ $Ratio = 0.030273$	Status: PASS Ratio: 0.030
14.5.2.1b	Flexural Strength (ACI 318-19, LRFD) S_m - Section modulus $S_m = \frac{b D^2}{6}$ $S_m = \frac{(48 \text{ in}) \times (48 \text{ in})^2}{6}$ $S_m = 18432 \text{ in}^3$ $\lambda = 1$ - Concrete modification factor (Normal concrete), Allowable flexural strength: M_n shall be the lesser of: $\phi M_{n,1}$ $\phi M_{n,1} = \phi \times 5 \times \lambda \times \sqrt{f'_c} \times S_m$ $\phi M_{n,1} = 0.65 \times 5 \times 1 \times \sqrt{(2.5 \text{ ksi})} \times 18432.001 \text{ in}^3$ $\phi M_{n,1} = 249.600 \text{ kip ft}$ $\phi M_{n,2}$ $\phi M_{n,2} = 0.85 f'_c S_m$	

	$\phi M_{n,2} = (0.65) \times 0.85 \times (2.5 \text{ ksi}) \times (18432 \text{ in}^3)$ $\phi M_{n,2} = 2121.6 \text{ kipft}$ Therefore, ϕM_n - Allowable flexural strength, $\phi M_n = \text{MIN}[\phi M_{n,1}, \phi M_{n,2}]$ $\phi M_n = \text{MIN}[(249.6 \text{ kipft}), (2121.6 \text{ kipft})]$ $\phi M_n = 249.6 \text{ kipft}$ Considering x-direction: $M_{max} = 7.8695 \text{ kipft}$ - Maximum moment in the x-direction, <i>Ratio</i> - Capacity $\text{Ratio} = \frac{M_{max}}{\phi M_n}$ $\text{Ratio} = \frac{(7.8695 \text{ kipft})}{(249.6 \text{ kipft})}$ $\text{Ratio} = 0.031529$	
		Status: PASS Ratio: 0.030