Your Project Calculations

Project Name: MTSOLAR_KA9EG1H0IKFA

S3D Model Link:
https://platform.skyciv.com/structural?preload_name=MTSOLAR_KA9EG1H0IKFA&preload_path=Shared%20Enterprise%20Folder/MT_Solar_Projects/9_2023

Public Model Link:
https://platform.skyciv.com/structural-viewer?project_id=zUzXASp24sm1t06nPuQmgnOiV7TY604UHvv3aq51KHgJi11xDOo6qaTZLJkTnvJS

Array Specification

Product:	Beam
Unique ID:	2P-19.75-6TOP-XD-45-L-5Hx6W-G8K2
Duty Classification:	XD
Module Width:	41.00 in
Module Length:	69.00in
Number of Rows:	5
Number of Columns:	6
Total Number of Modules:	30
Desired Tilt Angle:	25
Front Edge Clearance:	5
Total Array Height at Tilt:	12.26 ft
Total Frame Length:	34.75 ft
Frame Weight:	1707 lbs
Array Dimensions N/S:	17.29 ft
Array Dimensions E/W:	35.00 ft
Rail Length:	207.50 in
Rail Spacing:	2.88 ft
Rail Check:	Not Checked

Support Specifications

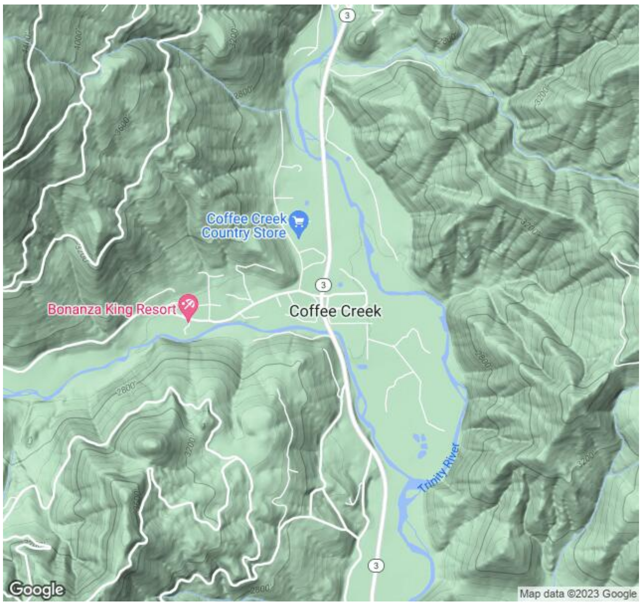
Pole Size:	6in Pipe Sch 40
Pole Length above Grade:	8.65 ft
Number of Poles:	2
Pole Spacing:	19.75 ft

Foundation Specifications

Foundation Type:	Square
Foundation Dimensions:	48 x 48 in
Foundation Depth (below grade):	Pile 1: 5.50 ft Pile 2: 5.50 ft
Foundation Volume:	6.519 y^3
Foundation Result:	PASSED
Mount Twist:	0.130972 kip

Site Info

Risk Category:	I
Exposure:	B
Soil Classification:	sand
Site Location:	CA-3, Callahan, CA 96014, USA
Wind Speed:	100 mph
Snow Load:	40 psf
Design Uplift Pressure:	Multiple pressures
Design Downforce Pressure:	Multiple pressures
Design Snow Pressure:	0.019793 ksf



Design Disclaimer

This software should be used for preliminary designs and should not be used as a final design unless reviewed, verified and designed by a qualified structural engineer.

AutoDesigner Input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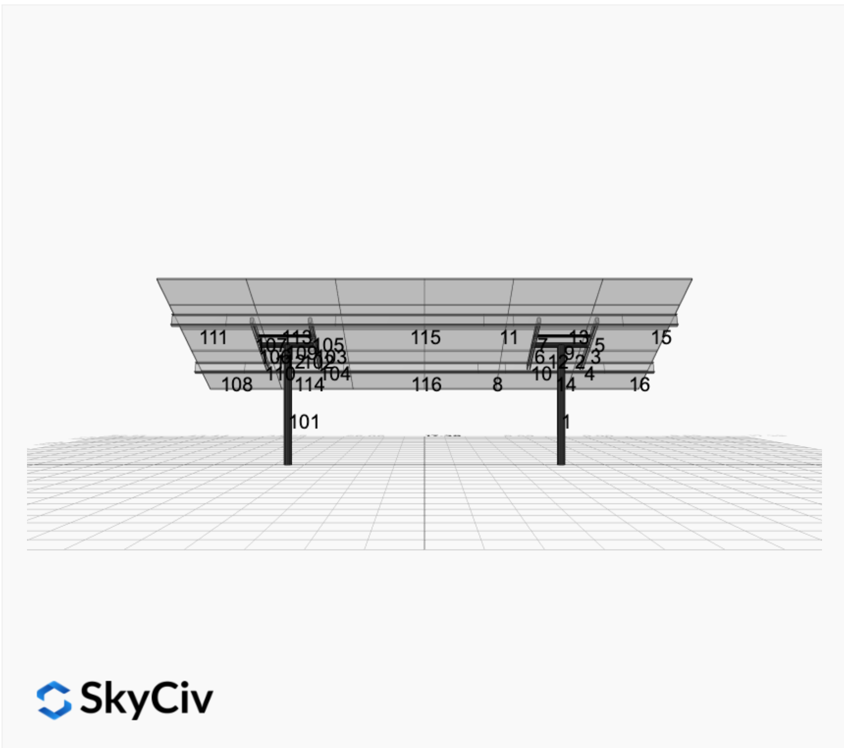
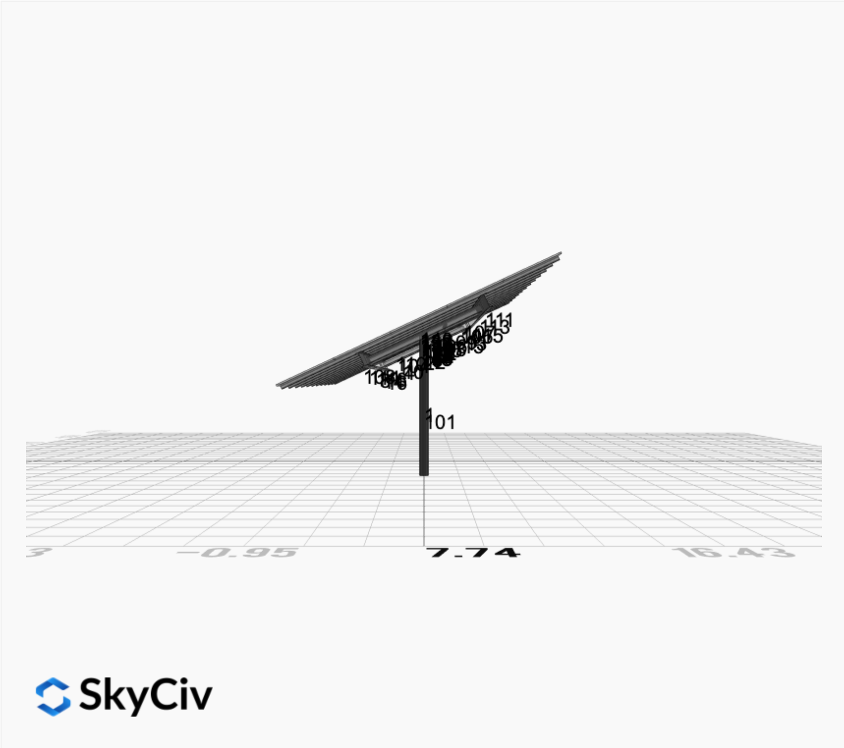
Design Notes:

- AISC Deflection checks are set to L/1 due to structure design intent
- Foundation Design and Sizing is approximate only

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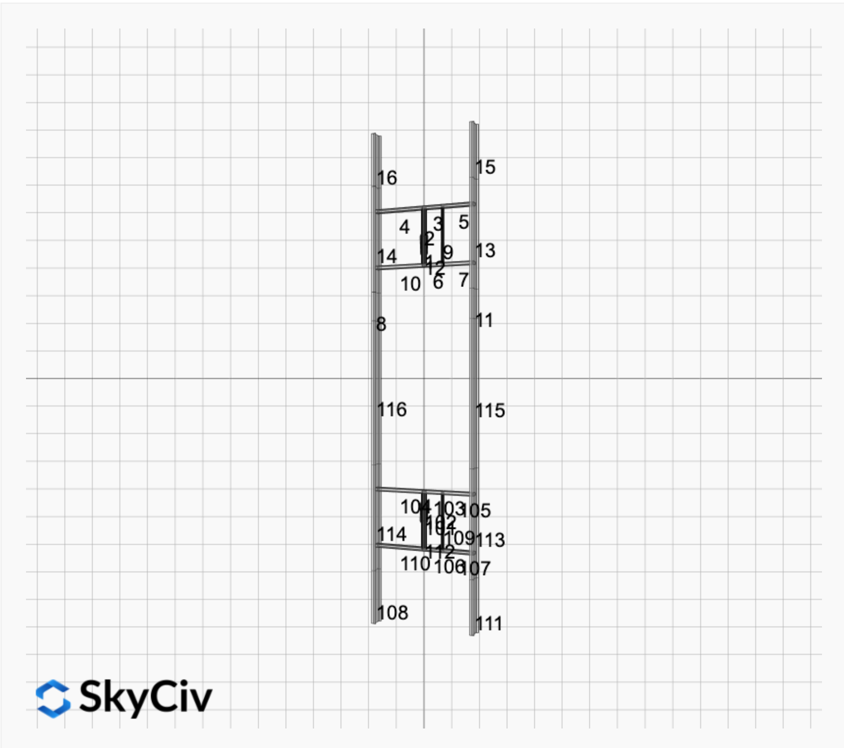
16.43
SkyCiv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15
4
3
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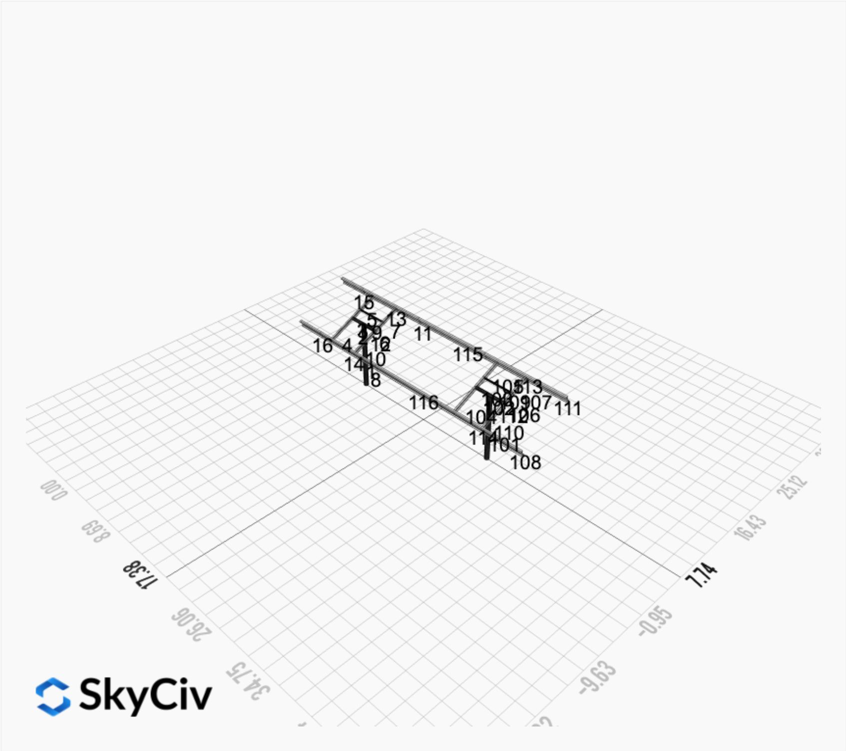
111
SkyCiv



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116
111
108
0.00
8.69
17.38
26.06
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25.12
16.43
7.74
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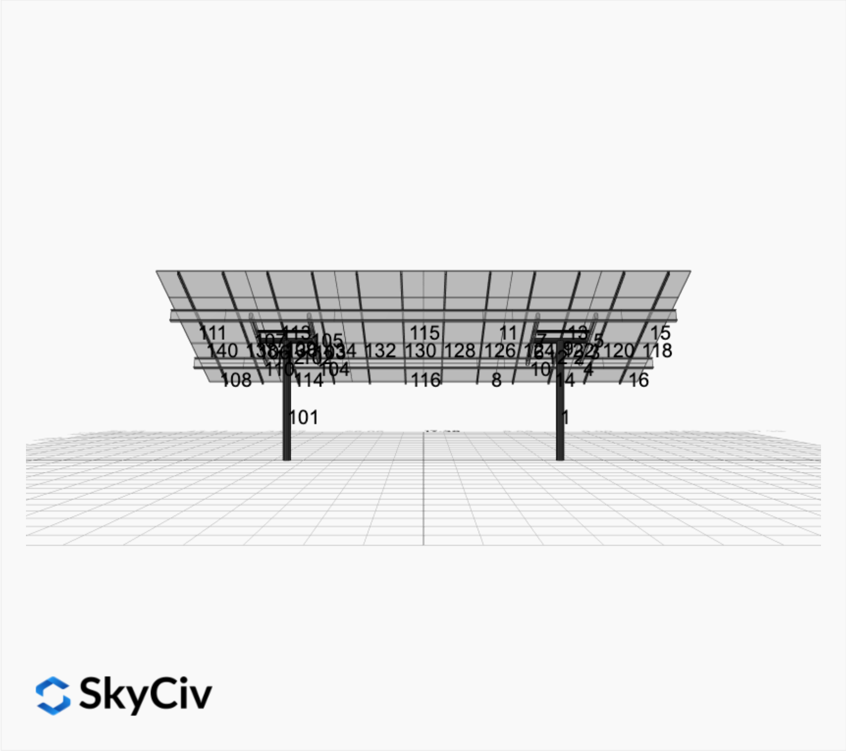
-9.63
SkyCiv



115
116
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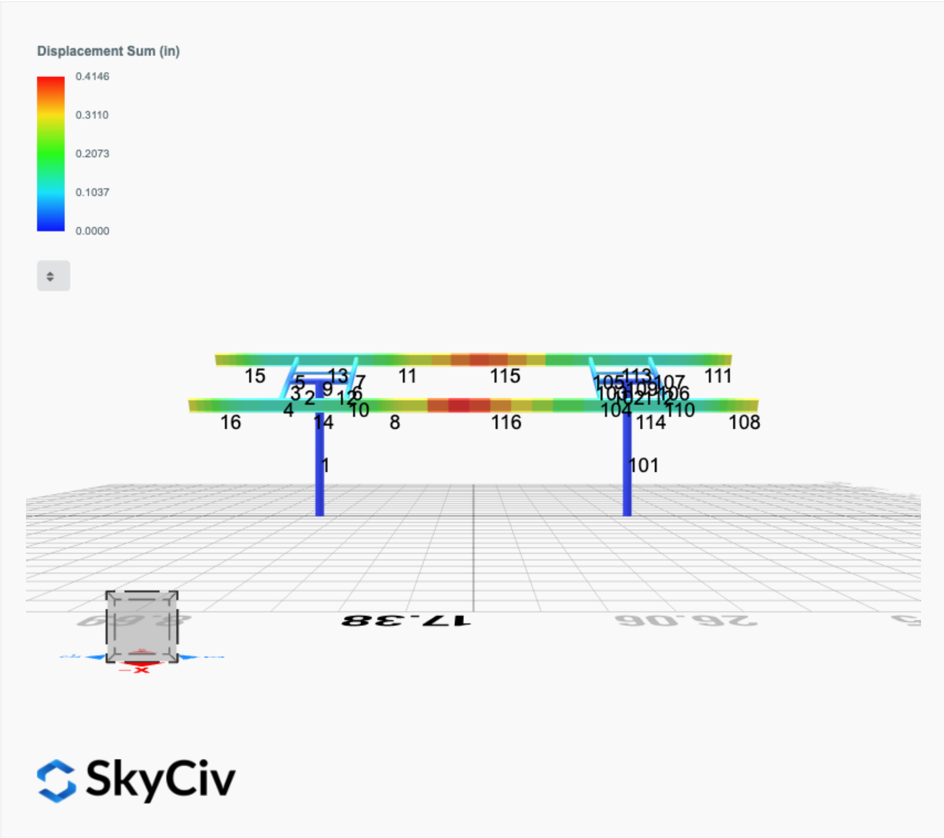
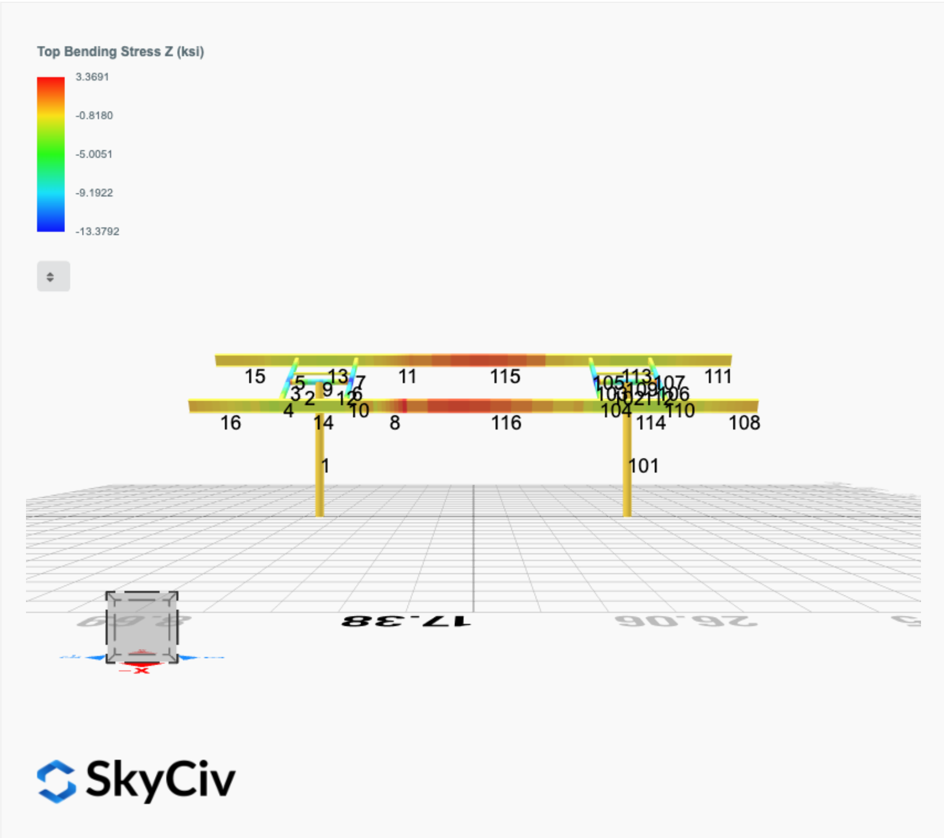
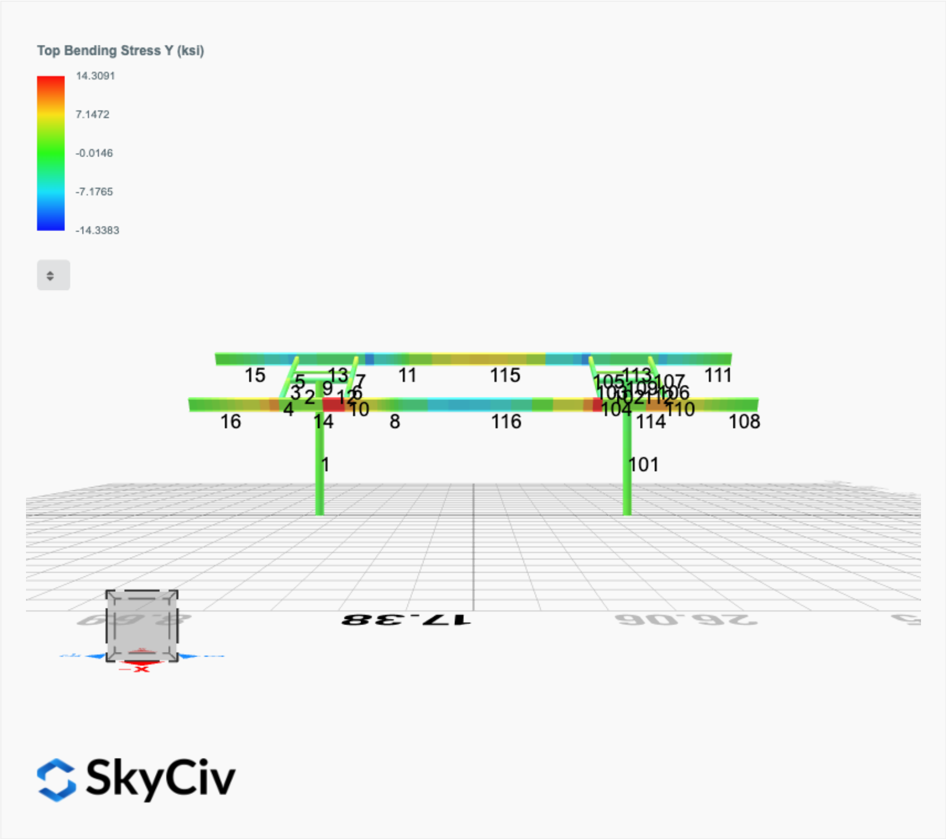
130
128
101
108
SkyCiv

FEM Results (Envelope Worst Case for each member)



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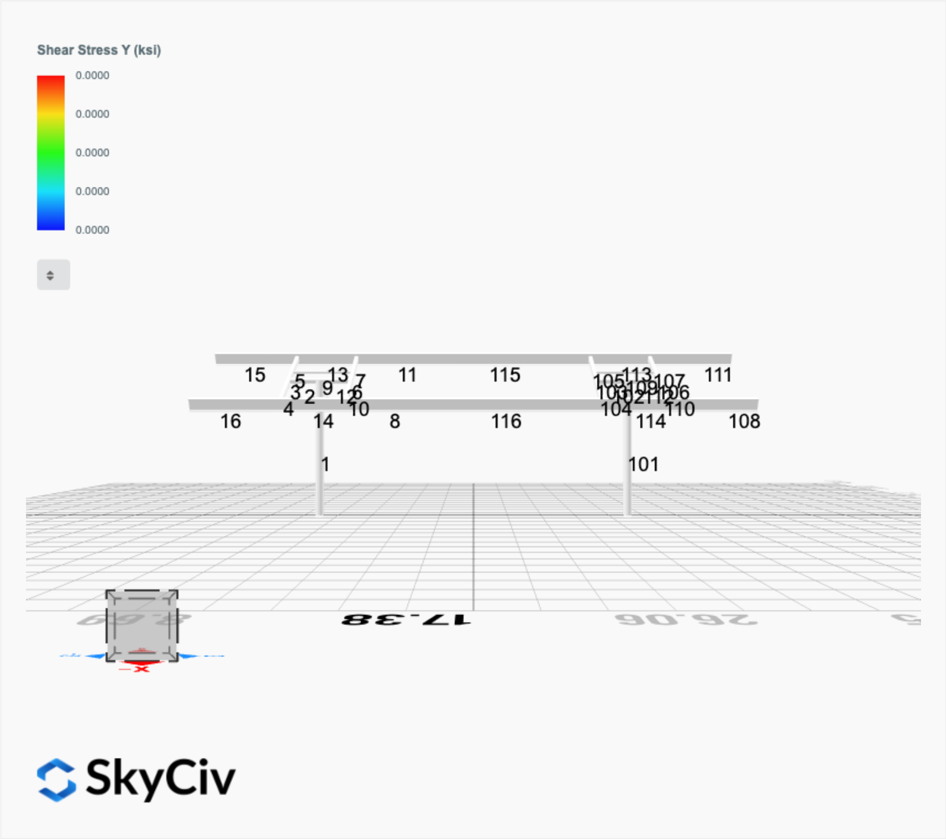
14.3091
7.1472
-0.0146
-7.1765
-14.3383
15
5
13
7
11
115
105
113
107
111
3
2
9
12
6
4
14
10
16
8
116
104
114
110
108
1
101
17.38
SkyCiv


Shear Stress Y (ksi)
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0.0000
0.0000
0.0000
0.0000
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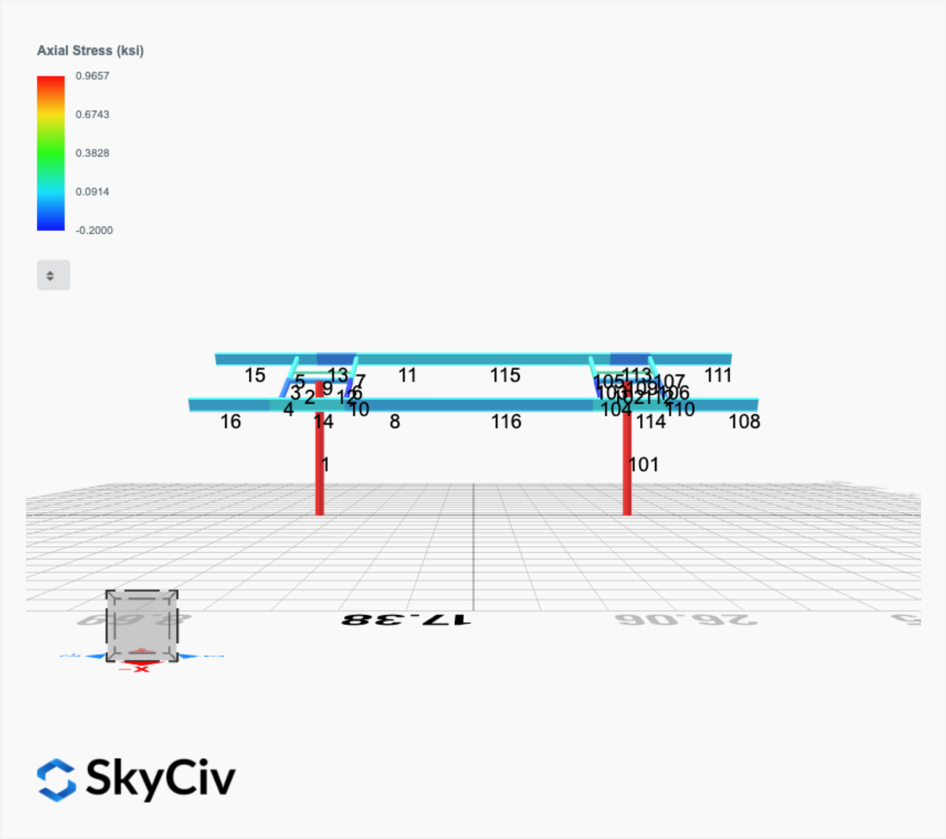
5
13
7
11
115
105
113
107
111
3
2
9
12
6
4
14
10
16
8
116
104
114
110
108
1
101
17.38
SkyCiv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0.0914
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13
7
11
115
111
16
14
8
116
108
1
101
17.38
SkyCiv

Reaction Forces for Foundation 1 (Node ID#1), (kip, kip-ft)

ASD Load Combination Results

Name	Fx	Fy	Fz	Mx	My	Mz
ULS: 1. D	-0.0000	2.2440	0.0314	0.0830	-0.0052	0.0289
ULS: 2. D + L	-0.0000	2.2440	0.0314	0.0830	-0.0052	0.0289
ULS: 3. D + (S or Lr or R)	-0.0001	7.6338	0.1279	0.3320	-0.0259	0.0221
ULS: 3. D + (S or Lr or R)	-0.0000	2.2440	0.0314	0.0830	-0.0052	0.0289
ULS: 4. D + 0.75L + 0.75(S or Lr or R)	-0.0001	6.2864	0.1037	0.2697	-0.0207	0.0238
ULS: 4. D + 0.75L + 0.75(S or Lr or R)	-0.0000	2.2440	0.0314	0.0830	-0.0052	0.0289
ULS: 5b. D + 0.7E	-0.0000	2.2440	0.0314	0.0830	-0.0052	0.0289
ULS: 6b. D + 0.75L + 0.75(0.7)E + 0.75S	-0.0001	6.2864	0.1037	0.2697	-0.0207	0.0238
ULS: 8. 0.6D + 0.7E	-0.0000	1.3464	0.0189	0.0498	-0.0031	0.0173
ULS: 5a. D + 0.6W_Wind downforce Case A only	-1.5421	5.5511	0.0915	0.2348	-0.0715	13.9588
ULS: 5a. D + 0.6W_Wind downforce Case B only	-1.5421	5.5511	0.0915	0.2348	-0.0715	13.9588
ULS: 5a. D + 0.6W_Wind uplift Case A only	1.3494	-0.6498	-0.0219	-0.0560	0.0484	-11.1683
ULS: 5a. D + 0.6W_Wind uplift Case B only	1.1566	-0.2363	-0.0159	-0.0443	0.0403	-17.1663
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case A only	-1.1567	8.7667	0.1488	0.3836	-0.0704	10.4713
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case B only	-1.1567	8.7667	0.1488	0.3836	-0.0704	10.4713
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case A only	1.0119	4.1160	0.0637	0.1655	0.0195	-8.3741
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case B only	0.8673	4.4261	0.0683	0.1743	0.0134	-12.8726
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case A only	-1.1566	4.7244	0.0765	0.1968	-0.0549	10.4763
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case B only	-1.1566	4.7244	0.0765	0.1968	-0.0549	10.4763
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case A only	1.0120	0.0737	-0.0086	-0.0212	0.0350	-8.3690
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case B only	0.8674	0.3838	-0.0040	-0.0125	0.0290	-12.8675
ULS: 7. 0.6D + 0.6W_Wind downforce Case A only	-1.5421	4.6535	0.0789	0.2016	-0.0694	13.9473
ULS: 7. 0.6D + 0.6W_Wind downforce Case B only	-1.5421	4.6535	0.0789	0.2016	-0.0694	13.9473
ULS: 7. 0.6D + 0.6W_Wind uplift Case A only	1.3494	-1.5474	-0.0345	-0.0892	0.0505	-11.1799
ULS: 7. 0.6D + 0.6W_Wind uplift Case B only	1.1566	-1.1339	-0.0284	-0.0775	0.0424	-17.1779

Worst Case Reactions LRFD

These calculations are taken directly from the FEA via SkyCiv and are used in the Concrete Checks of the Foundatino Module. Note: Worst case values are assumed as downforce wind load cases.

Result	Value (kip, kip-ft)
Axial	14.0737
Shear X	-2.5705
Shear Z	0.2680
Moment X	0.6602
Moment Y (Twist)	0.1404
Moment Z	29.4417

Worst Case Reactions ASD

These results are taken from the worst case values in the above table and are used in the Soil Checks in the Foundation Module. Note: Worst case values are assumed as downforce wind load cases.

Result	Value (kip, kip-ft)
Axial	8.7667
Shear X	-1.5421
Shear Z	0.1488
Moment X	0.3836
Moment Y (Twist)	0.0715
Moment Z	17.1779

Reaction Forces for Foundation 2 (Node ID#101), (kip, kip-ft)

ASD Load Combination Results

Name	Fx	Fy	Fz	Mx	My	Mz
ULS: 1. D	0.0000	2.2440	-0.0314	-0.0831	0.0051	0.0293
ULS: 2. D + L	0.0000	2.2440	-0.0314	-0.0831	0.0051	0.0293
ULS: 3. D + (S or Lr or R)	0.0001	7.6335	-0.1279	-0.3354	0.0229	0.0269
ULS: 3. D + (S or Lr or R)	0.0000	2.2440	-0.0314	-0.0831	0.0051	0.0293
ULS: 4. D + 0.75L + 0.75(S or Lr or R)	0.0001	6.2861	-0.1037	-0.2723	0.0185	0.0275
ULS: 4. D + 0.75L + 0.75(S or Lr or R)	0.0000	2.2440	-0.0314	-0.0831	0.0051	0.0293
ULS: 5b. D + 0.7E	0.0000	2.2440	-0.0314	-0.0831	0.0051	0.0293

Name	Fx	Fy	Fz	Mx	My	Mz
ULS: 6b. D + 0.75L + 0.75(0.7)E + 0.75S	0.0001	6.2861	-0.1037	-0.2723	0.0185	0.0275
ULS: 8. 0.6D + 0.7E	0.0000	1.3464	-0.0189	-0.0498	0.0030	0.0176
ULS: 5a. D + 0.6W_Wind downforce Case A only	-1.5421	5.5511	-0.0915	-0.2348	0.0715	13.9590
ULS: 5a. D + 0.6W_Wind downforce Case B only	-1.5421	5.5511	-0.0915	-0.2348	0.0715	13.9590
ULS: 5a. D + 0.6W_Wind uplift Case A only	1.3494	-0.6498	0.0219	0.0559	-0.0485	-11.1679
ULS: 5a. D + 0.6W_Wind uplift Case B only	1.1566	-0.2363	0.0159	0.0441	-0.0405	-17.1655
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case A only	-1.1565	8.7664	-0.1488	-0.3862	0.0683	10.4748
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case B only	-1.1565	8.7664	-0.1488	-0.3862	0.0683	10.4748
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case A only	1.0121	4.1158	-0.0637	-0.1681	-0.0217	-8.3704
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case B only	0.8676	4.4259	-0.0683	-0.1770	-0.0157	-12.8686
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case A only	-1.1566	4.7243	-0.0765	-0.1969	0.0549	10.4766
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind downforce Case B only	-1.1566	4.7243	-0.0765	-0.1969	0.0549	10.4766
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case A only	1.0120	0.0737	0.0086	0.0211	-0.0351	-8.3686
ULS: 6a. D + 0.75L + 0.75(0.6)W + 0.75(S or Lr or R)_Wind uplift Case B only	0.8675	0.3838	0.0040	0.0123	-0.0291	-12.8668
ULS: 7. 0.6D + 0.6W_Wind downforce Case A only	-1.5421	4.6535	-0.0789	-0.2016	0.0694	13.9473
ULS: 7. 0.6D + 0.6W_Wind downforce Case B only	-1.5421	4.6535	-0.0789	-0.2016	0.0694	13.9473
ULS: 7. 0.6D + 0.6W_Wind uplift Case A only	1.3494	-1.5474	0.0345	0.0891	-0.0505	-11.1796
ULS: 7. 0.6D + 0.6W_Wind uplift Case B only	1.1566	-1.1339	0.0284	0.0773	-0.0425	-17.1772

Worst Case Reactions LRFD

These calculations are taken directly from the FEA via SkyCiv and are used in the Concrete Checks of the Foundatino Module. Note: Worst case values are assumed as downforce wind load cases.

Result	Value (kip, kip-ft)
Axial	14.0706
Shear X	-2.5702
Shear Z	-0.2680
Moment X	-0.6926
Moment Y (Twist)	0.1310
Moment Z	29.4406

Worst Case Reactions ASD

These results are taken from the worst case values in the above table and are used in the Soil Checks in the Foundation Module. Note: Worst case values are assumed as downforce wind load cases.

Result	Value (kip, kip-ft)
Axial	8.7664
Shear X	-1.5421
Shear Z	-0.1488
Moment X	-0.3862
Moment Y (Twist)	0.0715
Moment Z	17.1772

Project Details

Design Code: AISC 360-16 LRFD
Provision: LRFD
Country: United States

User Name: sales@mtsolar.us
Unit System: imperial

Design Input Information

Design Factors			
Φ_t	Φ_c	Φ_b	Φ_v
0.9	0.9	0.9	0.9

Design Materials			
ID	E (ksi)	F_y (ksi)	F_u (ksi)
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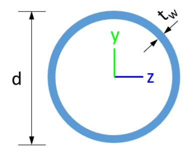
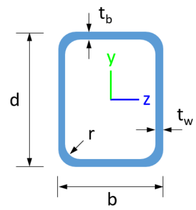
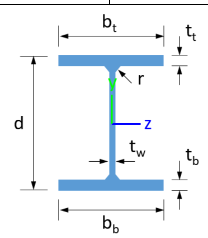
Section Dimensions



ID	Name	d (in)	t_w (in)					
3	2in Pipe Sch 120	2.38	0.25					
6	4in Pipe Sch 120	4.50	0.44					
7	6in Pipe Sch 40	6.63	0.28					



ID	Name	d (in)	b (in)	t_w (in)	t_b (in)	r (in)		
17	HSS5x3x1/4	5.00	3.00	0.23	0.23	0.23		



ID	Name	d (in)	t_w (in)	b_t (in)	b_b (in)	t_t (in)	t_b (in)	r (in)
20	W10x12	9.87	0.19	3.96	3.96	0.21	0.21	0.30

Section Properties								
ID	Name	A (in^2)	J (in^4)	I_{yp} (in^4)	I_{zp} (in^4)	I_w (in^6)	S_{yp} (in^3)	S_{zp} (in^3)
3	2in Pipe Sch 120	1.67	1.91	0.96	0.96	0.00	1.13	1.13
6	4in Pipe Sch 120	5.58	23.29	11.64	11.64	0.00	7.24	7.24
7	6in Pipe Sch 40	5.58	56.28	28.14	28.14	0.00	11.28	11.28

17	HSS5x3x1/4	3.37	11.00	4.81	10.70	62.42	3.77	5.38
20	W10x12	3.54	0.05	2.18	53.80	50.90	1.74	12.60

Member Properties								
Member ID	Section ID	K_zL (ft)	K_yL (ft)	L_b(ft)	C_b	LST	LSC	LD
1	7	18.17	18.17	8.65	-	300	200	1
2	6	1.30	1.30	2.00	-	300	200	1
3	17	0.92	0.92	1.42	1.19,1.18,1.19,1.18,1.18,1.19,1.18,1.18,1.15,1.17,1.18,1.18,1.17,1.17,1.18,1.18,1.18,1.18,1.18,1.18,1.14,1.17,1.18,1.18,1.17,1.17	300	200	1
4	17	2.44	2.44	3.75	1.69,1.68,1.69,1.67,1.68,1.69,1.67,1.67,1.62,1.68,1.67,1.67,1.65,1.72,1.67,1.67,1.67,1.67,1.68,1.68,1.60,1.70,1.67,1.67,1.66,1.76	300	200	1
5	17	1.52	1.52	2.33	1.68,1.68,1.68,1.67,1.68,1.68,1.67,1.67,1.63,1.66,1.67,1.67,1.66,1.66,1.67,1.67,1.68,1.68,1.67,1.67,1.62,1.65,1.67,1.67,1.66,1.66	300	200	1
6	17	0.92	0.92	1.42	1.19,1.18,1.19,1.18,1.19,1.19,1.18,1.18,1.15,1.17,1.18,1.18,1.17,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.14,1.17,1.18,1.18,1.17,1.18	300	200	1
7	17	1.52	1.52	2.33	1.68,1.68,1.68,1.68,1.68,1.68,1.67,1.67,1.64,1.66,1.67,1.67,1.66,1.66,1.67,1.67,1.68,1.68,1.67,1.67,1.62,1.65,1.67,1.67,1.66,1.66	300	200	1
8	20	1.33	1.33	2.05	1.89,2.12,1.84,2.19,2.00,1.76,1.49,1.49,2.21,2.25,1.29,1.29,1.07,2.28,2.17,2.17,2.21,2.23,1.41,1.41,2.11,2.22,1.32,1.32,1.11,2.26	300	200	1
9	3	2.60	2.60	4.00	-	300	200	1
10	17	2.44	2.44	3.75	1.69,1.67,1.69,1.67,1.68,1.69,1.67,1.67,1.62,1.68,1.67,1.67,1.65,1.72,1.67,1.67,1.67,1.67,1.67,1.67,1.60,1.70,1.67,1.67,1.66,1.79	300	200	1
11	20	1.33	1.33	2.05	1.43,1.53,1.44,2.12,1.44,1.46,1.33,1.33,2.23,2.21,1.01,1.01,1.53,1.76,1.66,1.66,2.17,2.22,1.02,1.02,2.15,2.14,1.11,1.11,1.16,1.27	300	200	1
12	6	1.30	1.30	2.00	-	300	200	1
13	20	4.88	4.00	7.50	1.13,1.13,1.13,1.12,1.13,1.13,1.13,1.13,2.83,2.13,1.13,1.13,1.13,1.14,1.12,1.12,1.18,1.98,1.13,1.13,1.25,1.26,1.13,1.13,1.13,1.14	300	200	1
14	20	4.88	4.00	7.50	1.13,1.15,1.13,1.49,1.13,1.13,1.13,1.13,2.32,2.82,1.14,1.14,1.13,3.85,1.17,1.17,1.83,2.21,1.13,1.13,1.14,2.24,1.14,1.14,1.13,4.33	300	200	1
15	20	7.88	7.88	3.75	2.16,2.07,2.18,2.12,2.13,2.22,2.12,2.12,2.30,2.35,1.75,1.75,2.05,2.22,2.29,2.29,2.41,2.32,1.77,1.77,2.42,2.44,1.92,1.92,1.62,1.60	300	200	1
16	20	7.88	7.88	3.75	2.46,2.43,2.47,2.37,2.45,2.44,1.98,1.98,2.34,2.29,2.07,2.07,1.56,2.28,2.43,2.43,2.34,2.31,2.15,2.15,2.46,2.32,2.12,2.12,1.91,2.27	300	200	1
101	7	18.17	18.17	8.65	-	300	200	1
102	6	1.30	1.30	2.00	-	300	200	1
103	17	0.92	0.92	1.42	1.19,1.18,1.19,1.18,1.19,1.19,1.18,1.18,1.15,1.17,1.18,1.18,1.17,1.18,1.18,1.18,1.18,1.18,1.18,1.18,1.14,1.17,1.18,1.18,1.17,1.18	300	200	1
104	17	2.44	2.44	3.75	1.69,1.68,1.69,1.67,1.68,1.69,1.67,1.67,1.62,1.68,1.67,1.67,1.65,1.72,1.67,1.67,1.67,1.67,1.67,1.67,1.60,1.70,1.67,1.67,1.66,1.79	300	200	1
105	17	1.52	1.52	2.33	1.68,1.67,1.68,1.67,1.68,1.68,1.67,1.67,1.63,1.66,1.67,1.67,1.66,1.66,1.67,1.67,1.67,1.67,1.67,1.67,1.62,1.65,1.67,1.67,1.66,1.66	300	200	1
106	17	0.92	0.92	1.42	1.19,1.18,1.19,1.18,1.18,1.19,1.18,1.18,1.15,1.17,1.18,1.18,1.17,1.17,1.18,1.18,1.18,1.18,1.18,1.18,1.14,1.17,1.18,1.18,1.17,1.17	300	200	1
107	17	1.52	1.52	2.33	1.68,1.68,1.68,1.67,1.68,1.68,1.67,1.67,1.63,1.66,1.67,1.67,1.66,1.66,1.67,1.67,1.68,1.68,1.67,1.67,1.62,1.65,1.67,1.67,1.66,1.66	300	200	1

108	20	7.88	7.88	3.75	2.46,2.43,2.47,2.37,2.45,2.44,1.98,1.98,2.34,2.29,2.07,2.07,1.56,2.28,2.43,2.43,2.34,2.31,2.15,2.15,2.46,2.32,2.12,2.12,1.91,2.27	300	200	1
109	3	2.60	2.60	4.00	-	300	200	1
110	17	2.44	2.44	3.75	1.69,1.68,1.69,1.67,1.68,1.69,1.67,1.67,1.62,1.68,1.67,1.67,1.65,1.72,1.67,1.67,1.67,1.68,1.68,1.60,1.70,1.67,1.67,1.66,1.76	300	200	1
111	20	7.88	7.88	3.75	2.16,2.07,2.18,2.11,2.13,2.22,2.11,2.11,2.30,2.35,1.75,1.75,2.05,2.22,2.30,2.30,2.41,2.32,1.77,1.77,2.42,2.44,1.92,1.92,1.62,1.60	300	200	1
112	6	1.30	1.30	2.00	-	300	200	1
113	20	4.88	4.00	7.50	1.13,1.13,1.13,1.13,1.13,1.13,1.13,1.13,2.85,2.16,1.13,1.13,1.13,1.14,1.12,1.12,1.15,1.88,1.13,1.13,1.25,1.26,1.13,1.13,1.13,1.14	300	200	1
114	20	4.88	4.00	7.50	1.13,1.15,1.13,1.34,1.13,1.13,1.13,2.34,2.81,1.14,1.14,1.13,3.85,1.12,1.12,1.72,2.11,1.13,1.13,1.14,2.24,1.14,1.14,1.13,4.33	300	200	1
115	20	6.63	6.63	10.20	1.12,1.12,1.12,1.12,1.12,1.12,1.11,1.11,1.12,1.12,1.11,1.11,1.11,1.11,1.11,1.11,1.13,1.14,1.11,1.11,1.10,1.10,1.11,1.11,1.11,1.11	300	200	1
116	20	6.63	6.63	10.20	1.12,1.12,1.12,1.13,1.12,1.12,1.11,1.11,1.11,1.18,1.11,1.11,1.11,1.25,1.13,1.13,1.14,1.15,1.11,1.11,1.10,1.14,1.11,1.11,1.11,1.52	300	200	1

Member Design Capacity

Member ID	$\Phi_t P_n$ (kip)	$\Phi_c P_n$ (kip)	$\Phi_b M_{zn}$ (k-ft)	$\Phi_b M_{yn}$ (k-ft)	$\Phi_v V_{yn}$ (kip)	$\Phi_v V_{zn}$ (kip)
1	251.16	126.02	42.30	42.30	75.35	75.35
2	251.01	248.88	27.16	27.16	75.30	75.30
3	151.65	150.70	20.17	14.14	54.12	28.95
4	151.65	145.15	20.17	14.14	54.12	28.95
5	151.65	149.10	20.17	14.14	54.12	28.95
6	151.65	150.70	20.17	14.14	54.12	28.95
7	151.65	149.10	20.17	14.14	54.12	28.95
8	159.30	142.47	46.90	6.46	56.26	44.91
9	75.10	66.32	4.25	4.25	22.53	22.53
10	151.65	145.15	20.17	14.14	54.12	28.95
11	159.30	142.47	46.90	6.46	56.26	44.91
12	251.01	248.88	27.16	27.16	75.30	75.30
13	159.30	116.35	34.23	6.46	56.26	44.91
14	159.30	116.35	34.53	6.46	56.26	44.91
15	159.30	55.15	46.90	6.46	56.26	44.91
16	159.30	55.15	46.90	6.46	56.26	44.91
101	251.16	126.02	42.30	42.30	75.35	75.35
102	251.01	248.88	27.16	27.16	75.30	75.30
103	151.65	150.70	20.17	14.14	54.12	28.95
104	151.65	145.15	20.17	14.14	54.12	28.95
105	151.65	149.10	20.17	14.14	54.12	28.95
106	151.65	150.70	20.17	14.14	54.12	28.95
107	151.65	149.10	20.17	14.14	54.12	28.95
108	159.30	55.15	46.90	6.46	56.26	44.91
109	75.10	66.32	4.25	4.25	22.53	22.53
110	151.65	145.15	20.17	14.14	54.12	28.95
111	159.30	55.15	46.90	6.46	56.26	44.91
112	251.01	248.88	27.16	27.16	75.30	75.30
113	159.30	116.35	34.23	6.46	56.26	44.91
114	159.30	116.35	34.23	6.46	56.26	44.91
115	159.30	75.13	21.18	6.46	56.26	44.91

115	159.30	75.13	21.18	6.46	56.26	44.91
116	159.30	75.13	21.18	6.46	56.26	44.91

Design Ratio

Member ID	P	M_z	M_y	V_y	V_z	(P,M_z,M_y)	Worst LC	KL/r	δ	Status
1	0.112	0.696	0.039	0.036	0.004	0.701	#16	0.486	Not Required	Pass
2	0.003	0.396	0.091	0.087	0.015	0.474	#21	0.036	Not Required	Pass
3	0.007	0.578	0.034	0.058	0.008	0.612	#21	0.046	Not Required	Pass
4	0.007	0.574	0.114	0.057	0.026	0.660	#21	0.082	Not Required	Pass
5	0.007	0.358	0.109	0.058	0.027	0.384	#21	0.076	Not Required	Pass
6	0.009	0.631	0.083	0.064	0.025	0.719	#21	0.046	Not Required	Pass
7	0.009	0.390	0.159	0.063	0.044	0.443	#21	0.076	Not Required	Pass
8	0.001	0.414	0.151	0.312	0.017	0.486	#24	0.102	Not Required	Pass
9	0.012	0.055	0.056	0.001	0.002	0.117	#21	0.206	Not Required	Pass
10	0.009	0.628	0.146	0.063	0.031	0.724	#21	0.082	Not Required	Pass
11	0.003	0.230	0.159	0.171	0.018	0.340	#24	0.102	Not Required	Pass
12	0.002	0.459	0.088	0.099	0.017	0.536	#21	0.036	Not Required	Pass
13	0.005	0.201	0.413	0.111	0.024	0.563	#24	0.306	Not Required	Pass
14	0.006	0.371	0.415	0.207	0.022	0.689	#24	0.204	Not Required	Pass
15	0.000	0.092	0.145	0.040	0.011	0.237	#24	0.401	Not Required	Pass
16	0.000	0.161	0.148	0.070	0.011	0.309	#24	0.401	Not Required	Pass
101	0.112	0.696	0.038	0.036	0.004	0.701	#16	0.486	Not Required	Pass
102	0.002	0.458	0.088	0.098	0.017	0.535	#21	0.036	Not Required	Pass
103	0.009	0.631	0.083	0.064	0.025	0.718	#21	0.046	Not Required	Pass
104	0.009	0.627	0.147	0.063	0.031	0.723	#21	0.082	Not Required	Pass
105	0.009	0.391	0.159	0.063	0.043	0.443	#21	0.076	Not Required	Pass
106	0.007	0.579	0.034	0.058	0.008	0.613	#21	0.046	Not Required	Pass
107	0.007	0.359	0.108	0.058	0.027	0.385	#21	0.076	Not Required	Pass
108	0.000	0.161	0.147	0.070	0.011	0.308	#24	0.401	Not Required	Pass
109	0.012	0.055	0.056	0.001	0.002	0.117	#21	0.206	Not Required	Pass
110	0.007	0.574	0.114	0.057	0.026	0.660	#21	0.082	Not Required	Pass
111	0.000	0.092	0.145	0.040	0.011	0.236	#24	0.401	Not Required	Pass
112	0.003	0.397	0.091	0.087	0.015	0.475	#21	0.036	Not Required	Pass
113	0.005	0.185	0.413	0.098	0.024	0.551	#24	0.306	Not Required	Pass
114	0.006	0.344	0.416	0.185	0.023	0.670	#24	0.306	Not Required	Pass
115	0.005	0.319	0.226	0.040	0.018	0.545	#21	0.507	Not Required	Pass
116	0.001	0.347	0.236	0.042	0.018	0.577	#21	0.507	Not Required	Pass

Definitions

Φ_t	Safety factor for tensile
Φ_c	Safety factor for compression
Φ_b	Safety factor for flexure
Φ_v	Safety factor for shear
E	Modulus of elasticity
F_y	Specified minimum yield stress
F_u	Specified minimum tensile strength
A	Cross-sectional area
J	Torsional constant
I_{yp}	Moment of inertia about the Y axes
I_{zp}	Moment of inertia about the Z axes
I_w	Warping constant
S_{yp}	Plastic section modulus about the Y axis
S_{zp}	Plastic section modulus about the Z axis
KL	Effective length
C_b	Buckling modification factor (from all load combinations)
L_b	Length between braced points

L_b	Length between braced points
LST	Limited slenderness for tension
LSC	Limited slenderness for compression
LD	Limited deflection
P_n	Nominal axial strength (tension/comresssion)
M_n	Nominal flexural strength (about Z/Y axis)
V_n	Nominal shear strength (along Z/Y axis)
P	Design ratio in case of axial force
M_z	Design ratio in case of bending about Z axis
M_y	Design ratio in case of bending about Y axis
V_y	Design ratio in case of shear along Y axis
V_z	Design ratio in case of shear along Z axis
(P,M_z,M_y)	Design ratio in case of axial force and bending action
KL/r	Design ratio in case of section slenderness
δ	Design ratio in case of member deflection
OK	Capacity is provided
NG	Capacity is not provided

REFERENCES	CALCULATIONS	RESULTS

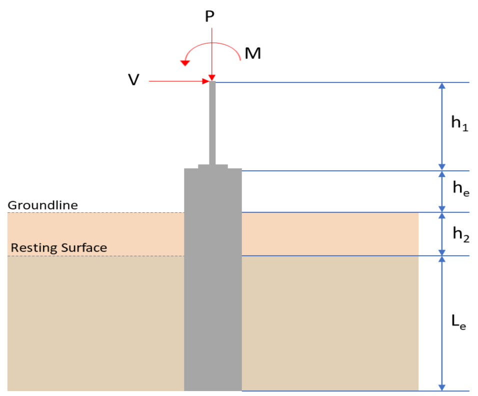
SkyCiv Foundation Design

Pile Foundation

Design Information :

Design code : IBC 2021 (International Building Code)
Unit System : Imperial

Pile Input



Geometry

Pile shape: rectangular
$b = 48 \text{ in}$ - Pile width
$D = 48 \text{ in}$ - Pile depth
$L = 5.5 \text{ ft}$ - Total pile length
$h_1 = 0 \text{ ft}$ - Lateral load height from the top of the pile,
$h_2 = 0 \text{ ft}$ - Depth to resisting surface
$h_e = 0 \text{ ft}$ - Length of pile above the ground

Tabulation of Soil Parameters

Layer	Label	Allowable Bearing Pressure (q_a) (psf)	Allowable Lateral Pressure (R) (psf/ft)
1	Sand, silty sand, clayey sand, silty gravel & clayey gravel	2000.000	150.000

Tabulation of Loads

Load Component	ASD	LRFD
P (kip)	8.767	14.074
V_x (kip)	-1.542	-2.571
V_z (kip)	0.149	0.268
M_x (kipft)	0.384	0.660
M_z (kipft)	17.178	29.442

Material Properties

$f'_{ck} = 2.5 \text{ ksi}$ - Concrete strength,

Required depth to resist lateral loads (ASD)

H - Point of application of the lateral load

$$H = h_1 + h_2 + h_e$$

$$H = (0 \text{ ft}) + (0 \text{ ft}) + (0 \text{ ft})$$

$$H = 0 \text{ ft}$$

Considering x-direction:

H_o - Lateral force per length of pile,

$$H_o = \frac{V_x}{1.57\, D}$$

$$H_o = \frac{(-1.542 \text{ kip})}{1.57 \times (48 \text{ in})}$$

$$H_o = -0.24554 \text{ kip/ft}$$

M_o - Moment per length of pile,

$$M_o = \frac{M_z + (V_x\, H)}{1.57\, D}$$

$$M_o = \frac{(17.178\ \mathrm{kipft}) + ((-1.542\ \mathrm{kip}) \times (0\ \mathrm{ft}))}{1.57 \times (48\ \mathrm{in})}$$

$$M_o = 2.7354\ \mathrm{kipft/ft}$$

Required depth of embedment in earth:

$$L_x^3 - \left(14.14 \times \frac{H_o \times L_x}{R}\right) - \left(18.85 \times \frac{M_o}{R}\right) = 0$$

Solving the cubic equation:
$L_{e,x} = 5.2168\ \mathrm{ft}$ - Required depth in x-direction,

Considering z-direction:

H_o - Lateral force per length of pile,

$$H_o = \frac{V_z}{1.57\, b}$$

$$H_o = \frac{(0.149\ \mathrm{kip})}{1.57 \times (48\ \mathrm{in})}$$

$$H_o = 0.023726\ \mathrm{kip/ft}$$

M_o - Moment per length of pile,

$$M_o = \frac{M_x + (V_z\, H)}{1.57\, b}$$

$$M_o = \frac{(0.384\ \mathrm{kipft}) + ((0.149\ \mathrm{kip}) \times (0\ \mathrm{ft}))}{1.57 \times (48\ \mathrm{in})}$$

$$M_o = 0.061146\ \mathrm{kipft/ft}$$

Required depth of embedment in earth:

$$L_z^3 - \left(14.14 \times \frac{H_o \times L_z}{R}\right) - \left(18.85 \times \frac{M_o}{R}\right) = 0$$

Solving the cubic equation:
$L_{e,z} = 1.975\ \mathrm{ft}$ - Required depth in z-direction,

Minimum embedded depth required:

$L_{e,req}$ - Depth of pile required,

$$L_{e,req} = MAX[L_{e,x}, L_{e,z}]$$

$$L_{e,req} = MAX[(5.2168\ \mathrm{ft}), (1.975\ \mathrm{ft})]$$

$$L_{e,req} = 5.217\ \mathrm{ft}$$

L_e - Actual embedded length of pile,

$$L_e = L - h_e - h_2$$

$$L_e = (5.5\ \mathrm{ft}) - (0\ \mathrm{ft}) - (0\ \mathrm{ft})$$

$$L_e = 5.5\ \mathrm{ft}$$

$Ratio$ - Embedded depth

$$Ratio = \frac{L_{e,req}}{L_e}$$

$$Ratio = \frac{(5.217\ \mathrm{ft})}{(5.5\ \mathrm{ft})}$$

$$Ratio = 0.94855$$

Status: **PASS**
Ratio: **0.950**

End-bearing Capacity (ASD)

A - Pile cross-section area

$$A = b\, D$$

$$A = (48\ \mathrm{in}) \times (48\ \mathrm{in})$$

$$A = 16\ \mathrm{ft}^2$$

q - End-bearing pressure

$$q = \frac{P_v}{A}$$

$$q = \frac{(8.767\ \mathrm{kip})}{(16\ \mathrm{ft}^2)}$$

$$q = 0.54794\ \mathrm{kip/ft}^2$$

$$q = 0.54794\ \mathrm{kip/ft}$$

Check bearing capacity ratio:

$Ratio$ - Capacity

$$Ratio = \frac{q}{q_a}$$

$$Ratio = \frac{\left(0.54794\ \mathrm{kip/ft^2}\right)}{\left(2000\ \mathrm{psf}\right)}$$

$$Ratio = 0.27397$$

Status: **PASS**
Ratio: **0.270**

Czerniak

Lateral Soil Pressure (ASD):

L/D - Length to least lateral dimension ratio,

$$L/D = \frac{L}{D}$$

$$L/D = \frac{\left(5.5\ \mathrm{ft}\right)}{\left(48\ \mathrm{in}\right)}$$

$$L/D = 1.375$$

Since L/D $\leq$ 10,

Pile is short.

Considering x-direction:

$H_o = -0.24554\ \mathrm{kip/ft}$ - Lateral force per length of pile,
$M_o = 2.7354\ \mathrm{kipft/ft}$ - Overturning moment per length of pile,
a - Distance from resting surface to pivot point,

$$a = \frac{\left(4\ M_o\ L_e\right) + \left(3\ H_o\ L_e^2\right)}{\left(6\ M_o\right) + \left(4\ H_o\ L_e\right)}$$

$$a = \frac{\left(4 \times \left(2.7354\ \mathrm{kipft/ft}\right) \times \left(5.5\ \mathrm{ft}\right)\right) + \left(3 \times \left(-0.24554\ \mathrm{kip/ft}\right) \times \left(5.5\ \mathrm{ft}\right)^2\right)}{\left(6 \times \left(2.7354\ \mathrm{kipft/ft}\right)\right) + \left(4 \times \left(-0.24554\ \mathrm{kip/ft}\right) \times \left(5.5\ \mathrm{ft}\right)\right)}$$

$$a = 3.7802\ \mathrm{ft}$$

p - Earth pressure against the pile at distance a/2 from resting surface,

$$p = \frac{0.75\ \left[\left(4\ M_o\right) + \left(3\ H_o\ L_e\right)\right]^2}{L_e^2\ \left[\left(3\ M_o\right) + \left(2\ H_o\ L_e\right)\right]}$$

$$p = \frac{0.75 \times \left[\left(4 \times \left(2.7354\ \mathrm{kipft/ft}\right)\right) + \left(3 \times \left(-0.24554\ \mathrm{kip/ft}\right) \times \left(5.5\ \mathrm{ft}\right)\right)\right]^2}{\left(5.5\ \mathrm{ft}\right)^2 \times \left[\left(3 \times \left(2.7354\ \mathrm{kipft/ft}\right)\right) + \left(2 \times \left(-0.24554\ \mathrm{kip/ft}\right) \times \left(5.5\ \mathrm{ft}\right)\right)\right]}$$

$$p = 0.2138\ \mathrm{kip/ft^2}$$

s - Earth pressure against the pile at distance L_e,

$$s = \frac{6\ \left[\left(2\ M_o\right) + \left(H_o\ L_e\right)\right]}{L_e^2}$$

$$s = \frac{6 \times \left[\left(2 \times \left(2.7354\ \mathrm{kipft/ft}\right)\right) + \left(\left(-0.24554\ \mathrm{kip/ft}\right) \times \left(5.5\ \mathrm{ft}\right)\right)\right]}{\left(5.5\ \mathrm{ft}\right)^2}$$

$$s = 0.81723\ \mathrm{kip/ft^2}$$

Check lateral soil pressure capacity:

p_a - Allowable lateral soil pressure at depth a/2,

$$p_a = R\ \frac{a}{2}$$

$$p_a = \left(150\ \mathrm{psf/ft}\right) \times \frac{\left(3.7802\ \mathrm{ft}\right)}{2}$$

$$p_a = 0.28351\ \mathrm{kip/ft^2}$$

$Ratio$ - Lateral soil capacity

$$Ratio = \frac{p}{p_a}$$

$$Ratio = \frac{\left(0.2138\ \mathrm{kip/ft^2}\right)}{\left(0.28351\ \mathrm{kip/ft^2}\right)}$$

$$Ratio = 0.75411$$

Status: **PASS**
Ratio: **0.750**

p_s - Allowable lateral soil pressure at depth L_e,

$$p_s = R\, L_e$$

$$p_s = (150 \text{ psf/ft}) \times (5.5 \text{ ft})$$

$$p_s = 0.825 \text{ kip/ft}^2$$

$Ratio$ - Lateral soil capacity

$$Ratio = \frac{s}{p_s}$$

$$Ratio = \frac{\left(0.81723 \text{ kip/ft}^2\right)}{\left(0.825 \text{ kip/ft}^2\right)}$$

$$Ratio = 0.9906$$

Status: PASS
Ratio: 0.990

Considering z-direction:

$H_o = 0.023726 \text{ kip/ft}$ - Lateral force per length of pile,
$M_o = 0.061146 \text{ kipft/ft}$ - Overturning moment per length of pile,
a - Distance from resting surface to pivot point,

$$a = \frac{(4\, M_o\, L_e) + \left(3\, H_o\, L_e^2\right)}{(6\, M_o) + (4\, H_o\, L_e)}$$

$$a = \frac{(4 \times (0.061146 \text{ kipft/ft}) \times (5.5 \text{ ft})) + \left(3 \times (0.023726 \text{ kip/ft}) \times (5.5 \text{ ft})^2\right)}{(6 \times (0.061146 \text{ kipft/ft})) + (4 \times (0.023726 \text{ kip/ft}) \times (5.5 \text{ ft}))}$$

$$a = 3.9358 \text{ ft}$$

p - Earth pressure against the pile at distance a/2 from resting surface,

$$p = \frac{0.75\, [(4\, M_o) + (3\, H_o\, L_e)]^2}{L_e^2\, [(3\, M_o) + (2\, H_o\, L_e)]}$$

$$p = \frac{0.75 \times [(4 \times (0.061146 \text{ kipft/ft})) + (3 \times (0.023726 \text{ kip/ft}) \times (5.5 \text{ ft}))]^{\ 2}}{(5.5 \text{ ft})^2 \times [(3 \times (0.061146 \text{ kipft/ft})) + (2 \times (0.023726 \text{ kip/ft}) \times (5.5 \text{ ft}))]}$$

$$p = 0.022571 \text{ kip/ft}^2$$

s - Earth pressure against the pile at distance L_e,

$$s = \frac{6\, [(2\, M_o) + (H_o\, L_e)]}{L_e^2}$$

$$s = \frac{6 \times [(2 \times (0.061146 \text{ kipft/ft})) + ((0.023726 \text{ kip/ft}) \times (5.5 \text{ ft}))]}{(5.5 \text{ ft})^2}$$

$$s = 0.050139 \text{ kip/ft}^2$$

Check lateral soil pressure capacity:

p_a - Allowable lateral soil pressure at depth a/2,

$$p_a = R\, \frac{a}{2}$$

$$p_a = (150 \text{ psf/ft}) \times \frac{(3.9358 \text{ ft})}{2}$$

$$p_a = 0.29519 \text{ kip/ft}^2$$

$Ratio$ - Lateral soil capacity

$$Ratio = \frac{p}{p_a}$$

$$Ratio = \frac{\left(0.022571 \text{ kip/ft}^2\right)}{\left(0.29519 \text{ kip/ft}^2\right)}$$

$$Ratio = 0.076462$$

Status: PASS
Ratio: 0.080

p_s - Allowable lateral soil pressure at depth L_e,

$$p_s = R\, L_e$$

$$p_s = (150 \text{ psf/ft}) \times (5.5 \text{ ft})$$

$$p_s = 0.825 \text{ kip/ft}^2$$

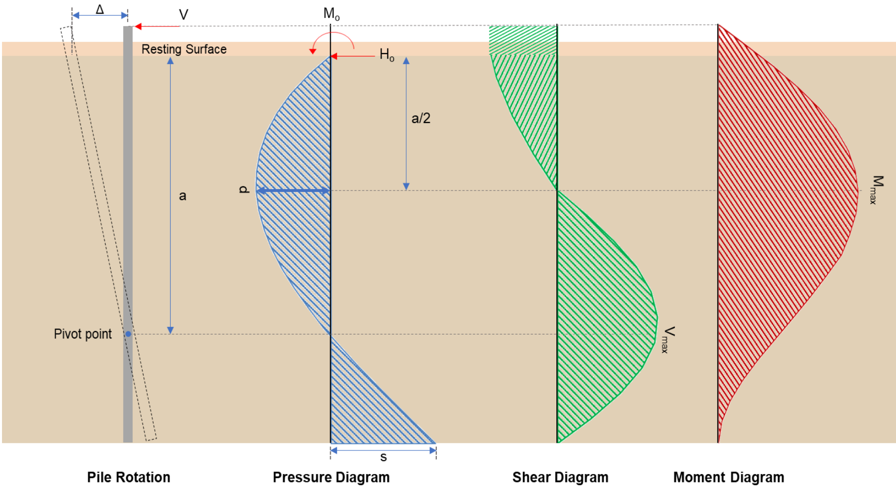
$Ratio$ - Lateral soil capacity

$$Ratio = \frac{s}{p_s}$$

$$Ratio = \frac{(0.050139 \text{ kip/ft}^2)}{(0.825 \text{ kip/ft}^2)}$$

$$Ratio = 0.060775$$

Status: **PASS**
Ratio: **0.060**



Shear force and Bending moment (x-direction, LRFD)

H_o - Lateral force per length of pile,

$$H_o = \frac{V_x}{1.57\, D}$$

$$H_o = \frac{(-2.571 \text{ kip})}{1.57 \times (48 \text{ in})}$$

$$H_o = -0.40939 \text{ kip/ft}$$

M_o - Moment per length of pile,

$$M_o = \frac{M_z + (V_x\, H)}{1.57\, D}$$

$$M_o = \frac{(29.442 \text{ kipft}) + ((-2.571 \text{ kip}) \times (0 \text{ ft}))}{1.57 \times (48 \text{ in})}$$

$$M_o = 4.6882 \text{ kipft/ft}$$

E - Distance from lateral load to resisting surface,

$$E = \frac{M_o}{H_o}$$

$$E = \frac{(4.6882 \text{ kipft/ft})}{(-0.40939 \text{ kip/ft})}$$

$$E = 11.452 \text{ ft}$$

a - Distance from resting surface to pivot point,

$$a = \frac{(4\, M_o\, L_e) + \left(3\, H_o\, L_e^2\right)}{(6\, M_o) + (4\, H_o\, L_e)}$$

$$a = \frac{(4 \times (4.6882 \text{ kipft/ft}) \times (5.5 \text{ ft})) + \left(3 \times (-0.40939 \text{ kip/ft}) \times (5.5 \text{ ft})^2\right)}{(6 \times (4.6882 \text{ kipft/ft})) + (4 \times (-0.40939 \text{ kip/ft}) \times (5.5 \text{ ft}))}$$

$$a = 3.7778 \text{ ft}$$

V_{max} - Max shear force located at depth a,

$$V_{max} = (H_o\, D) \left[1 - \left[3 \left(\frac{4\, E}{L_e} + 3\right) \left(\frac{a}{L_e}\right)^2\right] + \left[4 \left(\frac{3\, E}{L_e} + 2\right) \left(\frac{a}{L_e}\right)^3\right]\right]$$

$$V_{max} = ((-0.40939 \text{ kip/ft}) \times (48 \text{ in})) \times \left[1 - \left[3 \times \left(\frac{4 \times (11.452 \text{ ft})}{(5.5 \text{ ft})} + 3\right) \times \left(\frac{(3.7778 \text{ ft})}{(5.5 \text{ ft})}\right)^2\right] + \left[4 \times \left(\frac{3 \times (11.452 \text{ ft})}{(5.5 \text{ ft})} + 2\right) \times \left(\frac{(3.7778 \text{ ft})}{(5.5 \text{ ft})}\right)^3\right]\right]$$

$$V_{max} = 7.1149 \text{ kip}$$

M_{max} - Max bending moment located at depth a/2,

$$M_{max} = (H_o\, D\, L_e) \left[\left(\frac{E}{L_e} + \frac{a}{2\, L_e} \right) - \left[\left(\frac{4\, E}{L_e} + 3 \right) \left(\frac{a}{2\, L_e} \right)^3 \right] + \left[\left(\frac{3\, E}{L_e} + 2 \right) \left(\frac{a}{2\, L_e} \right)^4 \right] \right]$$

$$M_{max} = ((-0.40939 \text{ kip/ft}) \times (48 \text{ in}) \times (5.5 \text{ ft})) \times \left[\left(\frac{(11.452 \text{ ft})}{(5.5 \text{ ft})} + \frac{(3.7778 \text{ ft})}{2 \times (5.5 \text{ ft})} \right) - \left[\left(\frac{4 \times (11.452 \text{ ft})}{(5.5 \text{ ft})} + 3 \right) \times \left(\frac{(3.7778 \text{ ft})}{2 \times (5.5 \text{ ft})} \right)^3 \right] + \left[\left(\frac{3 \times (11.452 \text{ ft})}{(5.5 \text{ ft})} + 2 \right) \times \left(\frac{(3.7778 \text{ ft})}{2 \times (5.5 \text{ ft})} \right)^4 \right] \right]$$

$$M_{max} = 18.746 \text{ kipft}$$

Shear force and Bending moment (z-direction, LRFD)

H_o - Lateral force per length of pile,

$$H_o = \frac{V_z}{1.57\, b}$$

$$H_o = \frac{(0.268 \text{ kip})}{1.57 \times (48 \text{ in})}$$

$$H_o = 0.042675 \text{ kip/ft}$$

M_o - Moment per length of pile,

$$M_o = \frac{M_x + (V_z\, H)}{1.57\, b}$$

$$M_o = \frac{(0.66 \text{ kipft}) + ((0.268 \text{ kip}) \times (0 \text{ ft}))}{1.57 \times (48 \text{ in})}$$

$$M_o = 0.1051 \text{ kipft/ft}$$

E - Distance from lateral load to resisting surface,

$$E = \frac{M_o}{H_o}$$

$$E = \frac{(0.1051 \text{ kipft/ft})}{(0.042675 \text{ kip/ft})}$$

$$E = 2.4627 \text{ ft}$$

a - Distance from resting surface to pivot point,

$$a = \frac{(4\, M_o\, L_e) + \left(3\, H_o\, L_e^2\right)}{(6\, M_o) + (4\, H_o\, L_e)}$$

$$a = \frac{(4 \times (0.1051 \text{ kipft/ft}) \times (5.5 \text{ ft})) + \left(3 \times (0.042675 \text{ kip/ft}) \times (5.5 \text{ ft})^2\right)}{(6 \times (0.1051 \text{ kipft/ft})) + (4 \times (0.042675 \text{ kip/ft}) \times (5.5 \text{ ft}))}$$

$$a = 3.9408 \text{ ft}$$

V_{max} - Max shear force located at depth a,

$$V_{max} = (H_o\, b) \left[1 - \left[3 \left(\frac{4\, E}{L_e} + 3 \right) \left(\frac{a}{L_e} \right)^2 \right] + \left[4 \left(\frac{3\, E}{L_e} + 2 \right) \left(\frac{a}{L_e} \right)^3 \right] \right]$$

$$V_{max} = ((0.042675 \text{ kip/ft}) \times (48 \text{ in})) \times \left[1 - \left[3 \times \left(\frac{4 \times (2.4627 \text{ ft})}{(5.5 \text{ ft})} + 3 \right) \times \left(\frac{(3.9408 \text{ ft})}{(5.5 \text{ ft})} \right)^2 \right] + \left[4 \times \left(\frac{3 \times (2.4627 \text{ ft})}{(5.5 \text{ ft})} + 2 \right) \times \left(\frac{(3.9408 \text{ ft})}{(5.5 \text{ ft})} \right)^3 \right] \right]$$

$$V_{max} = 0.24917 \text{ kip}$$

M_{max} - Max bending moment located at depth a/2,

$$M_{max} = (H_o\, b\, L_e) \left[\left(\frac{E}{L_e} + \frac{a}{2\, L_e} \right) - \left[\left(\frac{4\, E}{L_e} + 3 \right) \left(\frac{a}{2\, L_e} \right)^3 \right] + \left[\left(\frac{3\, E}{L_e} + 2 \right) \left(\frac{a}{2\, L_e} \right)^4 \right] \right]$$

$$M_{max} = ((0.042675 \text{ kip/ft}) \times (48 \text{ in}) \times (5.5 \text{ ft})) \times \left[\left(\frac{(2.4627 \text{ ft})}{(5.5 \text{ ft})} + \frac{(3.9408 \text{ ft})}{2 \times (5.5 \text{ ft})} \right) - \left[\left(\frac{4 \times (2.4627 \text{ ft})}{(5.5 \text{ ft})} + 3 \right) \times \left(\frac{(3.9408 \text{ ft})}{2 \times (5.5 \text{ ft})} \right)^3 \right] + \left[\left(\frac{3 \times (2.4627 \text{ ft})}{(5.5 \text{ ft})} + 2 \right) \times \left(\frac{(3.9408 \text{ ft})}{2 \times (5.5 \text{ ft})} \right)^4 \right] \right]$$

$$M_{max} = 0.60161 \text{ kipft}$$

Minimum Reinforcement Check (LRFD)

Parameters:

$f'_{ck} = 2.5 \text{ ksi}$ - Concrete strength,
$f_{yk} = 60 \text{ ksi}$ - Longitudinal reinforcement strength,
$\phi = 0.65$ - Reduction factor for axial strength,
Table 22.4.2.1 $\alpha = 0.8$ - Alpha factor for axial strength,
$A_g = 2304 \text{ in}^2$ - Gross area of concrete,

Longitudinal reinforcement:

Required reinforcement due to axial load, $A_{st,required}$
22.4.2.2, 10.6.1.1 $A_{st,required}$

$$A_{st,required} = Min\left[\frac{\frac{P}{\phi\ \alpha} - \left(0.85\ f'_{ck}\ A_g\right)}{f_{yk} - \left(0.85\ f'_{ck}\right)}, \left(0.08\ A_g\right)\right]$$

$$A_{st,required} = Min\left[\frac{\frac{(14.074 \text{ kip})}{(0.65)\times(0.8)} - \left(0.85 \times (2.5 \text{ ksi}) \times \left(2304 \text{ in}^2\right)\right)}{(60 \text{ ksi}) - (0.85 \times (2.5 \text{ ksi}))}, \left(0.08 \times \left(2304 \text{ in}^2\right)\right)\right]$$

$$A_{st,required} = -84.128 \text{ in}^2$$

A_{min} - Governing minimum reinforcement area,

$$A_{min} = Max\left[A_{st,required}, \left(0.0018\ A_g\right)\right]$$

$$A_{min} = Max\left[\left(-84.128 \text{ in}^2\right), \left(0.0018 \times \left(2304 \text{ in}^2\right)\right)\right]$$

$$A_{min} = 4.1472 \text{ in}^2$$

n_{rebar} - Required number of reinforcement,

$$n_{rebar} = \frac{A_{min}}{A_{rebar}}$$

$$n_{rebar} = \frac{\left(4.1472 \text{ in}^2\right)}{\left(0.3068 \text{ in}^2\right)}$$

$$n_{rebar} = 14$$

A_{st} - Actual total reinforcement area,

$$A_{st} = n_{rebar}\ \frac{\pi\ d_{bar}^2}{4}$$

$$A_{st} = (14) \times \frac{\pi \times (0.625 \text{ in})^2}{4}$$

$$A_{st} = 4.2951 \text{ in}^2$$

$Ratio$ - Capacity

$$Ratio = \frac{A_{min}}{A_{st}}$$

$$Ratio = \frac{\left(4.1472 \text{ in}^2\right)}{\left(4.2951 \text{ in}^2\right)}$$

$$Ratio = 0.96556$$

Status: **PASS**
Ratio: **0.970**

25.2.3 s_{rebar} - Minimum spacing of reinforcement,

$$s_{rebar} = Max\left[1.5, \left(1.5\ d_{bar}\right)\right]$$

$$s_{rebar} = Max\left[1.5, (1.5 \times (0.625 \text{ in}))\right]$$

$$s_{rebar} = 1.5 \text{ in}$$

Ties:

25.7.2.2 Since longitudinal reinforcement is $\leq$ No. 10ø: Use #3(0.375 in)
25.7.2.1 s_{ties} - Maximum spacing of ties,

$$s_{ties} = Min\left[\left(16\ d_{bar}\right), \left(48\ d_{ties}\right), Min\left(D, b\right)\right]$$

$$s_{ties} = Min\left[(16 \times (0.625 \text{ in})), (48 \times (0.375 \text{ in})), Min\left((48 \text{ in}), (48 \text{ in})\right)\right]$$

$$s_{ties} = 10 \text{ in}$$

Summary:

Main reinforcement: **14 - #5 (0.625 in)**

	Ties: **#3(0.375 in) - 10 in**	
	Axial Compression Strength (ACI 318-19, LRFD)	
22.4.2.2	ϕP_N - Allowable axial compressive strength $$\phi P_N = \phi\, 0.80\, \left[\left(0.85\, f'_{ck}\, [A_g - A_{st}]\right) + (f_{yk}\, A_{st})\right]$$ $$\phi P_N = (0.65) \times 0.80 \times \left[\left(0.85 \times (2.5\ \mathrm{ksi}) \times \left[\left(2304\ \mathrm{in}^2\right) - \left(4.2951\ \mathrm{in}^2\right)\right]\right) + \left((60\ \mathrm{ksi}) \times \left(4.2951\ \mathrm{in}^2\right)\right)\right]$$ $$\phi P_N = 2675.2\ \mathrm{kip}$$ $Ratio$ - Capacity $$Ratio = \frac{P}{\phi P_N}$$ $$Ratio = \frac{(14.074\ \mathrm{kip})}{(2675.2\ \mathrm{kip})}$$ $$Ratio = 0.0052609$$	Status: **PASS** Ratio: **0.010**
	Shear Strength (ACI 318-19, LRFD) **Parameters:** $b_w = 48\ \mathrm{in}$ - Effective width,	
22.5.2.2	d - Effective depth $$d = 0.80\, D$$ $$d = 0.80 \times (48\ \mathrm{in})$$ $$d = 38.4\ \mathrm{in}$$	
22.5.5.1.3	λ_s - size effect modification factor $$\lambda_s = MIN\left[\sqrt{\frac{2}{1+\frac{d}{10}}}, 1\right]$$ $$\lambda_s = MIN\left[\sqrt{\frac{2}{1+\frac{(38.4\ \mathrm{in})}{10}}}, 1\right]$$ $$\lambda_s = 0.64282$$ The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5\ \mathrm{ksi} \rightarrow 2500\ \mathrm{psi}$,	
22.5.5.1.1	$V_{c,max}$ - Max shear strength of concrete $$V_{c,max} = 5\, \lambda_s\, \sqrt{f'_{ck}}\, b_w\, d$$ $$V_{c,max} = 5 \times (0.64282) \times \sqrt{(2500\ \mathrm{psi})} \times (48\ \mathrm{in}) \times (38.4\ \mathrm{in})$$ $$V_{c,max} = 296.21\ \mathrm{kip}$$ The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5\ \mathrm{ksi} \rightarrow 2500\ \mathrm{psi}$, $P = 14.074\ \mathrm{kip} \rightarrow 14074\ \mathrm{lbf}$,	
22.5.5.1.1(a)	$V_{c,a}$ - Shear strength of concrete (a) $$V_{c,a} = \left[2\, \lambda_s\, \sqrt{f'_{ck}} + \frac{P}{6\, A_g}\right]\, b_w\, d$$ $$V_{c,a} = \left[2 \times (0.64282) \times \sqrt{(2500\ \mathrm{psi})} + \frac{(14074\ \mathrm{lbf})}{6 \times (2304\ \mathrm{in}^2)}\right] \times (48\ \mathrm{in}) \times (38.4\ \mathrm{in})$$ $$V_{c,a} = 120.36\ \mathrm{kip}$$ The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5\ \mathrm{ksi} \rightarrow 2500\ \mathrm{psi}$,	
22.5.5.1.2	$V_{c,b}$ - Shear strength of concrete (b) $$V_{c,b} = \left[2\, \lambda_s\, \sqrt{f'_{ck}} + \left(0.05\, f'_{ck}\right)\right]\, b_w\, d$$ $$V_{c,b} = \left[2 \times (0.64282) \times \sqrt{(2500\ \mathrm{psi})} + (0.05 \times (2500\ \mathrm{psi}))\right] \times (48\ \mathrm{in}) \times (38.4\ \mathrm{in})$$ $$V_{c,b} = 348.89\ \mathrm{kip}$$ V_c - Governing shear strength of concrete $$V_c = Min\left[V_{c,max}, V_{c,a}, V_{c,b}\right]$$ $$V_c = Min\left[(296.21\ \mathrm{kip}), (120.36\ \mathrm{kip}), (348.89\ \mathrm{kip})\right]$$ $$V_c = 120.36\ \mathrm{kip}$$	

The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5 \text{ ksi} \rightarrow 2500 \text{ psi}$,

22.5.1.2 $V_{s,a}$ - Shear strength of steel (a)

$$V_{s,a} = 8 \sqrt{f'_{ck}}\, b_w\, d$$

$$V_{s,a} = 8 \times \sqrt{(2500 \text{ psi})} \times (48 \text{ in}) \times (38.4 \text{ in})$$

$$V_{s,a} = 737.28 \text{ kip}$$

A_v - Ties rebar area,

$$A_v = \frac{\pi\, d_{ties}^2}{4}$$

$$A_v = \frac{\pi \times (0.375 \text{ in})^2}{4}$$

$$A_v = 0.11045 \text{ in}^2$$

22.5.8.5.3 $V_{s,b}$ - Shear strength of steel (b)

$$V_{s,b} = \frac{2\, A_v\, f_{ywk}\, d}{s_{ties}}$$

$$V_{s,b} = \frac{2 \times \left(0.11045 \text{ in}^2\right) \times (60 \text{ ksi}) \times (38.4 \text{ in})}{(10 \text{ in})}$$

$$V_{s,b} = 50.894 \text{ kip}$$

V_s - Governing shear strength of steel

$$V_s = MIN\left[V_{s,a}, V_{s,b}\right]$$

$$V_s = MIN\left[(737.28 \text{ kip}), (50.894 \text{ kip})\right]$$

$$V_s = 50.894 \text{ kip}$$

22.5.1.1 ϕV_n - Allowable shear strength

$$\phi V_n = \phi\, \left(V_c + V_s\right)$$

$$\phi V_n = (0.65) \times ((120.36 \text{ kip}) + (50.894 \text{ kip}))$$

$$\phi V_n = 111.32 \text{ kip}$$

Considering x-direction:

$V_{max} = 7.1149 \text{ kip}$ - Maximum shear force in the x-direction,
$Ratio$ - Capacity

$$Ratio = \frac{V_{max}}{\phi V_n}$$

$$Ratio = \frac{(7.1149 \text{ kip})}{(111.32 \text{ kip})}$$

$$Ratio = 0.063916$$

Status: **PASS**
Ratio: **0.060**

Considering z-direction:

$V_{max} = 0.24917 \text{ kip}$ - Maximum shear force in the z-direction,
$Ratio$ - Capacity

$$Ratio = \frac{V_{max}}{\phi V_n}$$

$$Ratio = \frac{(0.24917 \text{ kip})}{(111.32 \text{ kip})}$$

$$Ratio = 0.0022384$$

Status: **PASS**
Ratio: **0.000**

Flexural Strength (ACI 318-19, LRFD)

S_m - Section modulus

$$S_m = \frac{b\, D^2}{6}$$

$$S_m = \frac{(48 \text{ in}) \times (48 \text{ in})^2}{6}$$

$$S_m = 18432 \text{ in}^3$$

	$\lambda = 1$ - Concrete modification factor (Normal concrete), Allowable flexural strength: M_n shall be the lesser of: $\phi M_{n,1}$ $$\phi M_{n,1} = \phi \times 5 \times \lambda \times \sqrt{(f_c')} \times S_m$$ $$\phi M_{n,1} = 0.65 \times 5 \times 1 \times \sqrt{(2.5ksi)} \times 18432.001in^3$$ $$\phi M_{n,1} = 249.600kipft$$	
14.5.2.1b	$\phi M_{n,2}$ $$\phi M_{n,2} = \phi \, 0.85 \, f_{ck}' \, S_m$$ $$\phi M_{n,2} = (0.65) \times 0.85 \times (2.5 \text{ ksi}) \times \left(18432 \text{ in}^3\right)$$ $$\phi M_{n,2} = 2121.6 \text{ kipft}$$ Therefore, ϕM_n - Allowable flexural strength, $$\phi M_n = MIN[\phi M_{n,1}, \phi M_{n,2}]$$ $$\phi M_n = MIN[(249.6 \text{ kipft}), (2121.6 \text{ kipft})]$$ $$\phi M_n = 249.6 \text{ kipft}$$ **Considering x-direction:** $M_{max} = 18.746 \text{ kipft}$ - Maximum moment in the x-direction, $Ratio$ - Capacity $$Ratio = \frac{M_{max}}{\phi M_n}$$ $$Ratio = \frac{(18.746 \text{ kipft})}{(249.6 \text{ kipft})}$$ $$Ratio = 0.075105$$	Status: **PASS** Ratio: **0.080**
	Considering z-direction: $M_{max} = 0.60161 \text{ kipft}$ - Maximum moment in the z-direction, $Ratio$ - Capacity $$Ratio = \frac{M_{max}}{\phi M_n}$$ $$Ratio = \frac{(0.60161 \text{ kipft})}{(249.6 \text{ kipft})}$$ $$Ratio = 0.0024103$$	Status: **PASS** Ratio: **0.000**

REFERENCES	CALCULATIONS	RESULTS

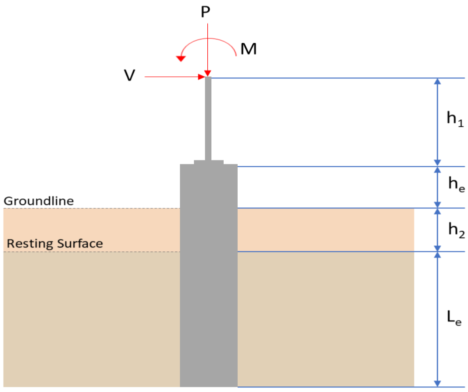
SkyCiv Foundation Design

Pile Foundation

Design Information :

Design code : IBC 2021 (International Building Code)
Unit System : Imperial

Pile Input



Geometry

Pile shape: rectangular
$b = 48\ \mathrm{in}$ - Pile width
$D = 48\ \mathrm{in}$ - Pile depth
$L = 5.5\ \mathrm{ft}$ - Total pile length
$h_1 = 0\ \mathrm{ft}$ - Lateral load height from the top of the pile,
$h_2 = 0\ \mathrm{ft}$ - Depth to resisting surface
$h_e = 0\ \mathrm{ft}$ - Length of pile above the ground

Tabulation of Soil Parameters

Layer	Label	Allowable Bearing Pressure (q_a) (psf)	Allowable Lateral Pressure (R) (psf/ft)
1	Sand, silty sand, clayey sand, silty gravel & clayey gravel	2000.000	150.000

Tabulation of Loads

Load Component	ASD	LRFD
P (kip)	8.766	14.071
V_x (kip)	-1.542	-2.570
V_z (kip)	-0.149	-0.268
M_x (kipft)	-0.386	-0.693
M_z (kipft)	17.177	29.441

Material Properties

$f'_{ck} = 2.5\ \mathrm{ksi}$ - Concrete strength,

Required depth to resist lateral loads (ASD)

H - Point of application of the lateral load

$$H = h_1 + h_2 + h_e$$

$$H = (0\ \mathrm{ft}) + (0\ \mathrm{ft}) + (0\ \mathrm{ft})$$

$$H = 0\ \mathrm{ft}$$

Considering x-direction:

H_o - Lateral force per length of pile,

$$H_o = \frac{V_x}{1.57\,D}$$

$$H_o = \frac{(-1.542\ \mathrm{kip})}{1.57 \times (48\ \mathrm{in})}$$

$$H_o = -0.24554\ \mathrm{kip/ft}$$

M_o - Moment per length of pile,

$$M_o = \frac{M_z + (V_x\,H)}{1.57\,D}$$

$$M_o = \frac{(17.177\ \mathrm{kipft}) + ((-1.542\ \mathrm{kip}) \times (0\ \mathrm{ft}))}{1.57 \times (48\ \mathrm{in})}$$

$$M_o = 2.7352\ \mathrm{kipft/ft}$$

Required depth of embedment in earth:

$$L_x^3 - \left(14.14 \times \frac{H_o \times L_x}{R}\right) - \left(18.85 \times \frac{M_o}{R}\right) = 0$$

Solving the cubic equation:
$L_{e,x} = 5.2166\ \mathrm{ft}$ - Required depth in x-direction,

Considering z-direction:

H_o - Lateral force per length of pile,

$$H_o = \frac{V_z}{1.57\, b}$$

$$H_o = \frac{(-0.149\ \mathrm{kip})}{1.57 \times (48\ \mathrm{in})}$$

$$H_o = -0.023726\ \mathrm{kip/ft}$$

M_o - Moment per length of pile,

$$M_o = \frac{M_x + (V_z\, H)}{1.57\, b}$$

$$M_o = \frac{(0.386\ \mathrm{kipft}) + ((-0.149\ \mathrm{kip}) \times (0\ \mathrm{ft}))}{1.57 \times (48\ \mathrm{in})}$$

$$M_o = 0.061465\ \mathrm{kipft/ft}$$

Required depth of embedment in earth:

$$L_z^3 - \left(14.14 \times \frac{H_o \times L_z}{R}\right) - \left(18.85 \times \frac{M_o}{R}\right) = 0$$

Solving the cubic equation:
$L_{e,z} = 1.4242\ \mathrm{ft}$ - Required depth in z-direction,

Minimum embedded depth required:

$L_{e,req}$ - Depth of pile required,

$$L_{e,req} = MAX[L_{e,x}, L_{e,z}]$$

$$L_{e,req} = MAX[(5.2166\ \mathrm{ft}), (1.4242\ \mathrm{ft})]$$

$$L_{e,req} = 5.217\ \mathrm{ft}$$

L_e - Actual embedded length of pile,

$$L_e = L - h_e - h_2$$

$$L_e = (5.5\ \mathrm{ft}) - (0\ \mathrm{ft}) - (0\ \mathrm{ft})$$

$$L_e = 5.5\ \mathrm{ft}$$

$Ratio$ - Embedded depth

$$Ratio = \frac{L_{e,req}}{L_e}$$

$$Ratio = \frac{(5.217\ \mathrm{ft})}{(5.5\ \mathrm{ft})}$$

$$Ratio = 0.94855$$

Status: **PASS**
Ratio: **0.950**

End-bearing Capacity (ASD)

A - Pile cross-section area

$$A = b\, D$$

$$A = (48\ \mathrm{in}) \times (48\ \mathrm{in})$$

$$A = 16\ \mathrm{ft}^2$$

q - End-bearing pressure

$$q = \frac{P_v}{A}$$

$$q = \frac{(8.766\ \mathrm{kip})}{(16\ \mathrm{ft}^2)}$$

$$q = 0.54788\ \mathrm{kip/ft}^2$$

$$q = 0.54788\ \mathrm{kip/ft^2}$$

Check bearing capacity ratio:

$Ratio$ - Capacity

$$Ratio = \frac{q}{q_a}$$

$$Ratio = \frac{\left(0.54788\ \mathrm{kip/ft^2}\right)}{(2000\ \mathrm{psf})}$$

$$Ratio = 0.27394$$

Status: **PASS**
Ratio: **0.270**

Czerniak

Lateral Soil Pressure (ASD):

L/D - Length to least lateral dimension ratio,

$$L/D = \frac{L}{D}$$

$$L/D = \frac{(5.5\ \mathrm{ft})}{(48\ \mathrm{in})}$$

$$L/D = 1.375$$

Since L/D $\leq$ 10,

Pile is short.

Considering x-direction:

$H_o = -0.24554\ \mathrm{kip/ft}$ - Lateral force per length of pile,
$M_o = 2.7352\ \mathrm{kipft/ft}$ - Overturning moment per length of pile,
a - Distance from resting surface to pivot point,

$$a = \frac{(4\, M_o\, L_e) + \left(3\, H_o\, L_e^2\right)}{(6\, M_o) + (4\, H_o\, L_e)}$$

$$a = \frac{(4 \times (2.7352\ \mathrm{kipft/ft}) \times (5.5\ \mathrm{ft})) + \left(3 \times (-0.24554\ \mathrm{kip/ft}) \times (5.5\ \mathrm{ft})^2\right)}{(6 \times (2.7352\ \mathrm{kipft/ft})) + (4 \times (-0.24554\ \mathrm{kip/ft}) \times (5.5\ \mathrm{ft}))}$$

$$a = 3.7802\ \mathrm{ft}$$

p - Earth pressure against the pile at distance a/2 from resting surface,

$$p = \frac{0.75\,[(4\, M_o) + (3\, H_o\, L_e)]^2}{L_e^2\,[(3\, M_o) + (2\, H_o\, L_e)]}$$

$$p = \frac{0.75 \times [(4 \times (2.7352\ \mathrm{kipft/ft})) + (3 \times (-0.24554\ \mathrm{kip/ft}) \times (5.5\ \mathrm{ft}))]^{\ 2}}{(5.5\ \mathrm{ft})^2 \times [(3 \times (2.7352\ \mathrm{kipft/ft})) + (2 \times (-0.24554\ \mathrm{kip/ft}) \times (5.5\ \mathrm{ft}))]}$$

$$p = 0.21378\ \mathrm{kip/ft^2}$$

s - Earth pressure against the pile at distance L_e,

$$s = \frac{6\,[(2\, M_o) + (H_o\, L_e)]}{L_e^2}$$

$$s = \frac{6 \times [(2 \times (2.7352\ \mathrm{kipft/ft})) + ((-0.24554\ \mathrm{kip/ft}) \times (5.5\ \mathrm{ft}))]}{(5.5\ \mathrm{ft})^2}$$

$$s = 0.81717\ \mathrm{kip/ft^2}$$

Check lateral soil pressure capacity:

p_a - Allowable lateral soil pressure at depth a/2,

$$p_a = R\,\frac{a}{2}$$

$$p_a = (150\ \mathrm{psf/ft}) \times \frac{(3.7802\ \mathrm{ft})}{2}$$

$$p_a = 0.28351\ \mathrm{kip/ft^2}$$

$Ratio$ - Lateral soil capacity

$$Ratio = \frac{p}{p_a}$$

$$Ratio = \frac{\left(0.21378\ \mathrm{kip/ft^2}\right)}{\left(0.28351\ \mathrm{kip/ft^2}\right)}$$

$$Ratio = 0.75403$$

Status: **PASS**
Ratio: **0.750**

p_s - Allowable lateral soil pressure at depth L_e,

$$p_s = R\,L_e$$

$$p_s = (150\ \mathrm{psf/ft}) \times (5.5\ \mathrm{ft})$$

$$p_s = 0.825\ \mathrm{kip/ft^2}$$

$Ratio$ - Lateral soil capacity

$$Ratio = \frac{s}{p_s}$$

$$Ratio = \frac{\left(0.81717\ \mathrm{kip/ft^2}\right)}{\left(0.825\ \mathrm{kip/ft^2}\right)}$$

$$Ratio = 0.99051$$

Status: **PASS**
Ratio: **0.990**

Considering z-direction:

$H_o = -0.023726\ \mathrm{kip/ft}$ - Lateral force per length of pile,
$M_o = 0.061465\ \mathrm{kipft/ft}$ - Overturning moment per length of pile,
a - Distance from resting surface to pivot point,

$$a = \frac{(4\,M_o\,L_e) + \left(3\,H_o\,L_e^2\right)}{(6\,M_o) + (4\,H_o\,L_e)}$$

$$a = \frac{(4 \times (0.061465\ \mathrm{kipft/ft}) \times (5.5\ \mathrm{ft})) + \left(3 \times (-0.023726\ \mathrm{kip/ft}) \times (5.5\ \mathrm{ft})^2\right)}{(6 \times (0.061465\ \mathrm{kipft/ft})) + (4 \times (-0.023726\ \mathrm{kip/ft}) \times (5.5\ \mathrm{ft}))}$$

$$a = 3.9352\ \mathrm{ft}$$

p - Earth pressure against the pile at distance a/2 from resting surface,

$$p = \frac{0.75\,[(4\,M_o) + (3\,H_o\,L_e)]^2}{L_e^2\,[(3\,M_o) + (2\,H_o\,L_e)]}$$

$$p = \frac{0.75 \times [(4 \times (0.061465\ \mathrm{kipft/ft})) + (3 \times (-0.023726\ \mathrm{kip/ft}) \times (5.5\ \mathrm{ft}))]^{\,2}}{(5.5\ \mathrm{ft})^2 \times [(3 \times (0.061465\ \mathrm{kipft/ft})) + (2 \times (-0.023726\ \mathrm{kip/ft}) \times (5.5\ \mathrm{ft}))]}$$

$$p = -0.0068643\ \mathrm{kip/ft^2}$$

s - Earth pressure against the pile at distance L_e,

$$s = \frac{6\,[(2\,M_o) + (H_o\,L_e)]}{L_e^2}$$

$$s = \frac{6 \times [(2 \times (0.061465\ \mathrm{kipft/ft})) + ((-0.023726\ \mathrm{kip/ft}) \times (5.5\ \mathrm{ft}))]}{(5.5\ \mathrm{ft})^2}$$

$$s = -0.0015002\ \mathrm{kip/ft^2}$$

Check lateral soil pressure capacity:

p_a - Allowable lateral soil pressure at depth a/2,

$$p_a = R\,\frac{a}{2}$$

$$p_a = (150\ \mathrm{psf/ft}) \times \frac{(3.9352\ \mathrm{ft})}{2}$$

$$p_a = 0.29514\ \mathrm{kip/ft^2}$$

$Ratio$ - Lateral soil capacity

$$Ratio = \frac{p}{p_a}$$

$$Ratio = \frac{\left(-0.0068643\ \mathrm{kip/ft^2}\right)}{\left(0.29514\ \mathrm{kip/ft^2}\right)}$$

$$Ratio = -0.023258$$

Status: **PASS**
Ratio: **-0.020**

p_s - Allowable lateral soil pressure at depth L_e,

$$p_s = R\,L_e$$

$$p_s = (150\ \mathrm{psf/ft}) \times (5.5\ \mathrm{ft})$$

$$p_s = 0.825\ \mathrm{kip/ft^2}$$

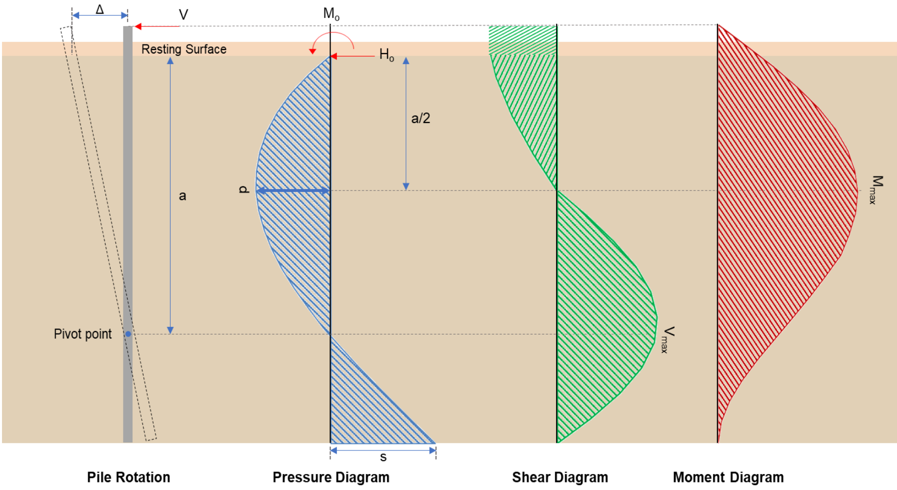
$Ratio$ - Lateral soil capacity

$$Ratio = \frac{s}{p_s}$$

$$Ratio = \frac{\left(-0.0015002\ \mathrm{kip/ft^2}\right)}{\left(0.825\ \mathrm{kip/ft^2}\right)}$$

$$Ratio = -0.0018185$$

Status: **PASS**
Ratio: **0.000**



Shear force and Bending moment (x-direction, LRFD)

H_o - Lateral force per length of pile,

$$H_o = \frac{V_x}{1.57\ D}$$

$$H_o = \frac{(-2.57\ \mathrm{kip})}{1.57 \times (48\ \mathrm{in})}$$

$$H_o = -0.40924\ \mathrm{kip/ft}$$

M_o - Moment per length of pile,

$$M_o = \frac{M_z + (V_x\ H)}{1.57\ D}$$

$$M_o = \frac{(29.441\ \mathrm{kipft}) + ((-2.57\ \mathrm{kip}) \times (0\ \mathrm{ft}))}{1.57 \times (48\ \mathrm{in})}$$

$$M_o = 4.6881\ \mathrm{kipft/ft}$$

E - Distance from lateral load to resisting surface,

$$E = \frac{M_o}{H_o}$$

$$E = \frac{(4.6881\ \mathrm{kipft/ft})}{(-0.40924\ \mathrm{kip/ft})}$$

$$E = 11.456\ \mathrm{ft}$$

a - Distance from resting surface to pivot point,

$$a = \frac{(4\ M_o\ L_e) + \left(3\ H_o\ L_e^2\right)}{(6\ M_o) + (4\ H_o\ L_e)}$$

$$a = \frac{(4 \times (4.6881\ \mathrm{kipft/ft}) \times (5.5\ \mathrm{ft})) + \left(3 \times (-0.40924\ \mathrm{kip/ft}) \times (5.5\ \mathrm{ft})^2\right)}{(6 \times (4.6881\ \mathrm{kipft/ft})) + (4 \times (-0.40924\ \mathrm{kip/ft}) \times (5.5\ \mathrm{ft}))}$$

$$a = 3.7778\ \mathrm{ft}$$

V_{max} - Max shear force located at depth a,

$$V_{max} = (H_o\ D) \left[1 - \left[3 \left(\frac{4\ E}{L_e} + 3\right) \left(\frac{a}{L_e}\right)^2\right] + \left[4 \left(\frac{3\ E}{L_e} + 2\right) \left(\frac{a}{L_e}\right)^3\right]\right]$$

$$V_{max} = ((-0.40924\ \mathrm{kip/ft}) \times (48\ \mathrm{in})) \times \left[1 - \left[3 \times \left(\frac{4 \times (11.456\ \mathrm{ft})}{(5.5\ \mathrm{ft})} + 3\right) \times \left(\frac{(3.7778\ \mathrm{ft})}{(5.5\ \mathrm{ft})}\right)^2\right] + \left[4 \times \left(\frac{3 \times (11.456\ \mathrm{ft})}{(5.5\ \mathrm{ft})} + 2\right) \times \left(\frac{(3.7778\ \mathrm{ft})}{(5.5\ \mathrm{ft})}\right)^3\right]\right]$$

$$V_{max} = 7.1143\ \mathrm{kip}$$

M_{max} - Max bending moment located at depth a/2,

$$M_{max} = (H_o\,D\,L_e)\left[\left(\frac{E}{L_e}+\frac{a}{2\,L_e}\right) - \left[\left(\frac{4\,E}{L_e}+3\right)\left(\frac{a}{2\,L_e}\right)^3\right]+\left[\left(\frac{3\,E}{L_e}+2\right)\left(\frac{a}{2\,L_e}\right)^4\right]\right]$$

$$M_{max} = ((-0.40924\text{ kip/ft})\times(48\text{ in})\times(5.5\text{ ft}))\times\left[\left(\frac{(11.456\text{ ft})}{(5.5\text{ ft})}+\frac{(3.7778\text{ ft})}{2\times(5.5\text{ ft})}\right) - \left[\left(\frac{4\times(11.456\text{ ft})}{(5.5\text{ ft})}+3\right)\times\left(\frac{(3.7778\text{ ft})}{2\times(5.5\text{ ft})}\right)^3\right]+\left[\left(\frac{3\times(11.456\text{ ft})}{(5.5\text{ ft})}+2\right)\times\left(\frac{(3.7778\text{ ft})}{2\times(5.5\text{ ft})}\right)^4\right]\right]$$

$$M_{max} = 18.745\text{ kipft}$$

Shear force and Bending moment (z-direction, LRFD)

H_o - Lateral force per length of pile,

$$H_o = \frac{V_z}{1.57\,b}$$

$$H_o = \frac{(-0.268\text{ kip})}{1.57\times(48\text{ in})}$$

$$H_o = -0.042675\text{ kip/ft}$$

M_o - Moment per length of pile,

$$M_o = \frac{M_x+(V_z\,H)}{1.57\,b}$$

$$M_o = \frac{(0.693\text{ kipft})+((-0.268\text{ kip})\times(0\text{ ft}))}{1.57\times(48\text{ in})}$$

$$M_o = 0.11035\text{ kipft/ft}$$

E - Distance from lateral load to resisting surface,

$$E = \frac{M_o}{H_o}$$

$$E = \frac{(0.11035\text{ kipft/ft})}{(-0.042675\text{ kip/ft})}$$

$$E = 2.5858\text{ ft}$$

a - Distance from resting surface to pivot point,

$$a = \frac{(4\,M_o\,L_e)+\left(3\,H_o\,L_e^2\right)}{(6\,M_o)+(4\,H_o\,L_e)}$$

$$a = \frac{(4\times(0.11035\text{ kipft/ft})\times(5.5\text{ ft}))+\left(3\times(-0.042675\text{ kip/ft})\times(5.5\text{ ft})^2\right)}{(6\times(0.11035\text{ kipft/ft}))+(4\times(-0.042675\text{ kip/ft})\times(5.5\text{ ft}))}$$

$$a = 3.9354\text{ ft}$$

V_{max} - Max shear force located at depth a,

$$V_{max} = (H_o\,b)\left[1-\left[3\left(\frac{4\,E}{L_e}+3\right)\left(\frac{a}{L_e}\right)^2\right]+\left[4\left(\frac{3\,E}{L_e}+2\right)\left(\frac{a}{L_e}\right)^3\right]\right]$$

$$V_{max} = ((-0.042675\text{ kip/ft})\times(48\text{ in}))\times\left[1-\left[3\times\left(\frac{4\times(2.5858\text{ ft})}{(5.5\text{ ft})}+3\right)\times\left(\frac{(3.9354\text{ ft})}{(5.5\text{ ft})}\right)^2\right]+\left[4\times\left(\frac{3\times(2.5858\text{ ft})}{(5.5\text{ ft})}+2\right)\times\left(\frac{(3.9354\text{ ft})}{(5.5\text{ ft})}\right)^3\right]\right]$$

$$V_{max} = 0.25585\text{ kip}$$

M_{max} - Max bending moment located at depth a/2,

$$M_{max} = (H_o\,b\,L_e)\left[\left(\frac{E}{L_e}+\frac{a}{2\,L_e}\right) - \left[\left(\frac{4\,E}{L_e}+3\right)\left(\frac{a}{2\,L_e}\right)^3\right]+\left[\left(\frac{3\,E}{L_e}+2\right)\left(\frac{a}{2\,L_e}\right)^4\right]\right]$$

$$M_{max} = ((-0.042675\text{ kip/ft})\times(48\text{ in})\times(5.5\text{ ft}))\times\left[\left(\frac{(2.5858\text{ ft})}{(5.5\text{ ft})}+\frac{(3.9354\text{ ft})}{2\times(5.5\text{ ft})}\right) - \left[\left(\frac{4\times(2.5858\text{ ft})}{(5.5\text{ ft})}+3\right)\times\left(\frac{(3.9354\text{ ft})}{2\times(5.5\text{ ft})}\right)^3\right]+\left[\left(\frac{3\times(2.5858\text{ ft})}{(5.5\text{ ft})}+2\right)\times\left(\frac{(3.9354\text{ ft})}{2\times(5.5\text{ ft})}\right)^4\right]\right]$$

$$M_{max} = 0.61992 \text{ kipft}$$

Minimum Reinforcement Check (LRFD)

Parameters:

$f'_{ck} = 2.5 \text{ ksi}$ - Concrete strength,
$f_{yk} = 60 \text{ ksi}$ - Longitudinal reinforcement strength,
$\phi = 0.65$ - Reduction factor for axial strength,
Table 22.4.2.1 $\alpha = 0.8$ - Alpha factor for axial strength,
$A_g = 2304 \text{ in}^2$ - Gross area of concrete,

Longitudinal reinforcement:

Required reinforcement due to axial load, $A_{st,required}$
22.4.2.2, 10.6.1.1 $A_{st,required}$

$$A_{st,required} = Min\left[\frac{\frac{P}{\phi\ \alpha} - \left(0.85\ f'_{ck}\ A_g\right)}{f_{yk} - \left(0.85\ f'_{ck}\right)}, \left(0.08\ A_g\right)\right]$$

$$A_{st,required} = Min\left[\frac{\frac{(14.071 \text{ kip})}{(0.65)\times(0.8)} - \left(0.85 \times (2.5 \text{ ksi}) \times \left(2304 \text{ in}^2\right)\right)}{(60 \text{ ksi}) - (0.85 \times (2.5 \text{ ksi}))}, \left(0.08 \times \left(2304 \text{ in}^2\right)\right)\right]$$

$$A_{st,required} = -84.129 \text{ in}^2$$

A_{min} - Governing minimum reinforcement area,

$$A_{min} = Max\left[A_{st,required}, \left(0.0018\ A_g\right)\right]$$

$$A_{min} = Max\left[\left(-84.129 \text{ in}^2\right), \left(0.0018 \times \left(2304 \text{ in}^2\right)\right)\right]$$

$$A_{min} = 4.1472 \text{ in}^2$$

n_{rebar} - Required number of reinforcement,

$$n_{rebar} = \frac{A_{min}}{A_{rebar}}$$

$$n_{rebar} = \frac{\left(4.1472 \text{ in}^2\right)}{\left(0.3068 \text{ in}^2\right)}$$

$$n_{rebar} = 14$$

A_{st} - Actual total reinforcement area,

$$A_{st} = n_{rebar}\ \frac{\pi\ d_{bar}^2}{4}$$

$$A_{st} = (14) \times \frac{\pi \times (0.625 \text{ in})^2}{4}$$

$$A_{st} = 4.2951 \text{ in}^2$$

$Ratio$ - Capacity

$$Ratio = \frac{A_{min}}{A_{st}}$$

$$Ratio = \frac{\left(4.1472 \text{ in}^2\right)}{\left(4.2951 \text{ in}^2\right)}$$

$$Ratio = 0.96556$$

Status: **PASS**
Ratio: **0.970**

25.2.3 s_{rebar} - Minimum spacing of reinforcement,

$$s_{rebar} = Max\left[1.5, \left(1.5\ d_{bar}\right)\right]$$

$$s_{rebar} = Max\left[1.5, (1.5 \times (0.625 \text{ in}))\right]$$

$$s_{rebar} = 1.5 \text{ in}$$

Ties:

25.7.2.2 Since longitudinal reinforcement is $\leq$ No. 10ø: Use #3(0.375 in)
25.7.2.1 s_{ties} - Maximum spacing of ties,

$$s_{ties} = Min\left[\left(16\ d_{bar}\right), \left(48\ d_{ties}\right), Min\left(D, b\right)\right]$$

$$s_{ties} = Min\left[(16 \times (0.625 \text{ in})), (48 \times (0.375 \text{ in})), Min\left((48 \text{ in}), (48 \text{ in})\right)\right]$$

$$s_{ties} = 10 \text{ in}$$

Summary:

Main reinforcement: **14 - #5 (0.625 in)**

	Ties: **#3(0.375 in) - 10 in**	

Axial Compression Strength (ACI 318-19, LRFD)

22.4.2.2 ϕP_N - Allowable axial compressive strength

$$\phi P_N = \phi\, 0.80\ \left[\left(0.85\, f'_{ck}\ \left[A_g - A_{st}\right]\right) + \left(f_{yk}\ A_{st}\right)\right]$$

$$\phi P_N = (0.65) \times 0.80 \times \left[\left(0.85 \times (2.5\ \mathrm{ksi}) \times \left[\left(2304\ \mathrm{in}^2\right) - \left(4.2951\ \mathrm{in}^2\right)\right]\right) + \left((60\ \mathrm{ksi}) \times \left(4.2951\ \mathrm{in}^2\right)\right)\right]$$

$$\phi P_N = 2675.2\ \mathrm{kip}$$

$Ratio$ - Capacity

$$Ratio = \frac{P}{\phi P_N}$$

$$Ratio = \frac{(14.071\ \mathrm{kip})}{(2675.2\ \mathrm{kip})}$$

$$Ratio = 0.0052598$$

Status: **PASS**
Ratio: **0.010**

Shear Strength (ACI 318-19, LRFD)

Parameters:

$b_w = 48\ \mathrm{in}$ - Effective width,

22.5.2.2 d - Effective depth

$$d = 0.80\ D$$

$$d = 0.80 \times (48\ \mathrm{in})$$

$$d = 38.4\ \mathrm{in}$$

22.5.5.1.3 λ_s - size effect modification factor

$$\lambda_s = MIN\left[\sqrt{\frac{2}{1 + \frac{d}{10}}}, 1\right]$$

$$\lambda_s = MIN\left[\sqrt{\frac{2}{1 + \frac{(38.4\ \mathrm{in})}{10}}}, 1\right]$$

$$\lambda_s = 0.64282$$

The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5\ \mathrm{ksi} \to 2500\ \mathrm{psi}$,

22.5.5.1.1 $V_{c,max}$ - Max shear strength of concrete

$$V_{c,max} = 5\ \lambda_s\ \sqrt{f'_{ck}}\ b_w\ d$$

$$V_{c,max} = 5 \times (0.64282) \times \sqrt{(2500\ \mathrm{psi})} \times (48\ \mathrm{in}) \times (38.4\ \mathrm{in})$$

$$V_{c,max} = 296.21\ \mathrm{kip}$$

The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5\ \mathrm{ksi} \to 2500\ \mathrm{psi}$, $P = 14.071\ \mathrm{kip} \to 14071\ \mathrm{lbf}$,

22.5.5.1.1(a) $V_{c,a}$ - Shear strength of concrete (a)

$$V_{c,a} = \left[2\ \lambda_s\ \sqrt{f'_{ck}} + \frac{P}{6\ A_g}\right]\ b_w\ d$$

$$V_{c,a} = \left[2 \times (0.64282) \times \sqrt{(2500\ \mathrm{psi})} + \frac{(14071\ \mathrm{lbf})}{6 \times (2304\ \mathrm{in}^2)}\right] \times (48\ \mathrm{in}) \times (38.4\ \mathrm{in})$$

$$V_{c,a} = 120.36\ \mathrm{kip}$$

The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5\ \mathrm{ksi} \to 2500\ \mathrm{psi}$,

22.5.5.1.2 $V_{c,b}$ - Shear strength of concrete (b)

$$V_{c,b} = \left[2\ \lambda_s\ \sqrt{f'_{ck}} + \left(0.05\ f'_{ck}\right)\right]\ b_w\ d$$

$$V_{c,b} = \left[2 \times (0.64282) \times \sqrt{(2500\ \mathrm{psi})} + (0.05 \times (2500\ \mathrm{psi}))\right] \times (48\ \mathrm{in}) \times (38.4\ \mathrm{in})$$

$$V_{c,b} = 348.89\ \mathrm{kip}$$

V_c - Governing shear strength of concrete

$$V_c = Min\left[V_{c,max}, V_{c,a}, V_{c,b}\right]$$

$$V_c = Min\left[(296.21\ \mathrm{kip}), (120.36\ \mathrm{kip}), (348.89\ \mathrm{kip})\right]$$

$$V_c = 120.36\ \mathrm{kip}$$

The following variables were converted to be consistent with empirical formula $f'_{ck} = 2.5\ \mathrm{ksi} \rightarrow 2500\ \mathrm{psi}$,

22.5.1.2 $V_{s,a}$ - Shear strength of steel (a)

$$V_{s,a} = 8 \sqrt{f'_{ck}}\, b_w\, d$$

$$V_{s,a} = 8 \times \sqrt{(2500\ \mathrm{psi})} \times (48\ \mathrm{in}) \times (38.4\ \mathrm{in})$$

$$V_{s,a} = 737.28\ \mathrm{kip}$$

A_v - Ties rebar area,

$$A_v = \frac{\pi\, d_{ties}^2}{4}$$

$$A_v = \frac{\pi \times (0.375\ \mathrm{in})^2}{4}$$

$$A_v = 0.11045\ \mathrm{in}^2$$

22.5.8.5.3 $V_{s,b}$ - Shear strength of steel (b)

$$V_{s,b} = \frac{2\, A_v\, f_{ywk}\, d}{s_{ties}}$$

$$V_{s,b} = \frac{2 \times \left(0.11045\ \mathrm{in}^2\right) \times (60\ \mathrm{ksi}) \times (38.4\ \mathrm{in})}{(10\ \mathrm{in})}$$

$$V_{s,b} = 50.894\ \mathrm{kip}$$

V_s - Governing shear strength of steel

$$V_s = MIN\left[V_{s,a}, V_{s,b}\right]$$

$$V_s = MIN\left[(737.28\ \mathrm{kip}), (50.894\ \mathrm{kip})\right]$$

$$V_s = 50.894\ \mathrm{kip}$$

22.5.1.1 ϕV_n - Allowable shear strength

$$\phi V_n = \phi\ (V_c + V_s)$$

$$\phi V_n = (0.65) \times ((120.36\ \mathrm{kip}) + (50.894\ \mathrm{kip}))$$

$$\phi V_n = 111.32\ \mathrm{kip}$$

Considering x-direction:

$V_{max} = 7.1143\ \mathrm{kip}$ - Maximum shear force in the x-direction,
$Ratio$ - Capacity

$$Ratio = \frac{V_{max}}{\phi V_n}$$

$$Ratio = \frac{(7.1143\ \mathrm{kip})}{(111.32\ \mathrm{kip})}$$

$$Ratio = 0.063911$$

Status: **PASS**
Ratio: **0.060**

Considering z-direction:

$V_{max} = 0.25585\ \mathrm{kip}$ - Maximum shear force in the z-direction,
$Ratio$ - Capacity

$$Ratio = \frac{V_{max}}{\phi V_n}$$

$$Ratio = \frac{(0.25585\ \mathrm{kip})}{(111.32\ \mathrm{kip})}$$

$$Ratio = 0.0022984$$

Status: **PASS**
Ratio: **0.000**

Flexural Strength (ACI 318-19, LRFD)

S_m - Section modulus

$$S_m = \frac{b\, D^2}{6}$$

$$S_m = \frac{(48\ \mathrm{in}) \times (48\ \mathrm{in})^2}{6}$$

$$S_m = 18432\ \mathrm{in}^3$$

	$\lambda = 1$ - Concrete modification factor (Normal concrete), Allowable flexural strength: M_n shall be the lesser of: $\phi M_{n,1}$ $$\phi M_{n,1} = \phi \times 5 \times \lambda \times \sqrt{(f_c')} \times S_m$$ $$\phi M_{n,1} = 0.65 \times 5 \times 1 \times \sqrt{(2.5ksi)} \times 18432.001in^3$$ $$\phi M_{n,1} = 249.600kipft$$	
14.5.2.1b	$\phi M_{n,2}$ $$\phi M_{n,2} = \phi\, 0.85\, f_{ck}'\, S_m$$ $$\phi M_{n,2} = (0.65) \times 0.85 \times (2.5\ \mathrm{ksi}) \times \left(18432\ \mathrm{in}^3\right)$$ $$\phi M_{n,2} = 2121.6\ \mathrm{kipft}$$ Therefore, ϕM_n - Allowable flexural strength, $$\phi M_n = MIN[\phi M_{n,1}, \phi M_{n,2}]$$ $$\phi M_n = MIN[(249.6\ \mathrm{kipft}), (2121.6\ \mathrm{kipft})]$$ $$\phi M_n = 249.6\ \mathrm{kipft}$$ **Considering x-direction:** $M_{max} = 18.745\ \mathrm{kipft}$ - Maximum moment in the x-direction, $Ratio$ - Capacity $$Ratio = \frac{M_{max}}{\phi M_n}$$ $$Ratio = \frac{(18.745\ \mathrm{kipft})}{(249.6\ \mathrm{kipft})}$$ $$Ratio = 0.0751$$	Status: **PASS** Ratio: **0.080**
	Considering z-direction: $M_{max} = 0.61992\ \mathrm{kipft}$ - Maximum moment in the z-direction, $Ratio$ - Capacity $$Ratio = \frac{M_{max}}{\phi M_n}$$ $$Ratio = \frac{(0.61992\ \mathrm{kipft})}{(249.6\ \mathrm{kipft})}$$ $$Ratio = 0.0024836$$	Status: **PASS** Ratio: **0.000**